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Heavy flavor theory overview



Second workshop on advancing the understanding of non-perturbative QCD using energy flow CFNS, Stony Brook, NY / Online November 6-9, 2023



Outline of the talk

Heavy flavor in elementary collisions
Heavy flavor in reactions with nuclei
Conclusions



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Heavy flavor in elementary collisions



Heavy flavor schemes and effects on PDF extraction

Treatment of charm, beauty, and top in perturbative QCD

S. Alekhin et al . (2020)

$$\begin{split} F_{2,h}^{FFN} &= \sum_{k=1}^{\infty} a_s^k(n_f) \sum_{i=q,g} H_{2,i}^{(k)}(n_f) \otimes f_i(n_f) \,, \\ F_{2,h}^{ZMVFN} &= \sum_{k=0}^{\infty} a_s^k(n_f+1) \sum_{i=q,g,h} C_{2,i}^{(k)}(n_f+1) \otimes f_i(n_f+1) \end{split}$$

Fixed flavor schemes – typically at low virtualities

Variable flavor schemes – as one goes to higherenergies, effectively resum Q_2/m_2c (or Q_2/m_2b)

- Different schemes and different prescriptions in the variable flavor number scheme ACOT, S-ACOT, RT, FONLL, ...
- Critical assessment and comparisons will be necessary for the EIC





-0.0

-0.0



Machine learning applications for subtle signals in hadron structure. New analysis adds to hints from baseline dataset



Can be tested by F₂^{charm} at the EIC

 Opportunity to develop phenomenology / strategies to search for intrinsic charm at the the EIC

Intrinsic charm can be reflected in the nuclear modification of J/ Ψ at forward rapidity/x_F/x. Example of p+A reactions with 0.1%, 0.3%, and 1% intrinsic charm

intrinsic

NNPDF Collab. (2022)

- Extraction of intrinsic charm compared to models
- Effect of EMC and LHCb Z+c jet data on IC statistical significance (3σ)

T. Hobbs et al . (2017)



R. Vogt. (2021)

Heavy meson production



 $40 \text{ GeV} < p_T^{\text{jet}} < 50 \text{ GeV}$

0.4 0.5 0.6 0.7 0.8

z_h

aluor

0.02

0.01

1.5

0.5

1.5

0.5

: D_i^{D^{*+}}(z,μ²)

rel. uncertainty

rel. uncertainty

Charm and beauty jet production

 Recent advances are based in SCET – precision theory for small radius jets and heavy flavor jets based on semiinclusive jet functions

$$E_J \frac{d^3\sigma}{d^3P_J} = \frac{1}{S} \sum_{i,f} \int_0^1 \frac{dx}{x} \int_0^1 \frac{dz}{z^2} f^{i/N}(x,\mu) J_{J_Q/f}(z,p_T R,m,\mu) \left[\hat{\sigma}_{i\to f} + f_{\text{ren}}^{\gamma/\ell} \left(\frac{-t}{s+u},\mu\right) \hat{\sigma}^{\gamma i\to f}\right]$$

The SiJFs Evolve according to DGLAP-like equations

scales

Jet

Nucleus

Electron



B-jet production – example from pp collisions



- So far tested in pp. Data are consistent with the theoretical predictions
- For the ratio b-jets to inclusive jets the difference between NLO+LL and NLO can be traced also to the differences in the inclusive jet cross section

H. Li et al. (2018)

Heavy flavor jet substructure



Production of quarkonia and NRQCD



Opportunities in p+p and e+p





Use quarkonium production in jets to constrain LDMEs. Around mid-rapidity

R. Bain *et al.* (2017)





Fragmentation mechanism, and TMD formalism at small and intermediate $\ensuremath{p_{\mathsf{T}}}$

$$\frac{d\sigma}{dy \, d^2 q_{\perp}} = \frac{4M^4 \, H(M^2, \mu^2)}{2s M^2 (N_c^2 - 1)} \, \Gamma_{\rho\sigma}^* \Gamma_{\mu\nu}(2\pi) \int d^2 \mathbf{k}_{n\perp} d^2 \mathbf{k}_{\bar{n}\perp} d^2 \mathbf{k}_{s\perp} \, \delta^{(2)} \left(\mathbf{q}_{\perp} - \mathbf{k}_{n\perp} - \mathbf{k}_{\bar{n}\perp} - \mathbf{k}_{s\perp} \right) \\
\times G_{g/A}^{\sigma\nu}(x_A, \mathbf{k}_{n\perp}, S_A; \zeta_A, \mu) \, G_{g/B}^{\rho\mu}(x_B, \mathbf{k}_{\bar{n}\perp}, S_B; \zeta_B, \mu) \, S_{\eta Q} \Big[{}^1S_0^{[1]} \Big] \left(\mathbf{k}_{s\perp}; \mu \right),$$
(16)

Non-perturbative physics captured in shape functions

M. Echevarria (2019)

S. Fleming et al. (2019)

 $\tilde{S}_{\eta_Q} \Big[{}^{1}S_0^{[1]} \Big] (\xi_T; \mu) = \frac{\tilde{S}_{\eta_Q}^{(0)} \Big[{}^{1}S_0^{[1]} \Big] (\xi_T; \mu)}{\tilde{S}(\xi_T; \mu)}$

More in TMDs:

There are other approaches at small-x to combine NRQD + CGC

M. Echevarria et al. (2007)

Quarkonium polarization

Heavy flavor in reactions with nuclei

Heavy flavor propagation in matter

Formation time of the (soft) gluon at t $\frac{1}{\Delta E} = \tau_{form} = \frac{2\omega}{(k - q_2 - q_5)^2} \qquad LPM \sim L/\tau_f$

- In this case future interactions can affect this formation time (This is a quantum coherent effect.)
- Energy loss formalisms developed and connections explored

M. Djordjevic et al. (2003)

B. Zhang et al. (2003)

N. Armesto et al. (2003)

Y. Mehtar-Tani et al. (2019)

E-loss is the soft gluon emission limit of medium-induced radiative corrections

Collisional and radiative processes for heavy quarks

Collisional energy losses

$$\frac{dE_{\rm el}}{d\Delta z} = \frac{C_F}{4} \left(1 + \frac{N_f}{6}\right) \alpha_s(ET) g_s^2 T^2 \ln\left(\frac{ET}{m_D^2}\right) \left(\frac{1}{v} - \frac{1 - v^2}{2v^2} \ln\frac{1 + v}{1 - v}\right)$$

E. Braaten et al. (1991) B. Neufeld et al. (2014)

In-medium splitting functions necessary for higher order and resumed calculations

Develop specific EFTs for particle propagation in matter

Z. Kang et al . (2016) M. Sievert et al . (2018)

$$\begin{split} & \left(\frac{dN^{\text{med}}}{dxd^{2}k_{\perp}}\right)_{Q \to Qg} = \frac{\alpha_{s}}{2\pi^{2}}C_{F}\int \frac{d\Delta z}{\lambda_{g}(z)}\int d^{2}q_{\perp}\frac{1}{\sigma_{el}}\frac{d\sigma_{el}^{\text{med}}}{d^{2}q_{\perp}} \left\{ \left(\frac{1+(1-x)^{2}}{x}\right)\left[\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\right. \\ & \left. \times \left(\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}-\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)+\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}\cdot\left(2\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}-\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\right) \\ & \left. -\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{3})\Delta z]\right)+\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\cdot\frac{C_{\perp}}{C_{\perp}^{2}+\nu^{2}}\left(1-\cos[(\Omega_{2}-\Omega_{3})\Delta z]\right) \\ & \left. +\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\cdot\left(\frac{D_{\perp}}{D_{\perp}^{2}+\nu^{2}}-\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[\Omega_{4}\Delta z]\right)-\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}\cdot\frac{D_{\perp}}{D_{\perp}^{2}+\nu^{2}}\left(1-\cos[\Omega_{5}\Delta z]\right) \\ & \left. +\frac{1}{N_{c}^{2}}\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\cdot\left(\frac{A_{\perp}}{A_{\perp}^{2}+\nu^{2}}-\frac{B_{\perp}}{B_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)\right] \\ & \left. +x^{3}m^{2}\left[\frac{1}{B_{\perp}^{2}+\nu^{2}}\cdot\left(\frac{1}{B_{\perp}^{2}+\nu^{2}}-\frac{1}{C_{\perp}^{2}+\nu^{2}}\right)\left(1-\cos[(\Omega_{1}-\Omega_{2})\Delta z]\right)+\ldots\right]\right\} \begin{array}{c} \text{Paring} \\ \text{Then is the set of t$$

- Factorize form the hard part
- Gauge-invariant
- Depend on the properties of the medium
- Can be expressed as proportional to Altarelli-Parisi

Parton showers in matter are softer and broader than the ones in the vacuum

Heavy quarks as Brownian markers of QCD matter

Low p_T diffusion and recombination

- Hierarchy of hadronic species → signature of quark recombination
- Large elliptic flow
 - \rightarrow heavy quarks "dragged" along by QCD fireball

Hadronization is very important in this region – recombination vs fragmentation. Significant differences reman that are being studied

Charm and beauty jet production in HI collisions

The semi-inclusive jet function formalism for HF jets can be extended to heavy ion collisions

H. Li et al. (2019)

Collisional E-losses

$$J_{J_Q/i}^{\text{med},(0)}(z, p_T, \delta p_T^i) = z\delta_{iQ} \left[\delta \left(1 - z - \frac{\delta p_T^i}{p_T + \delta p_T^i} \right) - \delta(1 - z) \right]$$

Radiation: after summing over all diagrams

$$\begin{split} J_{J_Q/Q}^{\text{med},(1)}(z, p_T R, m, \mu) &= \left[\int_{z(1-z)p_T R}^{\mu} dq_{\perp} P_{QQ}^{\text{med}}(z, m, q_{\perp}) \right]_+ \\ J_{J_s/g}^{\text{med},(1)}(z, p_T R, m, \mu) &= \left[\int_{z(1-z)p_T R}^{\mu} dq_{\perp} P_{Qg}^{\text{med}}(z, m, q_{\perp}) \right]_+ + \int_{z(1-z)p_T R}^{\mu} dq_{\perp} P_{Qg}^{\text{med}}(z, m, q_{\perp}) \end{split}$$

- In addressing heavy flavor quenching, care should be taken in accounting for the significant gluon contribution to the charm and beauty production
- Control over the relative contribution of CNM effects, radiative and collisional energy losses is important
 - Significant effort is needed to understand the transition form the low p_T diffusive regime

Heavy flavor jet substructure

At RHIC jet energies, and at lower jet energies at the LHC there is a unique reversal of the mass hierarchy of jet quenching effects on jet substructure On can extend the studies to D and B meson transverse and longitudinal profile modification in jets and look for signatures of the dead cone effect in A+A

Heavy flavor at the EIC and the physics of hadronization

EIC theory will provide clear new insights into hadronization from light + heavy flavor

Highlighted in the 2023 LRP

Heavy flavor jets at EIC and centrality dependence

Jet measurements can benefit both nPDF extraction and understanding hadronization / nuclear matter transport properties - separate initial-state and final-state effects

Vacuum and in-medium shower differences define the ratio of modifications for 2 radii (it is a double ratio) $R_R = R_{eA}(R) / R_{eA}(R = 0.8)$

Effectively eliminates initial-state effects Final-state suppression can be almost a factor of 2 for small radii.

Centrality dependence of light and heavy flavor production at the EIC

Test the path length dependence of CNM effects

NRQCD in the nuclear medium

At the Lagrangian level

Y. Makris et al. (2019)

$$\mathcal{L}_{\mathrm{NRQCD}_G} = \mathcal{L}_{\mathrm{NRQCD}} + \mathcal{L}_{Q-G/C}(\psi, A_{G/C}^{\mu,a}) + \mathcal{L}_{g-G/C}(A_s^{\mu,b}, A_{G/C}^{\mu,a})$$

- Glauber gluons transverse to the direction of propagation contribution
- Coulomb gluons isotropic momentum distribution

$$\begin{aligned} \mathcal{L}_{Q-G/C}^{(0)}(\psi, A_{G/C}^{\mu, a}) &= \sum_{\mathbf{p}, \mathbf{q}_{T}} \psi_{\mathbf{p}+\mathbf{q}_{T}}^{\dagger} \left(-gA_{G/C}^{0} \right) \psi_{\mathbf{p}} \ (collinear/static/soft). \\ \mathcal{L}_{Q-G}^{(1)}(\psi, A_{G}^{\mu, a}) &= g \sum_{\mathbf{p}, \mathbf{q}_{T}} \psi_{\mathbf{p}+\mathbf{q}_{T}}^{\dagger} \left(\frac{2A_{G}^{\mathbf{n}}(\mathbf{n} \cdot \boldsymbol{\mathcal{P}}) - i \left[(\boldsymbol{\mathcal{P}}_{\perp} \times \mathbf{n}) A_{G}^{\mathbf{n}} \right] \cdot \boldsymbol{\sigma}}{2m} \right) \psi_{\mathbf{p}} \ (collinear) \\ \mathcal{L}_{Q-C}^{(1)}(\psi, A_{C}^{\mu, a}) &= 0 \ (static) \\ \mathcal{L}_{Q-C}^{(1)}(\psi, A_{C}^{\mu, a}) &= g \sum_{\mathbf{p}, \mathbf{q}_{T}} \psi_{\mathbf{p}+\mathbf{q}_{T}}^{\dagger} \left(\frac{2\mathbf{A}_{C} \cdot \boldsymbol{\mathcal{P}} + [\boldsymbol{\mathcal{P}} \cdot \mathbf{A}_{C}] - i \left[\boldsymbol{\mathcal{P}} \times \mathbf{A}_{C} \right] \cdot \boldsymbol{\sigma}}{2m} \right) \psi_{\mathbf{p}} \ (soft) \end{aligned}$$

Quarkonium transport in the QGP vs cold nuclear matter at the EIC

Dissociation rates will depend on the type of the source of scattering in the medium, but only at higher orders

In-medium heavy quarkonium propagation – open quantum systems

Probe = heavyquarkonium state Medium = light quarks and gluons that comprise the medium

 Can use open quantum systems methods and effective field theory methods to obtain quantum master equations for the evolution heavy quarkonium reduced density matrix.

Transverse-momentum

J. Boyd et al. (2023)

N. Brambilla et al. (2022)

HF programs

INT Program

July 29 - August 23, 2024 **Heavy Ion Physics in the EIC era (24-2b)** Y. T. Chien, M. Djordjevic, I. Vitev *Embedded Workshop: August 19 - 23* Expect to be in the Santa Fe area **Summer school on heavy flavor physics** J. Terry, I. Vitev *Dates: TBD – we will keep you posted*

Conclusions

- Heavy flavor production is an important driver of QCD theory. Still, many open theoretical questions remain – from relevant EFTs in multi-scale problems, to the non-perturbative HF content of nucleons and nuclei, hadronization into heavy mesons, and quarkonia. These must be resolved to fully utilize the RHIC, LHC, and EIC capabilities
- The precise analysis of HF observables suppression of D, B mesons, c,b-jets, and quarkonia; correlations; and HF jet substructure remain a priority using advanced theory that bridges the gap between high energy and nuclear physics. There are a number of dedicated efforts in the HF arena (much more so than in the light flavor and inclusive jets), including the new HEFTY NT topical collaboration
- There are new opportunities for HF physics to improve our understanding of nonperturbative aspects of QCD, develop new observables, understand the role of HQ mass on parton transport, QCD radiation, apply Bayesian statistical analysis to extract properties of cold and hot QCD matter, interface LQCD with PQCD and transport models. In order to achieve this, we must place emphasis on analytic theory. Without rigorous, systematically improvable first-principles theory the results of our numerical analyses will not be conclusive
- There are tremendous intellectual communalities in heavy flavor physics applied to hadronic, heavy ion, and DIS reactions. It is a natural point of convergence for the broad QCD community. It is important to realize and advance those connections. Now is the right time to capitalize on theory effort and investments to answer the most pressing HF questions with an eye on RHIC, LHC and the EIC

Quenching in small systems

W. Ke et al. (2022)

In small systems (e.g. pPb, dAu) ATLAS $\langle T_{pA} \rangle$ #1 ATLAS $\langle T_{pA} \rangle$ #2 ATLAS $\langle T_{pA} \rangle$ #3 azimuthal asymmetries have been ATLAS, 0-1% 0-1% 0-1% measured, interpreted as possible 2.0 Cronin+eloss+QGP Cronin+OGP ATLAS, 60-90% 60-90% 60-90% signatures of QGP formation R_{pA} , h^{\pm} Cronin+eloss+QGP Cronin+QGP 1.5 No evidence for jet quenching measurements. In fact, 1.0 incompatible with jet quenching 0.5 phenomenology 10¹ 10¹ 10¹ p_T [GeV] pT [GeV] p_T [GeV] 0-0 7.0 TeV 0-0 7.0 TeV 2.0 0-10% ▶ 0-10% 1.5 Significant interest R. Katz et al . (2020) R_{AB}, h[±] 30-50% R_{AB}, h ± 30-50% 1.5 in small symmetric 1.0 1.0 systems, such as 0.5 0.5 Without QGP ----- ¹⁶O-O 6.5 TeV OO, to better (a) With QGP 1.50 1.25 ⁴⁰Ar-Ar 5.85 TeV R_{AB}, D [±] R_{AB}, D [±] 0.150-10% constrain centrality ¹²⁹_{prol} Xe-Xe 5.44 TeV 1.25 1.00 $D^0 v_2\{2\}$ $---\frac{^{129}}{_{\rm spher.}} Xe-Xe 5.44 \text{ TeV}$ 1.00 and put limits on 0.75 0.1- ²⁰⁸Pb-Pb 5.02 TeV 0.75 the smallest OGP 1.2 1.1 0.05R_{AB}, B [±] R_{AB}, B^{\pm} droplets in nature 1.0 1.0 0.8 0.9 21050 p_T (GeV) 10² A. Huss et al . (2021) 10¹ 10¹ 10² $p_T [GeV/c]$ $p_T [GeV/c]$

Heavy flavor in transport simulations - LIDO

LIDO: partonic transport simulation of light & heavy-flavor dynamics in dense QGP

- $C_{nn}[f]$: diffusion + large-q collisions.
- $C_{n(n+1)}[f]$: induced radiation, with dynamical implementation of LPM effect.

W. Ke et al. (2019)

Recent progress made in the description of heavy flavor mesons and heavy flavor jets

Toward constraining heavy flavor dynamics with Bayesian analysis

