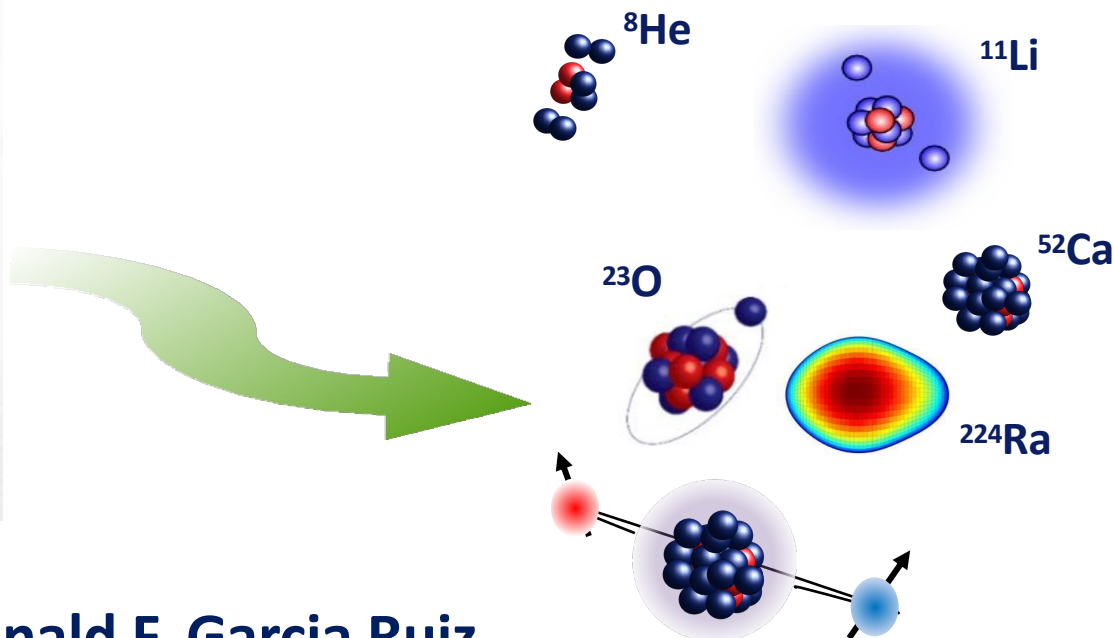




Charge radii measurements of exotic nuclei from laser spectroscopy



Figure modified from <https://sphereofinfluence360.com/>

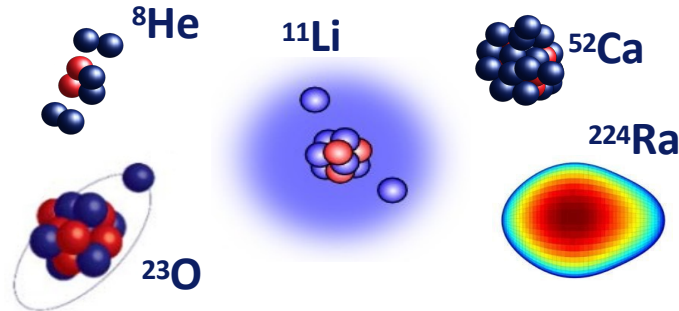


Ronald F. Garcia Ruiz
MIT

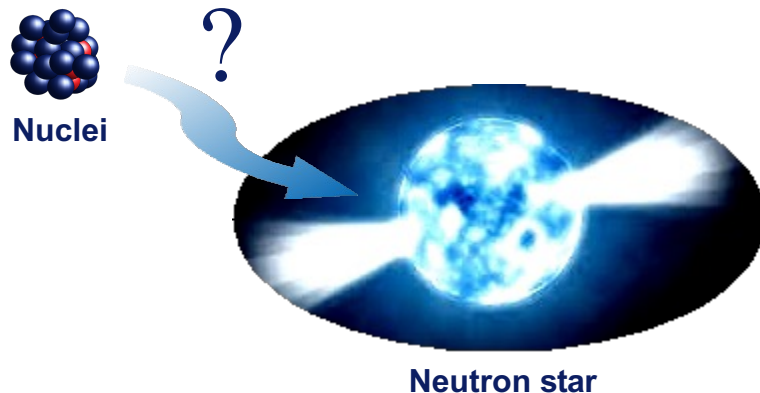
Workshop on NREC 2024
Stony Brook University, May 2024

Open questions in Nuclear and Particle Physics

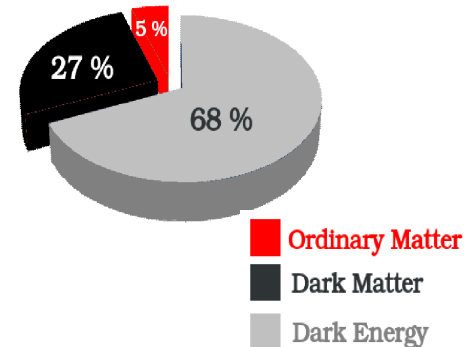
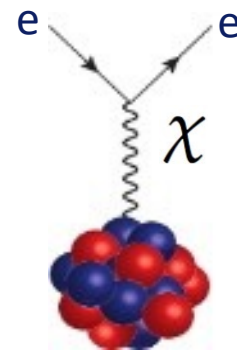
How do nuclear phenomena emerge from QCD?



What are the properties of nuclear matter (e.g. neutron stars)?



Are there new particles?
What are the properties of Dark Matter?



Isotope shift measurements of exotic nuclei can provide answers to these questions

Overview

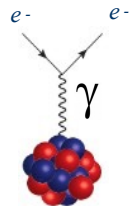
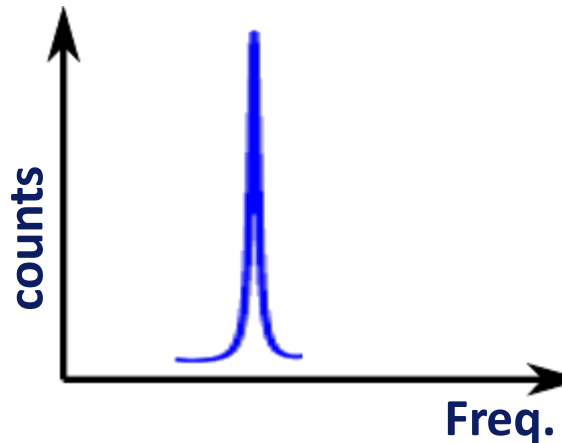
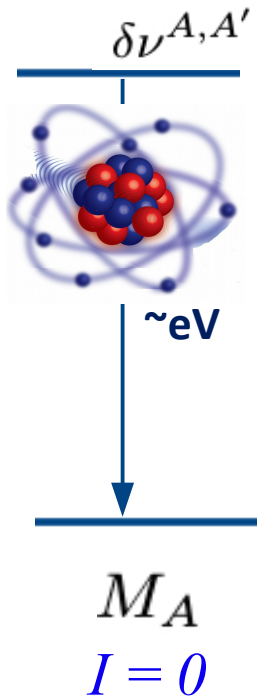
- **Laser spectroscopy**
- **Charge radii & Nuclear Structure**
- **Charge radii & Nuclear Matter**
- **Isotope shifts & BSM Physics**
- **Summary & Outlook**

[Yang, Wang, Wilkins, Garcia Ruiz. Prog. Part. Nucl. Phys. 129, 104005 (2023)]

[Koszorús, Groote, Cheal, Campbell, Moore. Eur. Phys. J. C 60, 20 (2024)]

[Nörtershäuser, Moore. Handbook Nucl. Phys 1, (2022)]

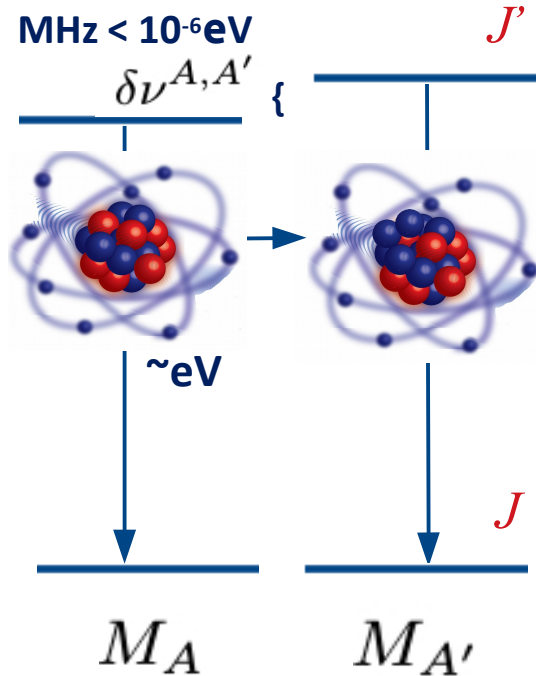
Laser spectroscopy -> Isotope Shifts



Laser spectroscopy -> Isotope Shifts

Isotope shift

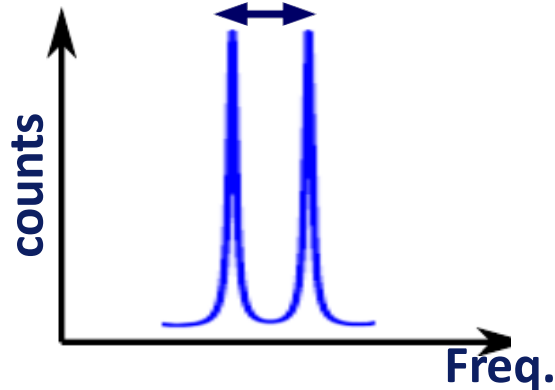
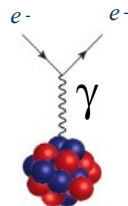
$\text{MHz} < 10^{-6} \text{eV}$



$I = 0$

$$\sim F \delta \langle r^2 \rangle^{A,A'}$$

Atom
Nuclear



$$\sim \sum_{i \neq j} \vec{p}_i \cdot \vec{p}_j$$

Mass shift

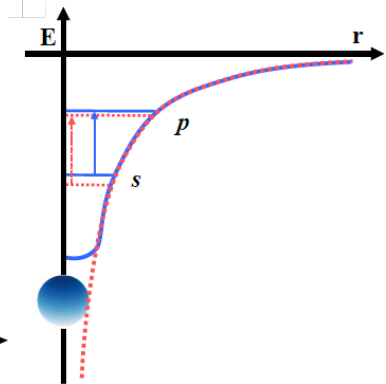
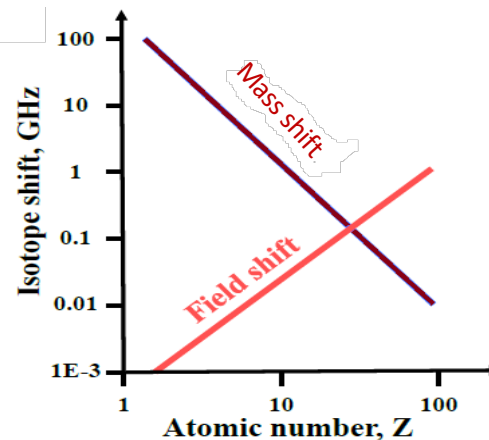
$$\sim |\psi(0)|^2$$

Field shift

$$\langle r^2 \rangle = -6 \left. \frac{dF(q)}{dq^2} \right|_{q=0}$$

rms charge radius

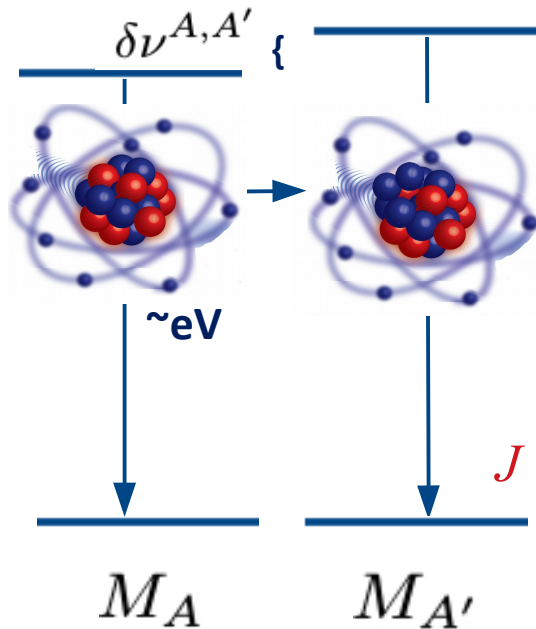
$$\delta \nu^{A,A'} = K_{MS} \frac{M_{A'} - M_A}{M_{A'} M_A} + F \delta \langle r^2 \rangle^{A,A'}$$



Laser spectroscopy -> Isotope Shifts

Isotope shift

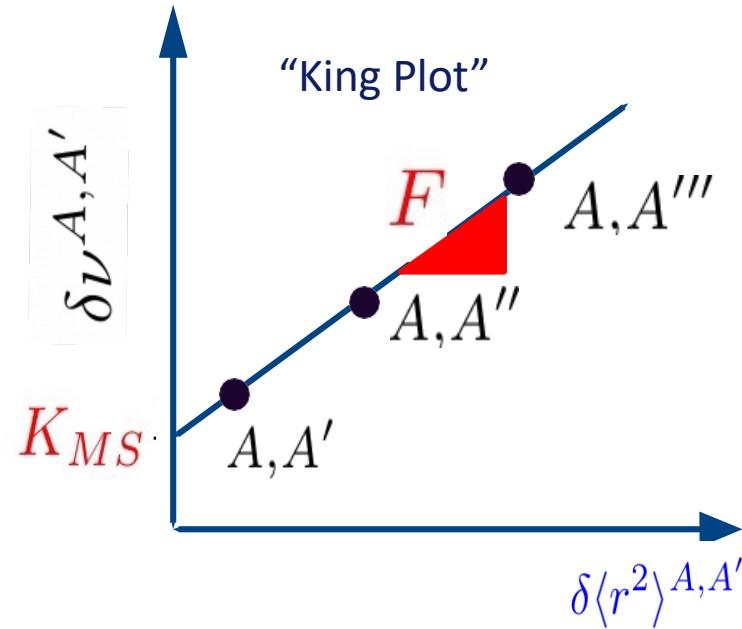
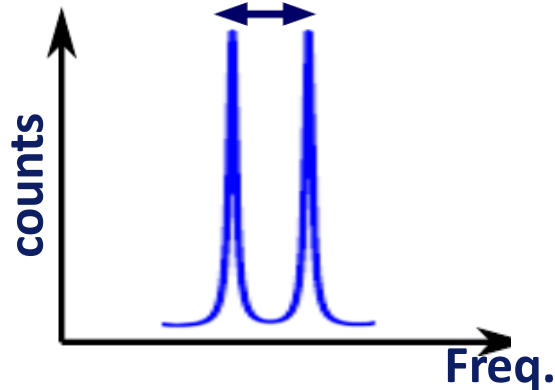
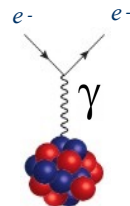
$\text{MHz} < 10^{-6} \text{eV}$



$I = 0$

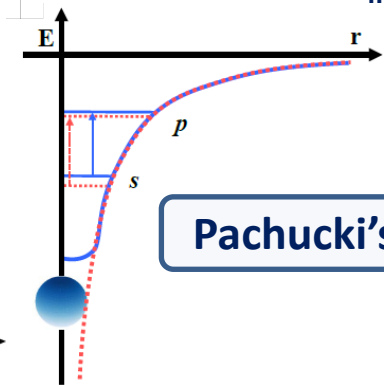
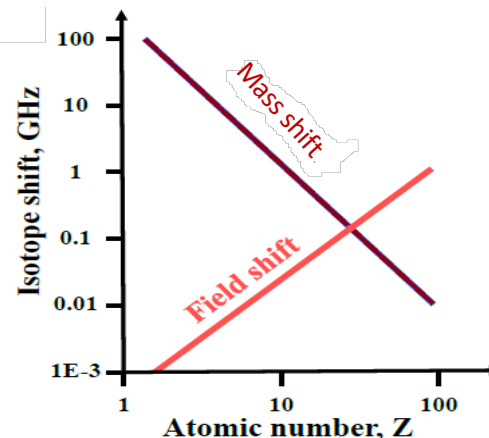
$$\sim F \delta \langle r^2 \rangle^{A,A'}$$

Atom
Nuclear



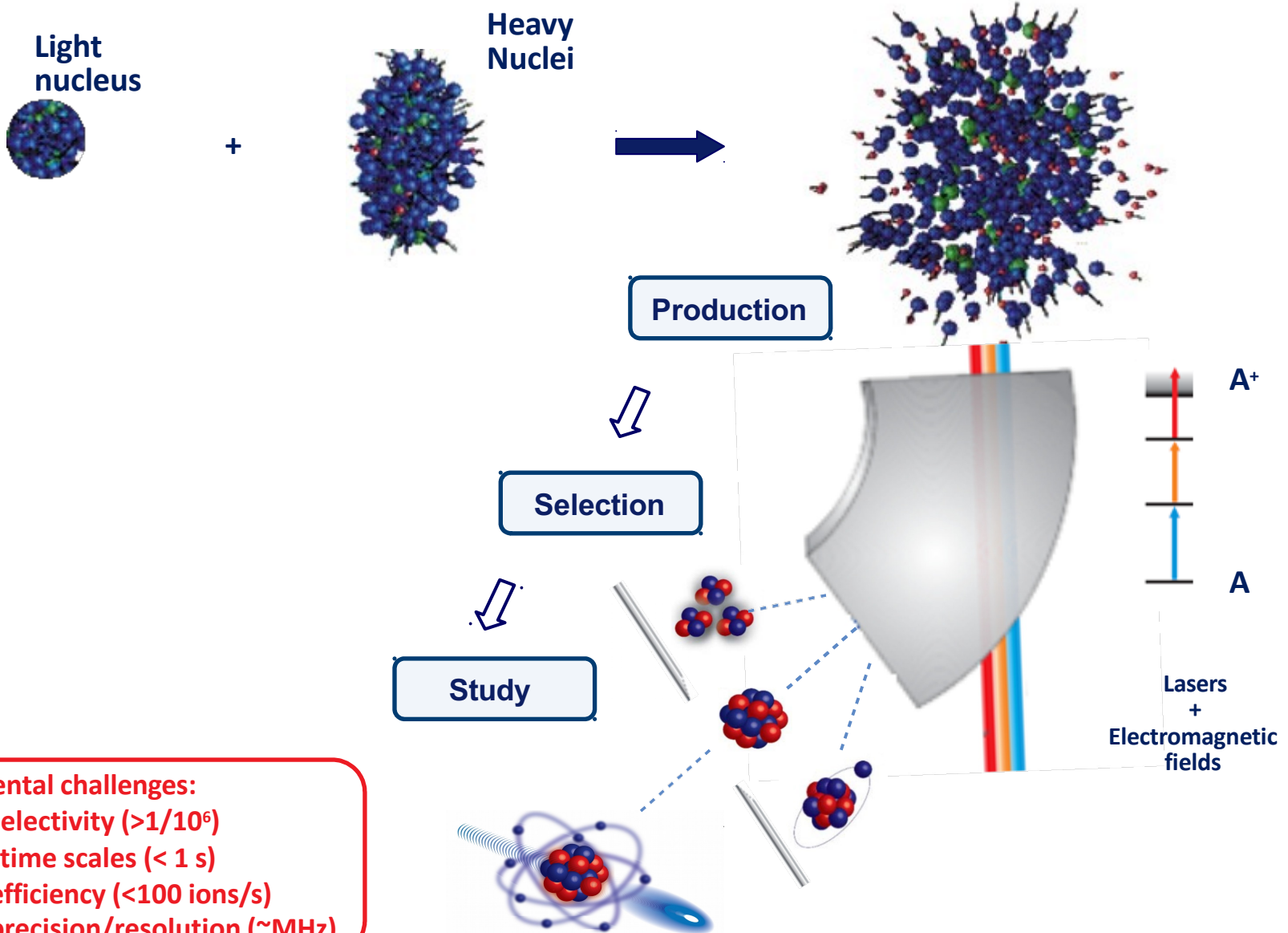
$$\delta \nu^{A,A'} = K_{MS} \frac{M_{A'} - M_A}{M_{A'} M_A} + F \delta \langle r^2 \rangle^{A,A'}$$

+
Higher order
Corrections
 $\langle r^4 \rangle$,
nuclear pol.,
...

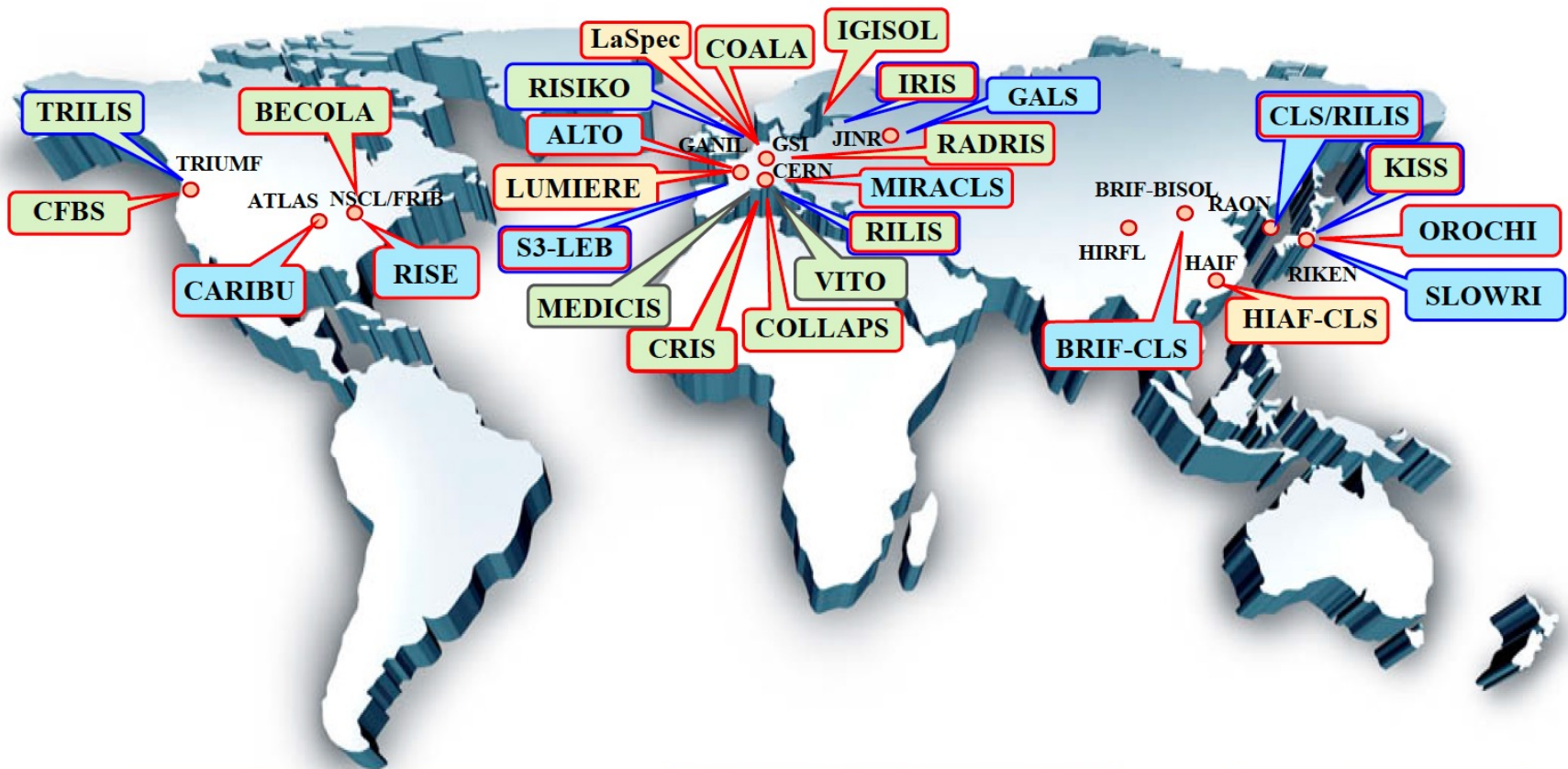


Pachucki's talk

Laser spectroscopy of Exotic Nuclei



Laser spectroscopy of Exotic Nuclei



Operational

Commissioning

Planning

Nuclear properties

Laser ion source

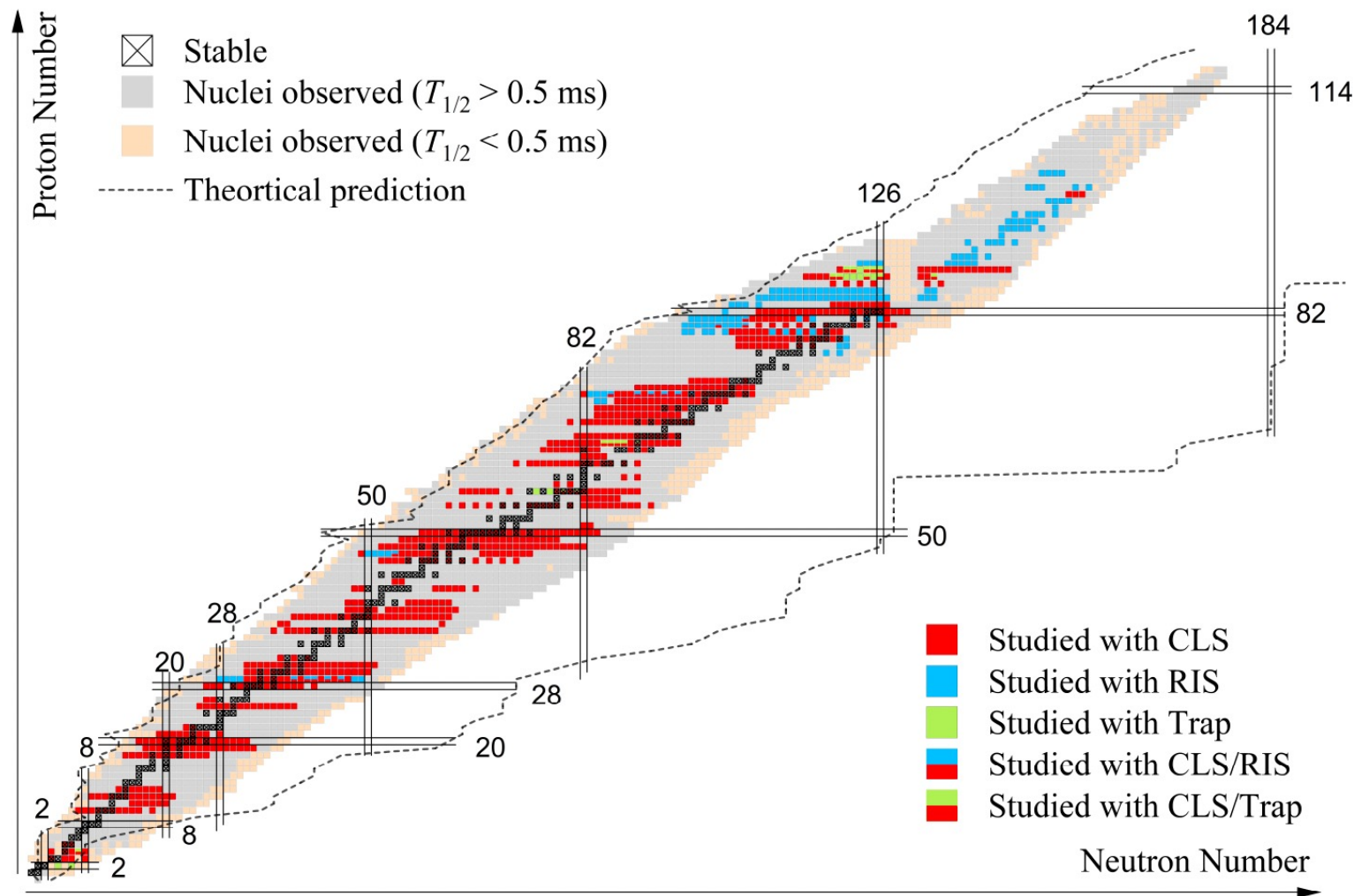
Application

Laser spectroscopy of Exotic Nuclei

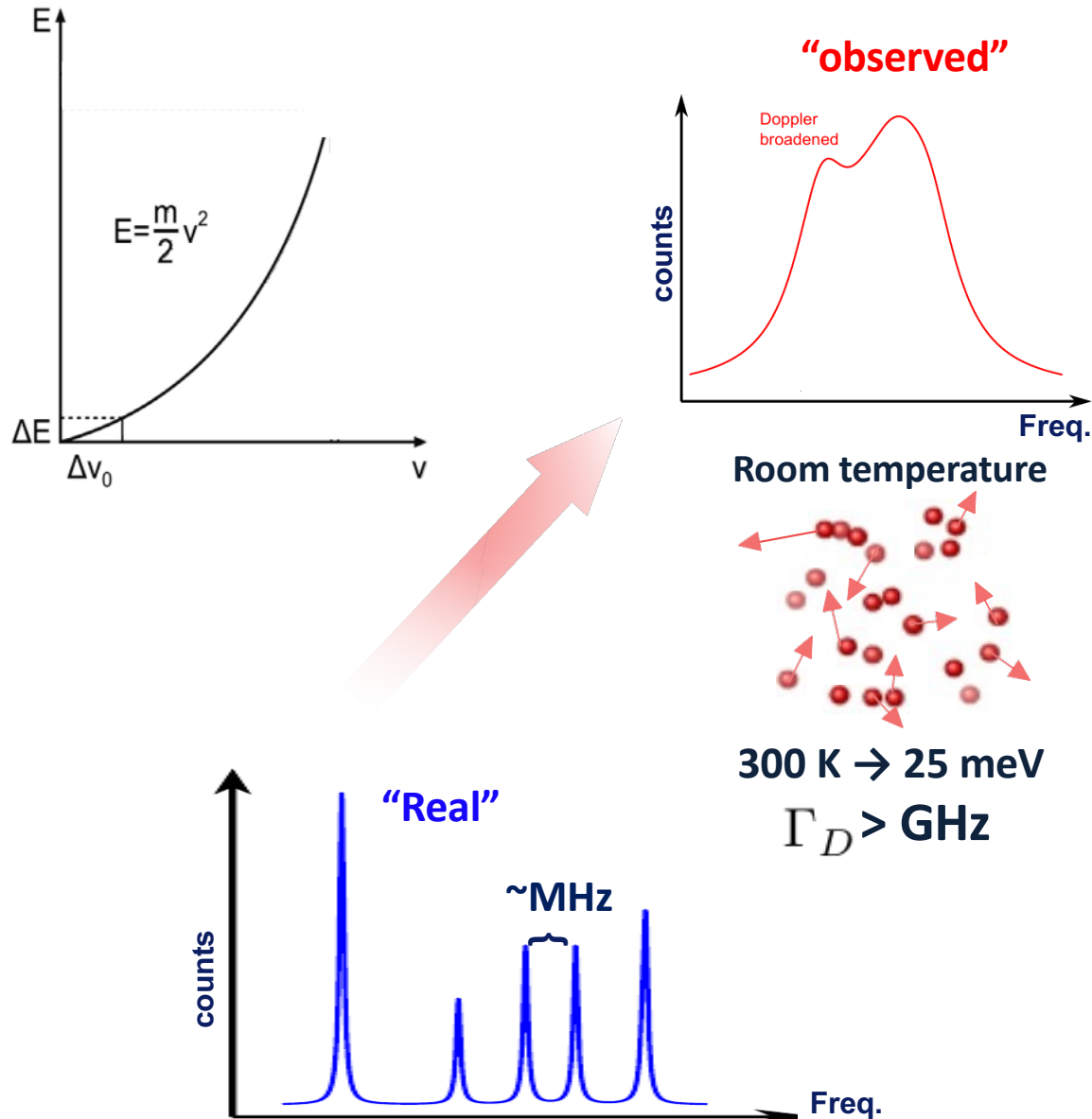
Nörtershäuser's talk
Ohayon's talk

1																	18
1 H 1.008	2	Studied by laser spectroscopy										13	14	15	16	17	2 He 4.003
3 Li 6.941	4 Be 9.012	To be studied in the current/new RI facilities										5 B 10.811	6 C 12.011	7 N 14.007	8 O 15.999	9 F 18.999	10 Ne 20.180
11 Na 22.990	12 Mg 24.305	3	4	5	6	7	8	9	10	11	12	13 Al 26.982	14 Si 28.086	15 P 30.974	16 S 32.065	17 Cl 35.453	18 Ar 39.948
19 K 39.098	20 Ca 40.078	21 Sc 44.956	22 Ti 47.867	23 V 50.942	24 Cr 51.996	25 Mn 54.938	26 Fe 55.845	27 Co 58.933	28 Ni 58.693	29 Cu 63.546	30 Zn 65.39	31 Ga 69.723	32 Ge 72.61	33 As 74.922	34 Se 78.97	35 Br 79.904	36 Kr 83.789
37 Rb 85.468	38 Sr 87.62	39 Y 88.906	40 Zr 91.224	41 Nb 92.906	42 Mo 95.95	43 Tc [98]	44 Ru 101.07	45 Rh 102.91	46 Pd 106.43	47 Ag 107.87	48 Cd 112.41	49 In 114.82	50 Sn 118.71	51 Sb 121.76	52 Te 127.60	53 I 126.90	54 Xe 131.29
55 Cs 132.91	56 Ba 137.33	57-71 *	72 Hf 178.49	73 Ta 180.95	74 W 183.84	75 Re 186.21	76 Os 190.23	77 Ir 192.22	78 Pt 195.08	79 Au 196.97	80 Hg 200.59	81 Tl 204.38	82 Pb 207.2	83 Bi 208.98	84 Po [209]	85 At [210]	86 Rn [222]
87 Fr [223]	88 Ra [226]	89-103 #	104 Rf [265]	105 Db [268]	106 Sg [271]	107 Bh [270]	108 Hs [277]	109 Mt [276]	110 Ds [281]	111 Rg [280]	112 Cn [285]	113 Nh [286]	114 Fl [289]	115 Mc [289]	116 Lv [293]	117 Ts [294]	118 Og [294]
* Lanthanide series			57 La 138.91	58 Ce 140.12	59 Pr 140.91	60 Nd 144.24	61 Pm [145]	62 Sm 150.36	63 Eu 151.96	64 Gd 157.25	65 Tb 158.93	66 Dy 162.50	67 Ho 164.91	68 Er 167.26	69 Tm 168.91	70 Yb 173.05	71 Lu 174.97
# Actinide series			89 Ac [227]	90 Th 232.01	91 Pa 231.04	92 U 238.03	93 Np [237]	94 Pu [244]	95 Am [243]	96 Cm [247]	97 Bk [247]	98 Cf [251]	99 Es [252]	100 Fm [257]	101 Md [258]	102 No [259]	103 Lr [262]

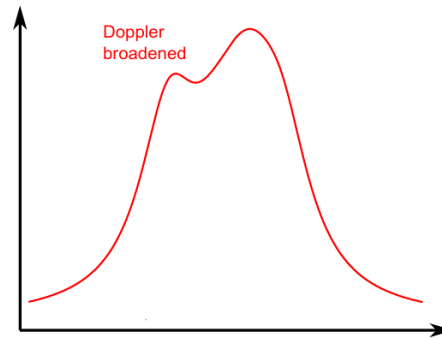
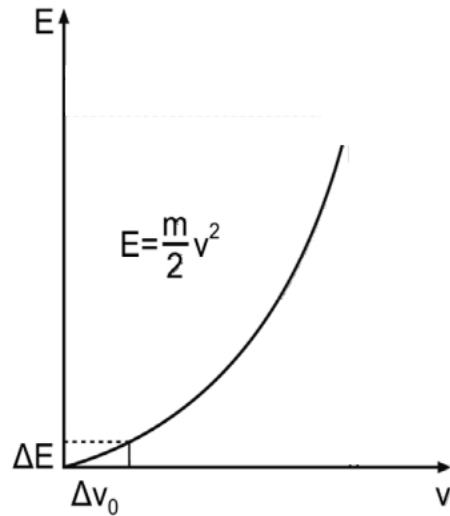
Laser spectroscopy of Exotic Nuclei



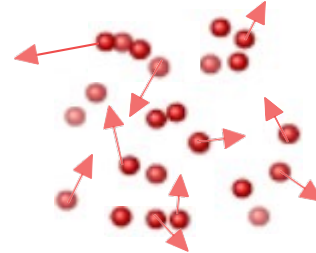
Collinear Laser spectroscopy of Exotic Nuclei



Collinear Laser spectroscopy of Exotic Nuclei

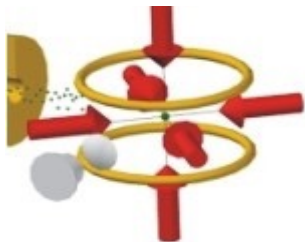


Room temperature



300 K $\rightarrow$ 25 meV

$\Gamma_D > \text{GHz}$

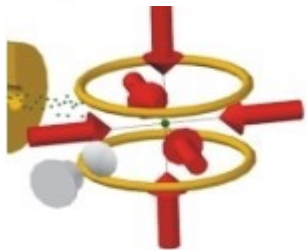
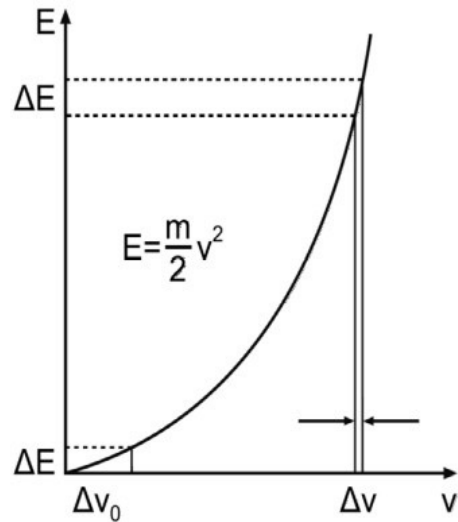


$T < \mu\text{K}$

$\Gamma_D < \text{MHz}$

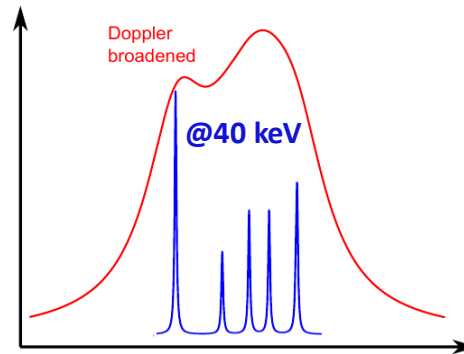
- ✓ High resolution ($< \text{MHz}$)
- High efficiency (< 100 ions/s) ?
- High selectivity ($> 1/10^6$) ?
- Short time scales (< 1 s) ?

Collinear Laser spectroscopy of Exotic Nuclei

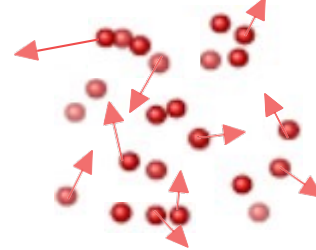


$T < \mu\text{K}$

$\Gamma_D < \text{MHz}$



Room temperature



300 K $\rightarrow$ 25 meV

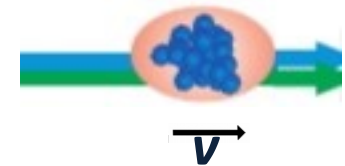
$\Gamma_D > \text{GHz}$

Energy spread

$$\Gamma_D = \nu_0 \frac{\delta E}{\sqrt{2eUmc^2}}$$

Ion beam energy

Fast beam



@ 40 keV

$\Gamma_D \sim \text{MHz}$

✓ High resolution ($< \text{MHz}$)

✓ High efficiency (< 100 ions/s) ?

✓ High selectivity ($> 1/10^6$) ?

✓ Short time scales (< 1 s) ?

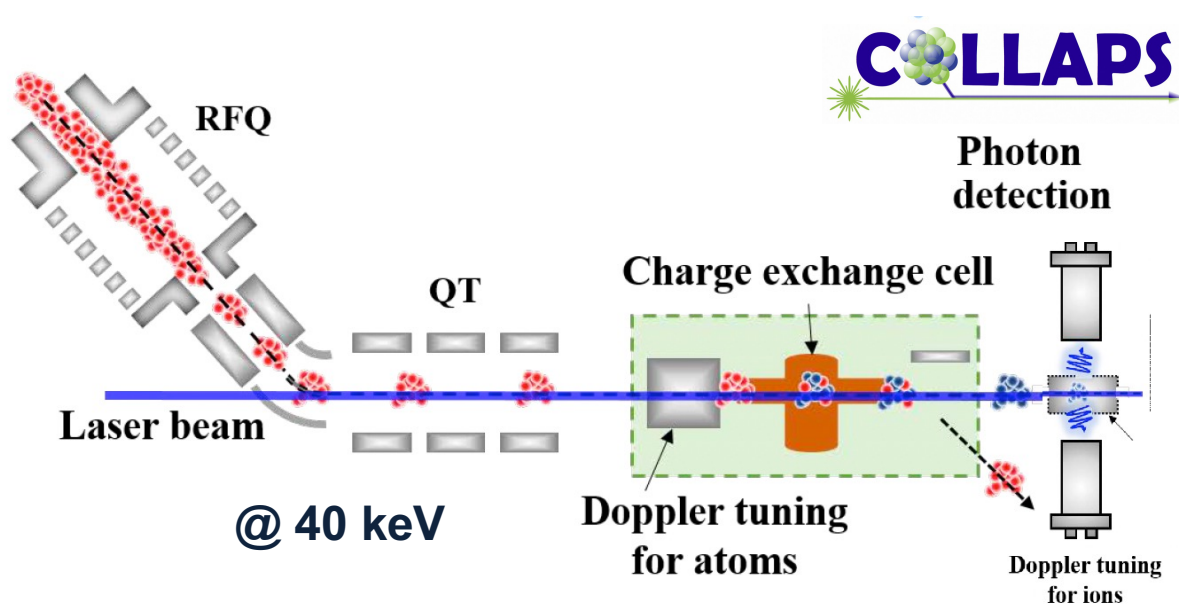
✓ High resolution ($\sim \text{MHz}$)

✓ High efficiency (< 100 ions/s)

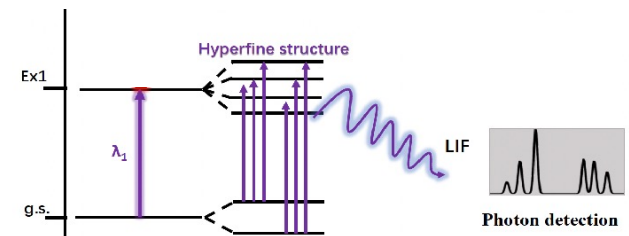
✓ High selectivity ($> 1/10^6$)

✓ Short time scales (< 1 s)

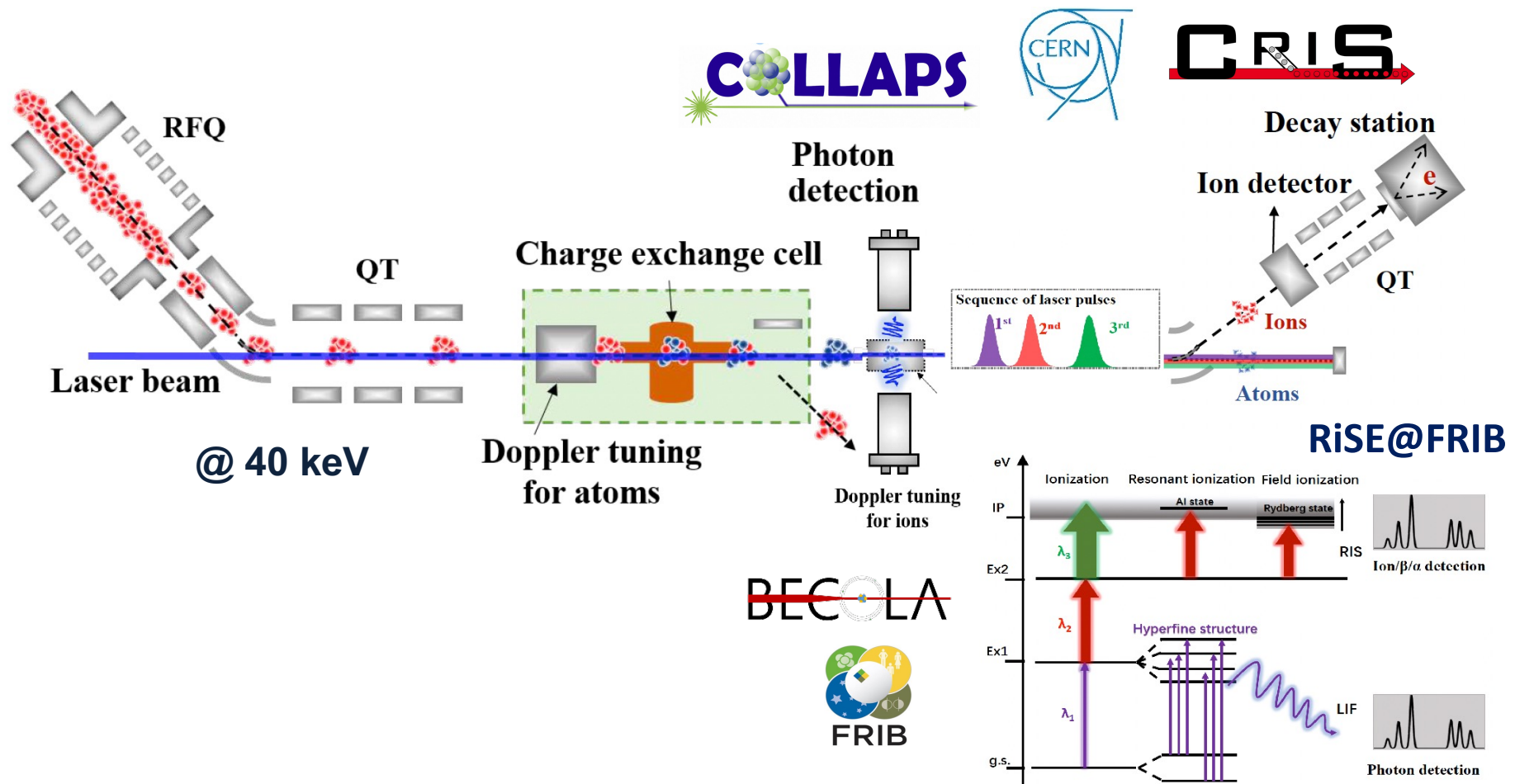
Collinear Laser spectroscopy of Exotic Nuclei



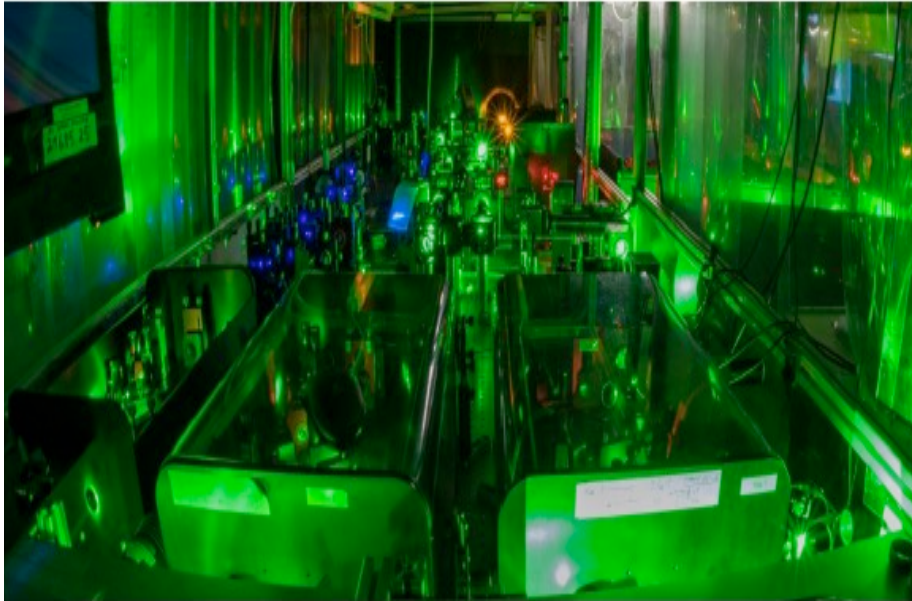
~~BECOLA~~



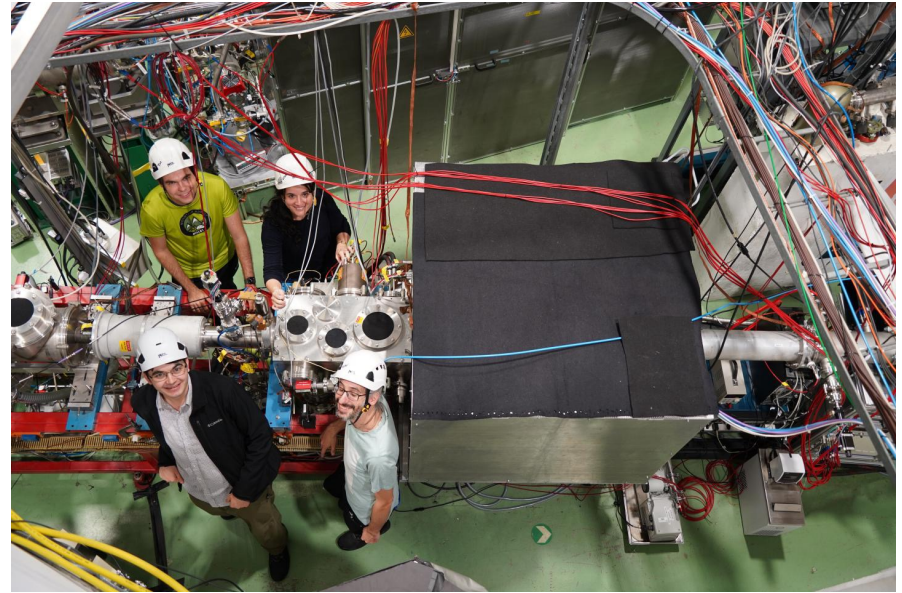
Collinear Laser spectroscopy of Exotic Nuclei



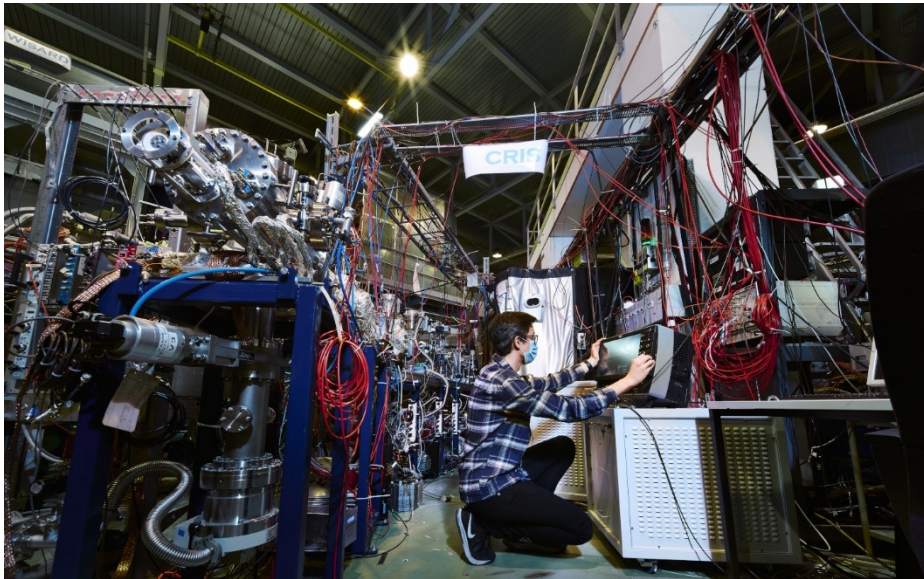
RILIS/ISOLDE @ CERN



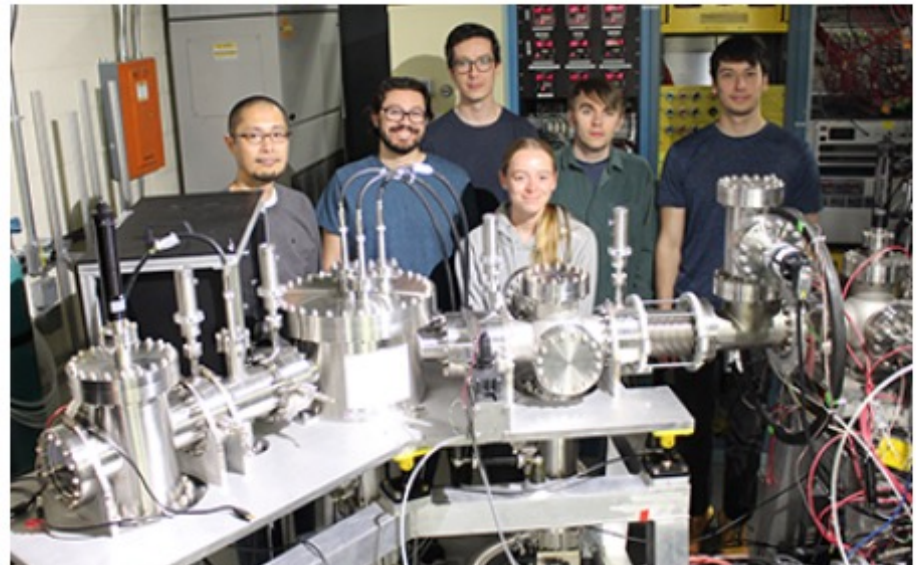
COLLAPS/ISOLDE @ CERN



CRIS/ISOLDE @ CERN



RISE/BECOLA @ FRIB



Overview

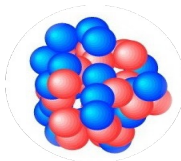
- Laser spectroscopy
- **Charge radii & Nuclear Structure**
- Charge radii & Nuclear Matter
- Isotope shifts & BSM Physics
- New Opportunities
- Summary & Outlook

Warning: A few selected results. A non-exhaustive, biased selection.

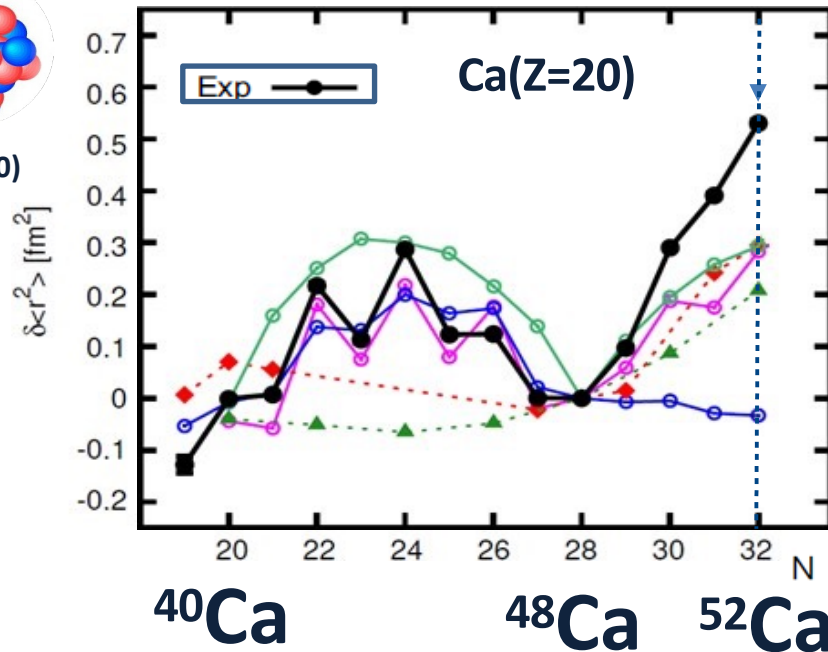
Evolution of the nuclear size away from stability

How do nuclear phenomena emerge from QCD?

[Garcia Ruiz et al., Nature Phys.12, 594 (2016)]



Ca(Z=20)



COLLAPSE

Theory
(ab-initio, shell-
model, DFT,
global fits)

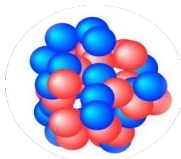
100LDE



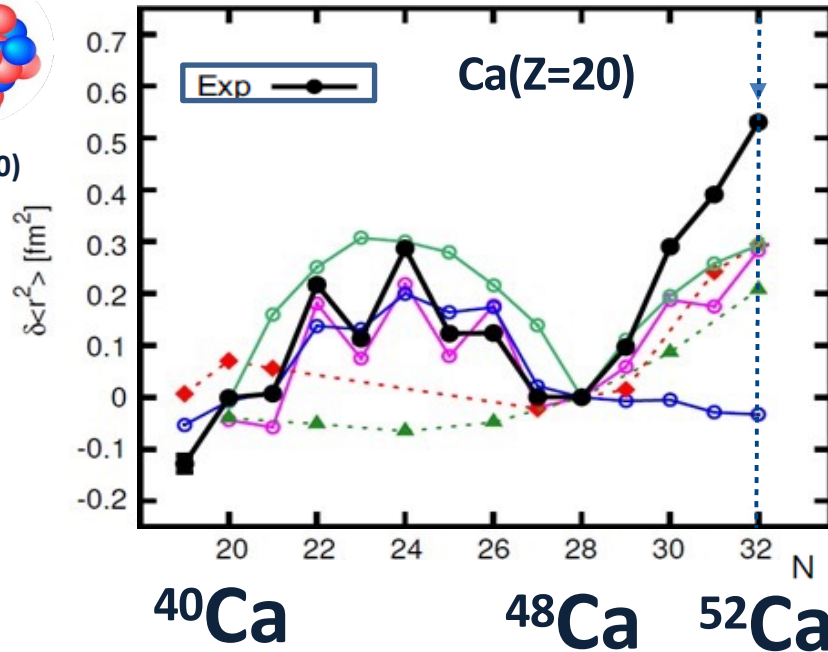
Evolution of the nuclear size away from stability

How do nuclear phenomena emerge from QCD?

[Garcia Ruiz et al., Nature Phys.12, 594 (2016)]



Ca(Z=20)



COLLAPS

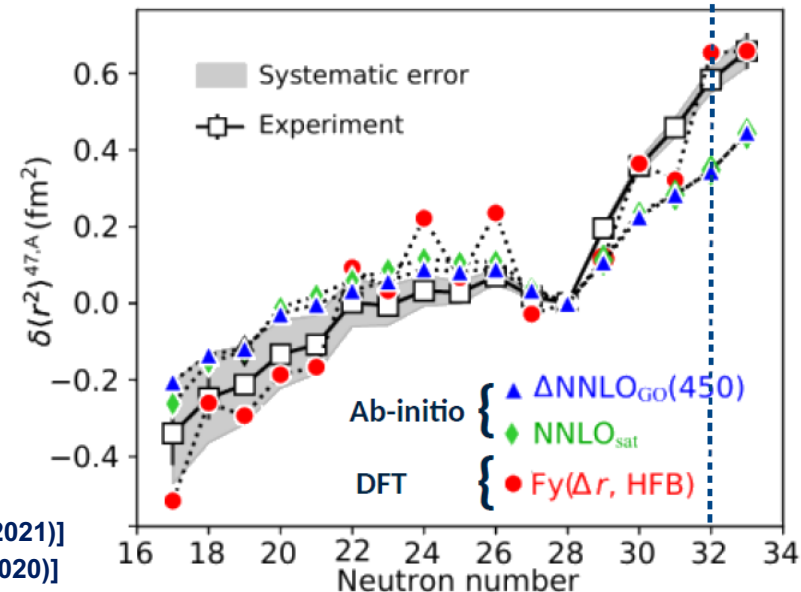
ISOLDE



CRIS



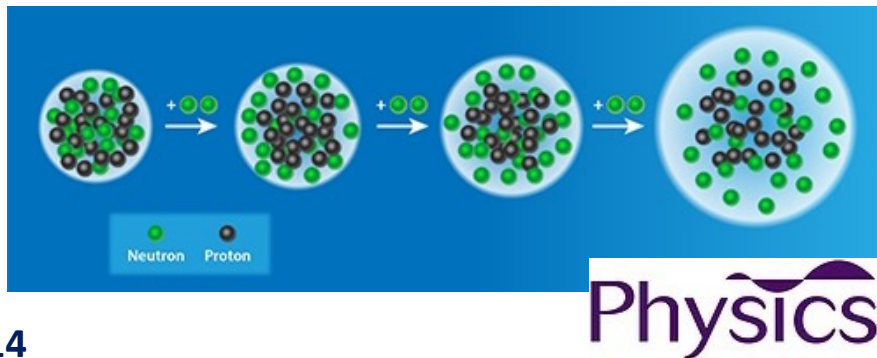
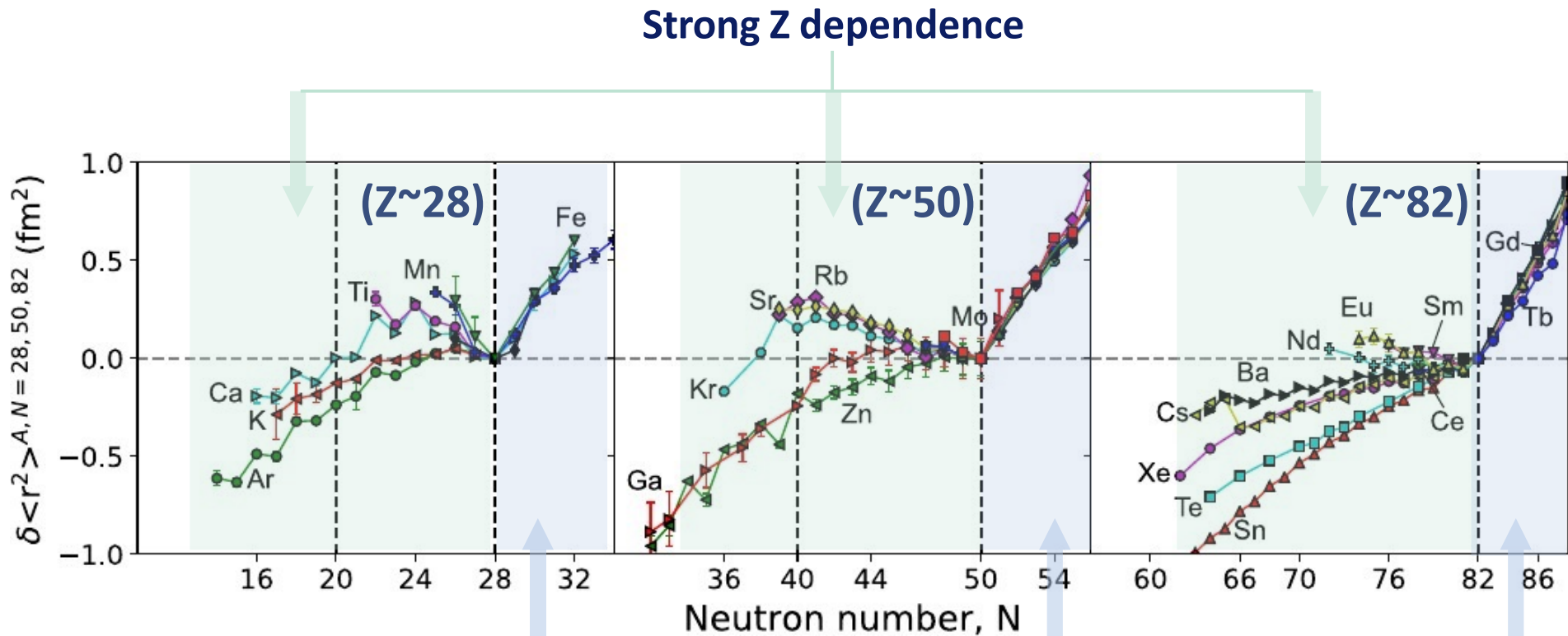
K(Z=19)



[Koszorus et al. Nature Phys. 17, 428 (2021)]

[Degroote et al. Nature Phys. 16, 620 (2020)]

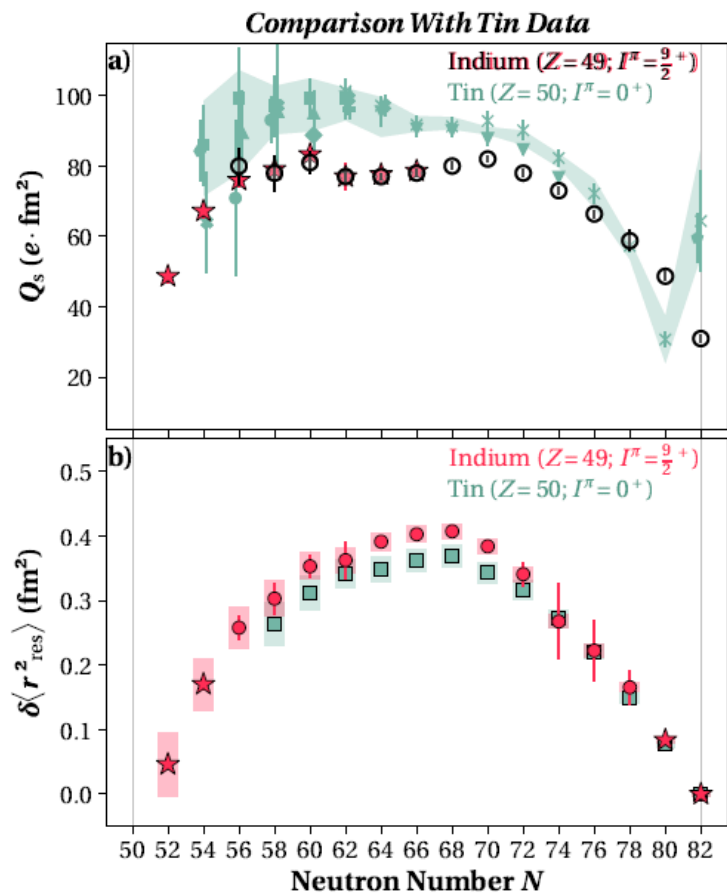
Nuclear charge radii across closed-shells



Similar trends for neutron-rich

- [Koszorus et al. Nature Phys. (2021)]
- [Degroote et al. Nature Phys. 16, 620 (2020)]
- [Kaufmann Phys. Rev. Lett. 124, 132502 (2020)]
- [Garcia Ruiz & Vernon EPJ A 56, 136 (2020)]
- [Gorges et al. Phys. Rev. Lett. 122, 192502 (2019)]
- [Garcia Ruiz et al. Nature Phys. 12, 594 (2016)]

Evolution of nuclear collectivity between closed-shells

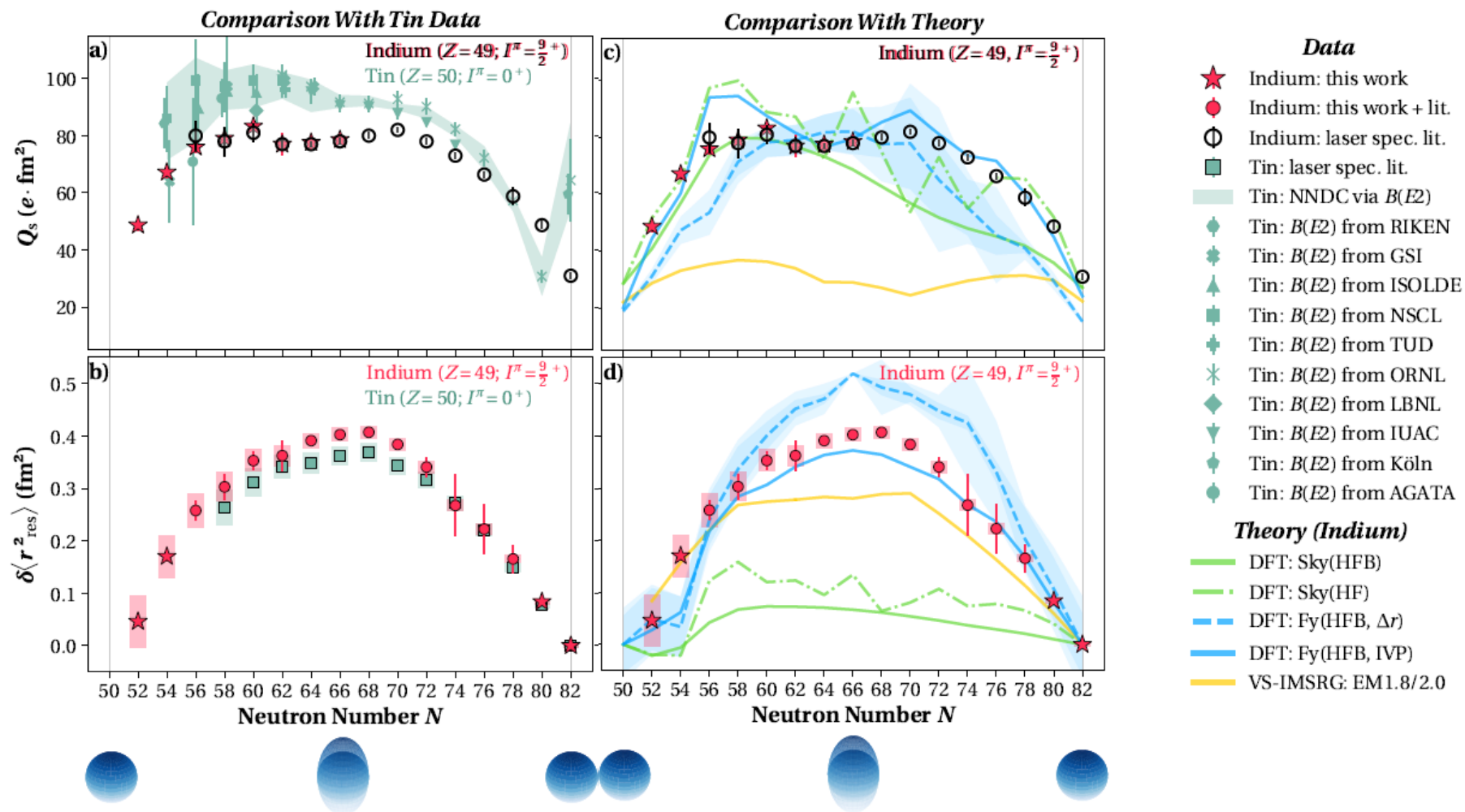


- Data**
- ★ Indium: this work
 - Indium: this work + lit.
 - Indium: laser spec. lit.
 - Tin: laser spec. lit.
 - Tin: NNDC via $B(E2)$
 - ◆ Tin: $B(E2)$ from RIKEN
 - ◆ Tin: $B(E2)$ from GSI
 - ▲ Tin: $B(E2)$ from ISOLDE
 - Tin: $B(E2)$ from NSCL
 - ◆ Tin: $B(E2)$ from TUD
 - * Tin: $B(E2)$ from ORNL
 - ◆ Tin: $B(E2)$ from LBNL
 - ▼ Tin: $B(E2)$ from IUAC
 - ◆ Tin: $B(E2)$ from Köln
 - ◆ Tin: $B(E2)$ from AGATA

[Vernon et al. Nature 607, 260(2022)]

[Karthain et al. Accepted Nature Phys. (2024)]

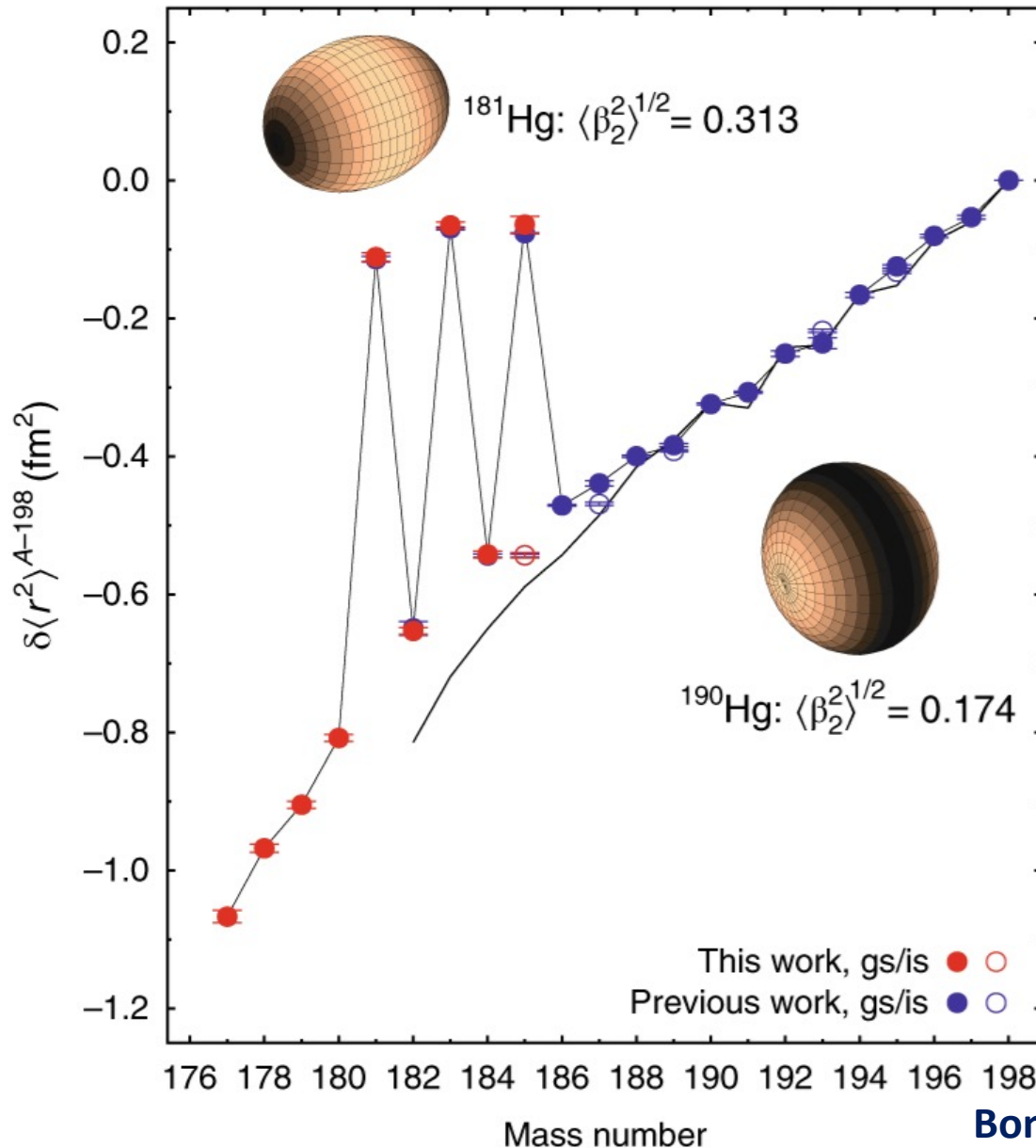
Evolution of nuclear collectivity between closed-shells



[Vernon et al. Nature 607, 260(2022)]

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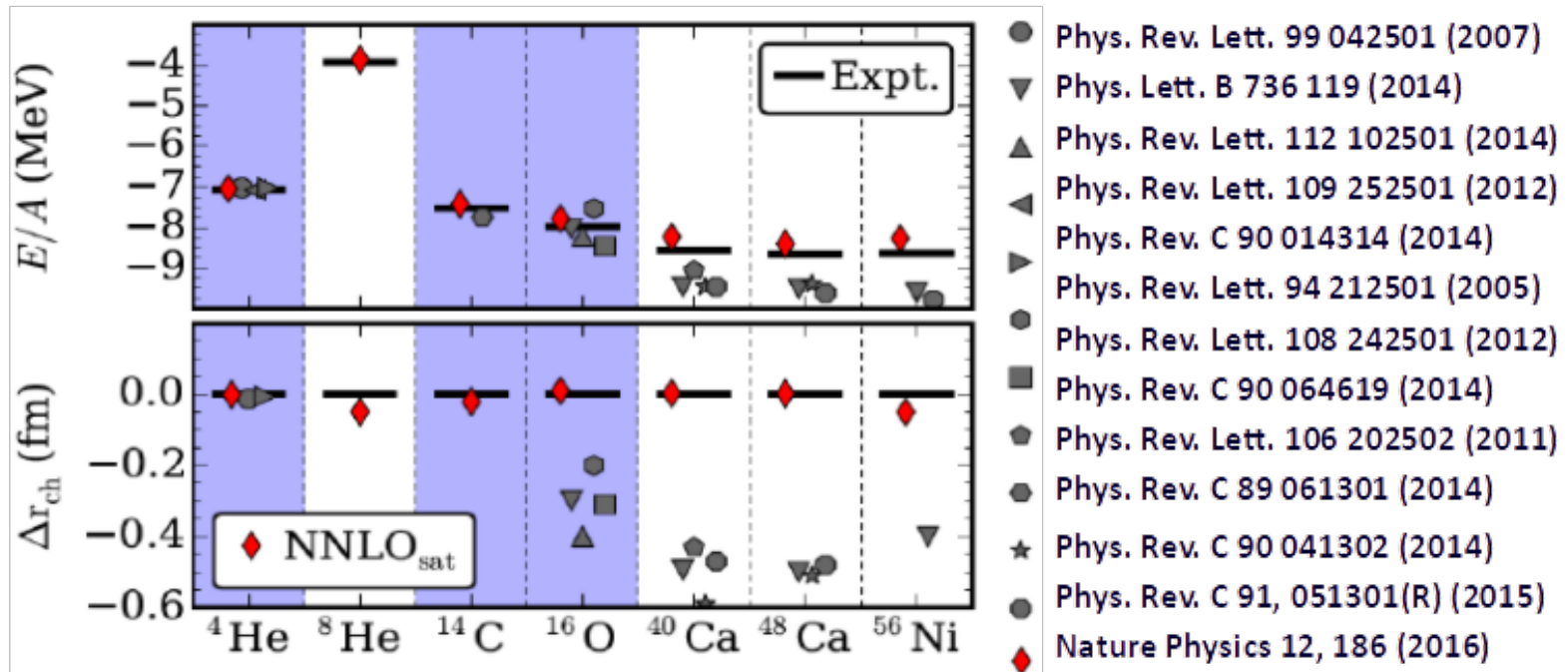
Shape staggering away closed-shells



Bonn et al. Phys. Lett. B 38, 308 (1972)

Marsh et al. Nature Phys. 14, 1163(2018)

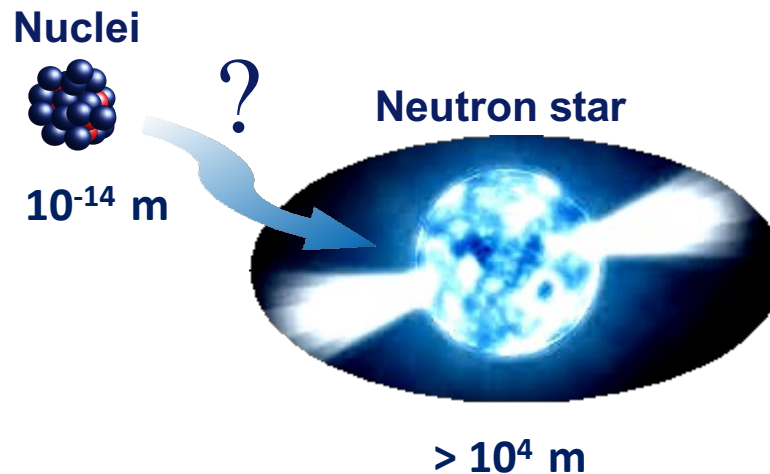
Open Challenge: Simultaneous reproduction of charge radii and binding energies has been a long-standing challenge for nuclear theory.



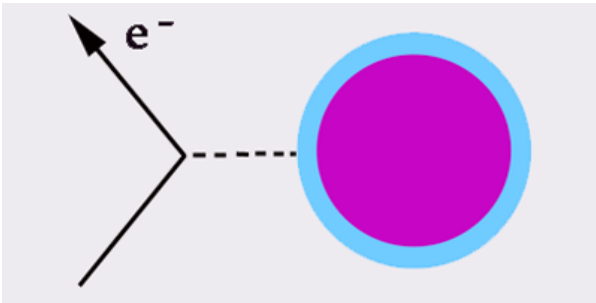
Overview

- Laser spectroscopy
- Charge radii & Nuclear Structure
- **Charge radii & Nuclear Matter**
- Isotope shifts & BSM Physics
- New Opportunities
- Summary & Outlook

Can we use the properties of nuclei to
constraint the properties of nuclear matter?



Radii of mirror nuclei & equation of state



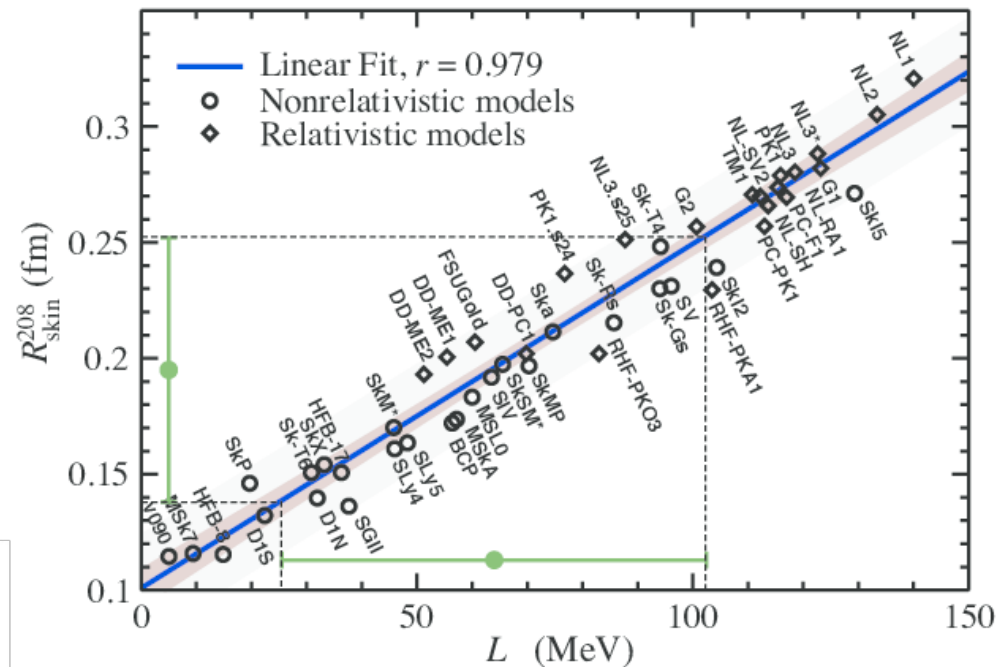
Credit: APS

Equation of state of nuclear matter

$$E(\rho, \delta) = E(\rho, 0) + E_{sym}(\rho) \delta^2 + \mathcal{O}(\delta)^4$$

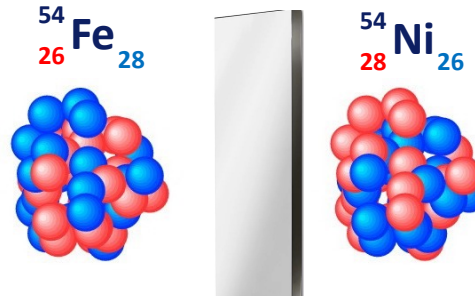
$$E_{sym}(\rho) = S_v + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \dots$$

Symmetry energy Slope ?



Roca-Maza et al. PRL 106, 252501 (2011)
PREX coll. PRL 126, 172502 (2021)

Radii of mirror nuclei & equation of state



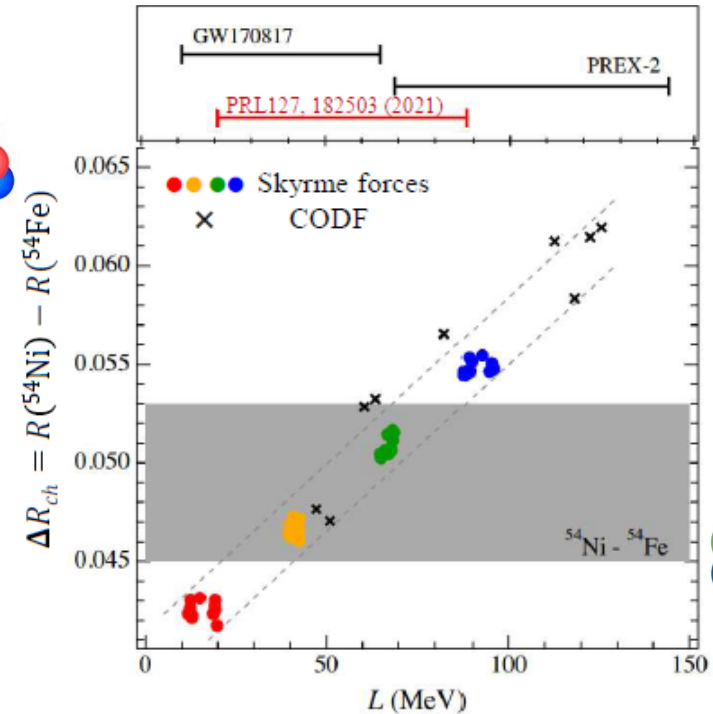
[Brown. Phys. Rev. Lett. 119, 122502 (2017)]
 [Yang & Piekarewicz, PRC 97, 014314 (2018)]

Equation of state of nuclear matter

$$E(\rho, \delta) = E(\rho, 0) + E_{\text{sym}}(\rho) \delta^2 + \mathcal{O}(\delta)^4$$

$$E_{\text{sym}}(\rho) = S_v + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \dots$$

↑ Symmetry energy
↑ Slope ?

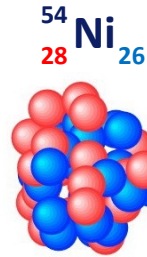
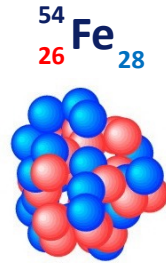


[S. Pineda Phys. Rev. Lett. 127, 182503 (2021)]

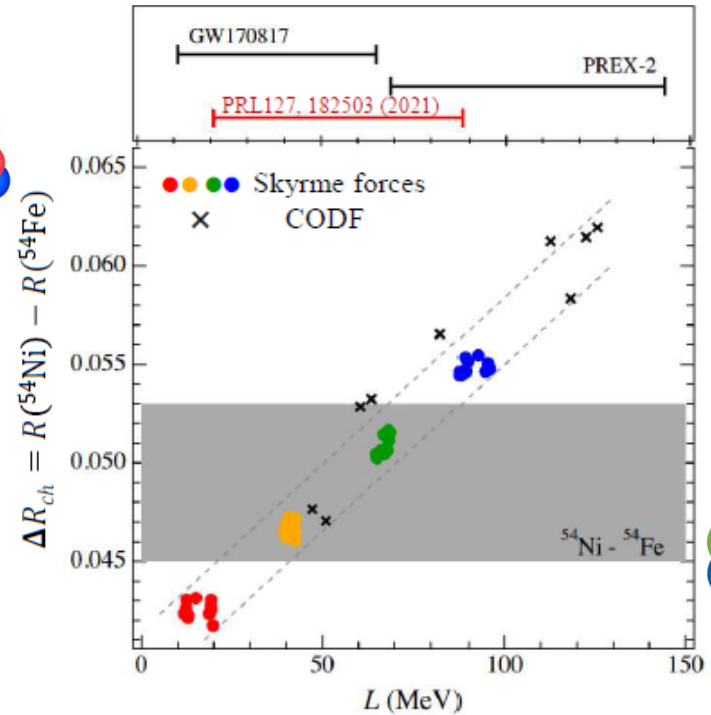
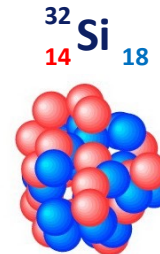
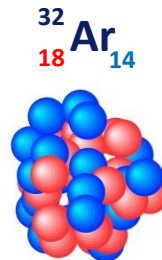
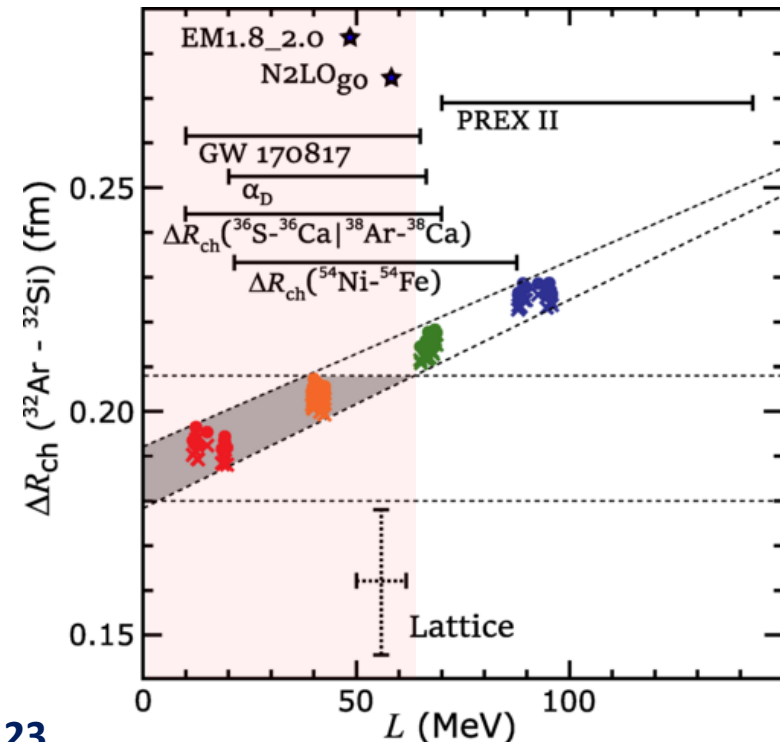
BECOLA



Radii of mirror nuclei & equation of state



Open Challenge: Atomic theory uncertainties



[S. Pineda Phys. Rev. Lett. 127, 182503 (2021)]

BECOLA



[Koning et al. PRL 132, 162502 (2024)]

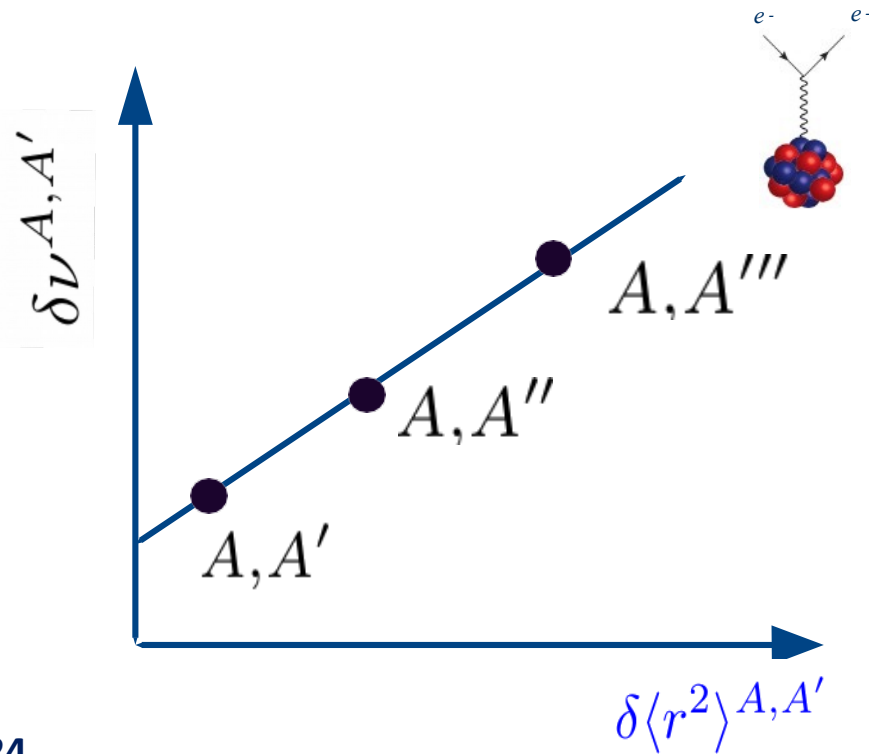
Overview

- Laser spectroscopy
- Charge radii & Nuclear Structure
- Charge radii & Nuclear Matter
- **Isotope shifts & BSM Physics**
- New Opportunities
- Summary & Outlook

Isotope shifts & BSM Physics

Atom
Nuclear

$$\delta\nu^{A,A'} = K_{MS} \frac{M_{A'} - M_A}{M_{A'} M_A} + F \delta\langle r^2 \rangle^{A,A'}$$

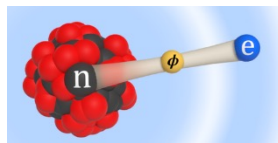


[Counts et al. Phys. Rev. Lett. 125, 123002 (2020)]

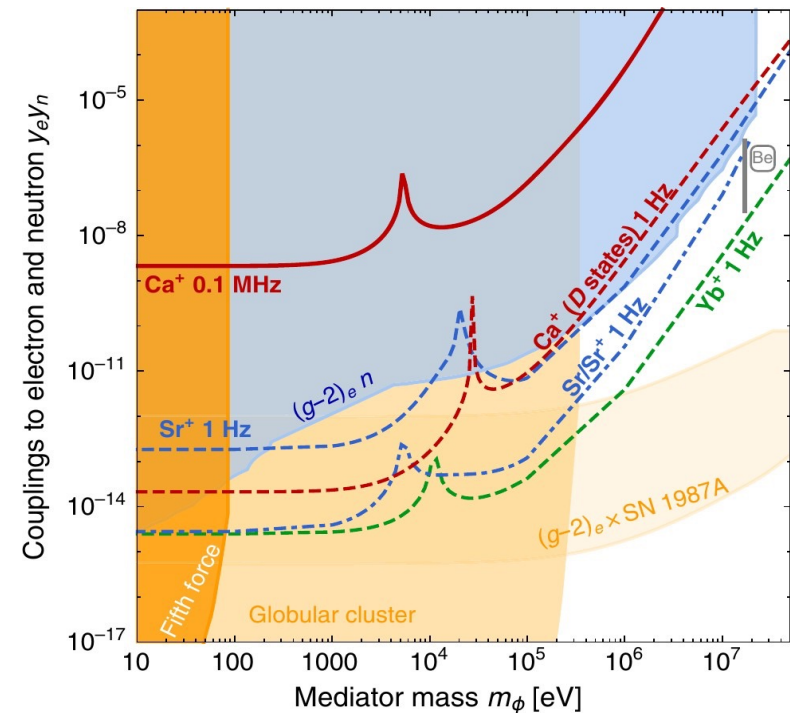
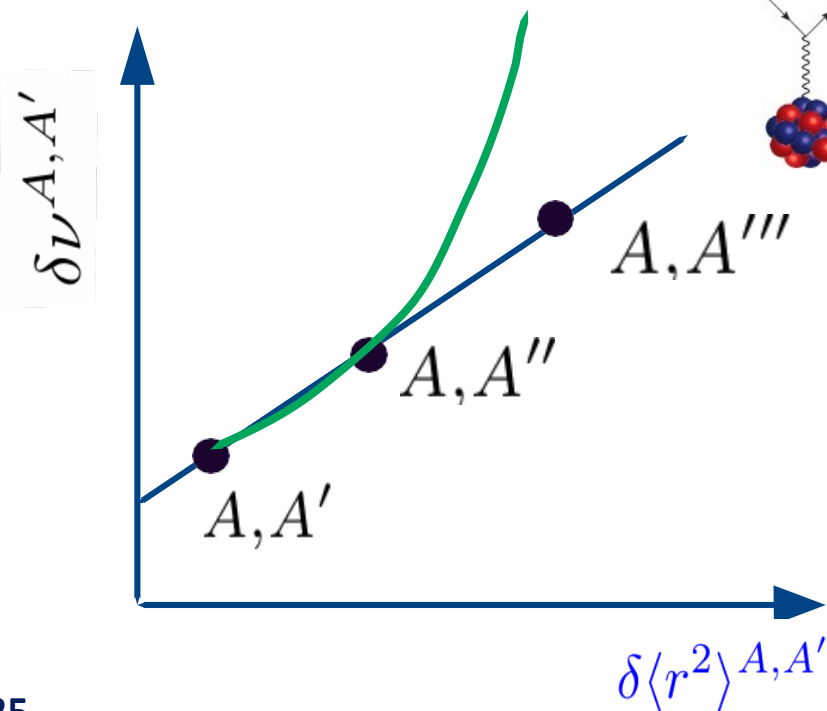
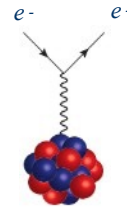
Isotope shifts & BSM Physics

Atom
Nuclear

$$\delta\nu^{A,A'} = K_{MS} \frac{M_{A'} - M_A}{M_{A'} M_A} + F \delta\langle r^2 \rangle^{A,A'} + \alpha_{NP} X_i \gamma_{AA'}$$



New physics



[Berengut et al. Phys. Rev. Lett 120, 091801 (2018)]

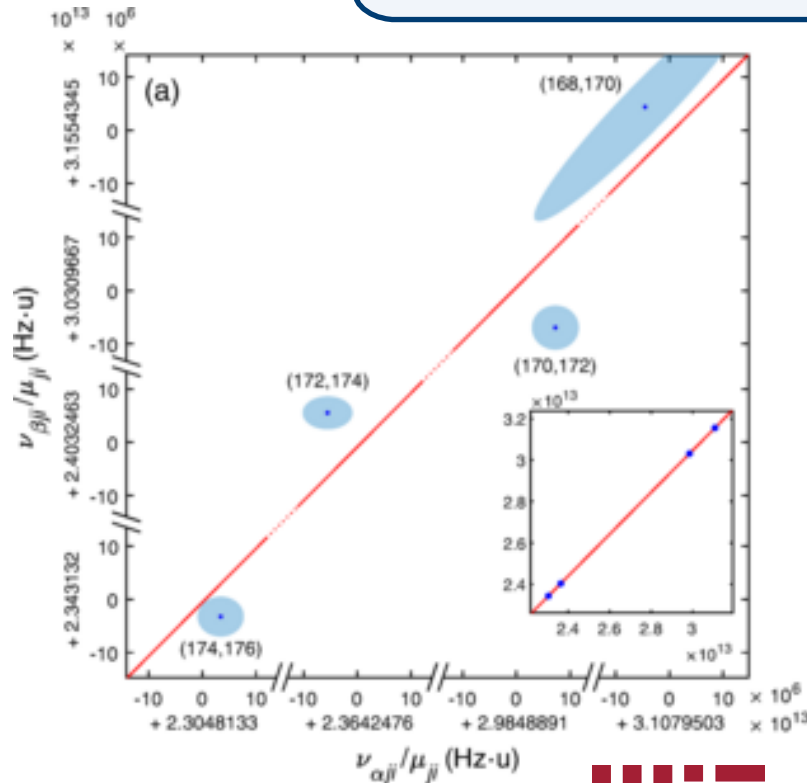
[Counts et al. Phys. Rev. Lett. 125, 123002 (2020)]

[Hur et al. Phys. Rev. Lett. 128, 163201 (2022)]

Isotope shifts & BSM Physics

Atomic factors
(two transitions)

$$\frac{\nu_2^{AA'}}{\mu^{AA'}} = \frac{F_2}{F_1} \frac{\nu_1^{AA'}}{\mu^{AA'}} + \left(K_2 - \frac{F_2}{F_1} K_1 \right) + \alpha_{\text{NP}} \left(\frac{X_2}{X_1} - \frac{F_2}{F_1} \frac{A - A'}{\mu^{AA'}} \right)$$

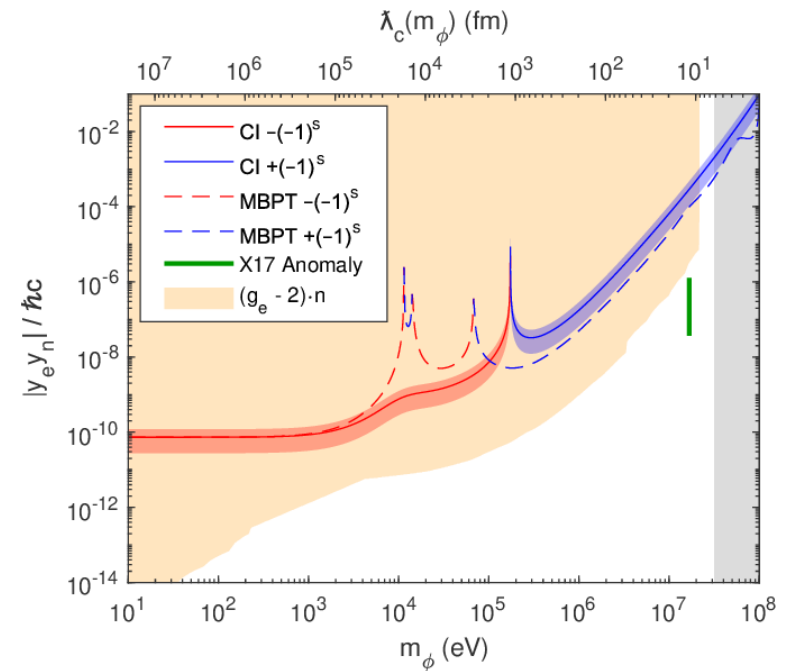


Yb⁺ → Vuletic's group at MIT



Accuracy < 100 Hz (stable) Vs ~ 1 MHz (exotic)

$$\mu^{AA'} = \frac{1}{M_A} - \frac{1}{M_{A'}}$$



[Counts et al. Phys. Rev. Lett. 125, 123002 (2020)]
[Hur et al. Phys. Rev. Lett. 128, 163201 (2022)]

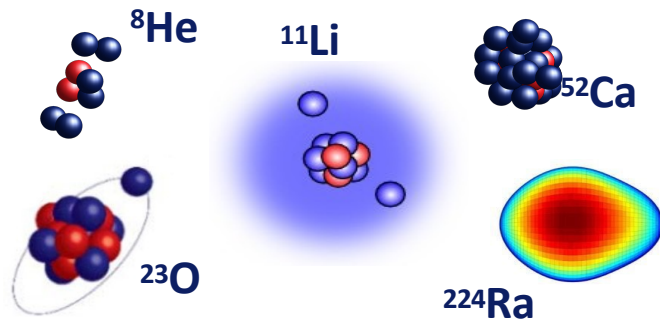
Open challenges: - Nuclear theory
- Experiments with more isotopes (exotic nuclei)

Summary & Outlook

Isotope shift measurements in Exotic Atoms allows for the exploration of rich physics phenomena



How do nuclear phenomena emerge from QCD?



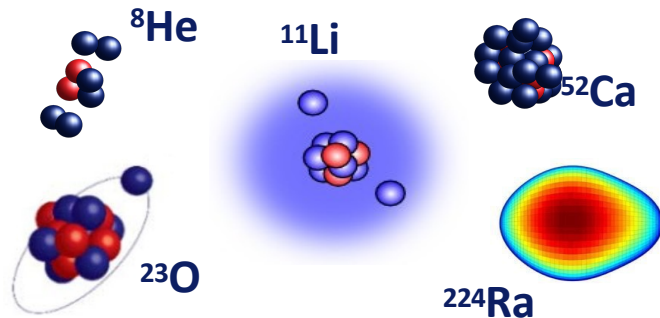
Open Challenges:

- Description of nuclear charge radii has been a long-standing challenge for ab-initio nuclear theory
- Light nuclear systems require precise experiments and atomic theory calculations.

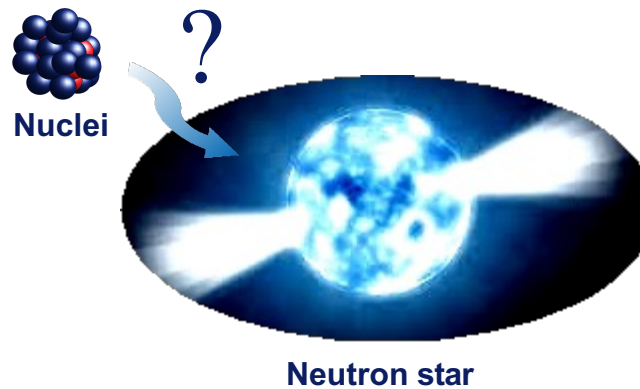
Summary & Outlook

Isotope shift measurements in Exotic Atoms allows for the exploration of rich physics phenomena

How do nuclear phenomena emerge from QCD?



What are the properties of dense nuclear matter?



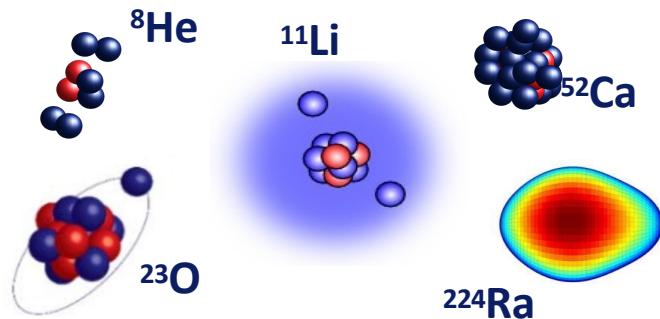
Open Challenges:

- Description of nuclear charge radii has been a long-standing challenge for ab-initio nuclear theory
- Light nuclear systems require precise experiments and atomic theory calculations.
- Precise atomic theory needed to constrain the EOS from mirror radii.

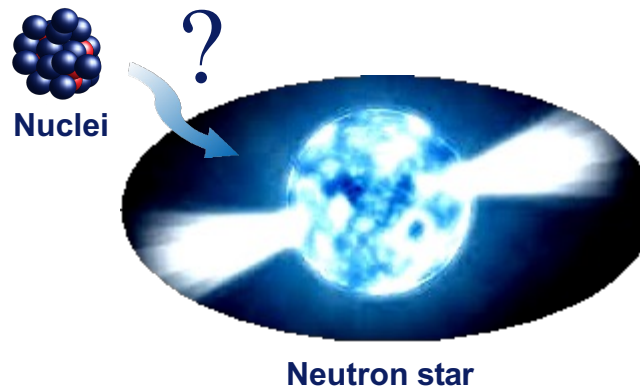
Summary & Outlook

Isotope shift measurements in Exotic Atoms allows for the exploration of rich physics phenomena

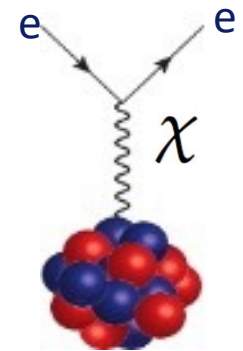
How do nuclear phenomena emerge from QCD?



What are the properties of dense nuclear matter?



Are there new forces?



Open Challenges:

- Description of nuclear charge radii has been a long-standing challenge for ab-initio nuclear theory
- Light nuclear systems require precise experiments and atomic theory calculations.
- Precise atomic theory needed to constrain the EOS from mirror radii.
- Precise nuclear theory needed to constrain BSM physics from isotope shift measurements.

Small Size – Big Science



<https://collaps.web.cern.ch/subpages/people.html>

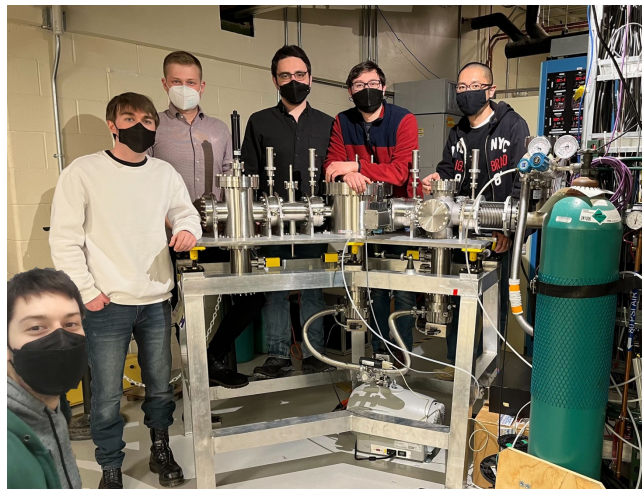


<https://isolde-cris.web.cern.ch/collaboration.html>



RISE/BECOLA @ FRIB

<https://groups.nsl.msui.edu/becola/people.html>



Nuclear & Atomic & Molecular

J. Dobaczewski (York)

J. Holt (TRIUMF)

R. Stroberg (U ND)

W. Nazarewicz (FRIB/MSU)

A. Borschevsky (Groningen)

B. Sahoo (PRL)

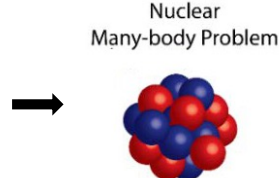
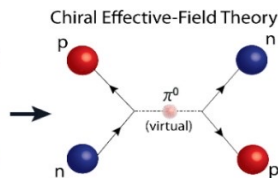
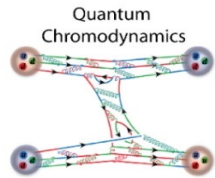
R. Berger (Malbroune)

...

Complex Nuclei with Simple Structure

Ab-initio methods

QMC, GFMC, CC, IMSRG, GGF....



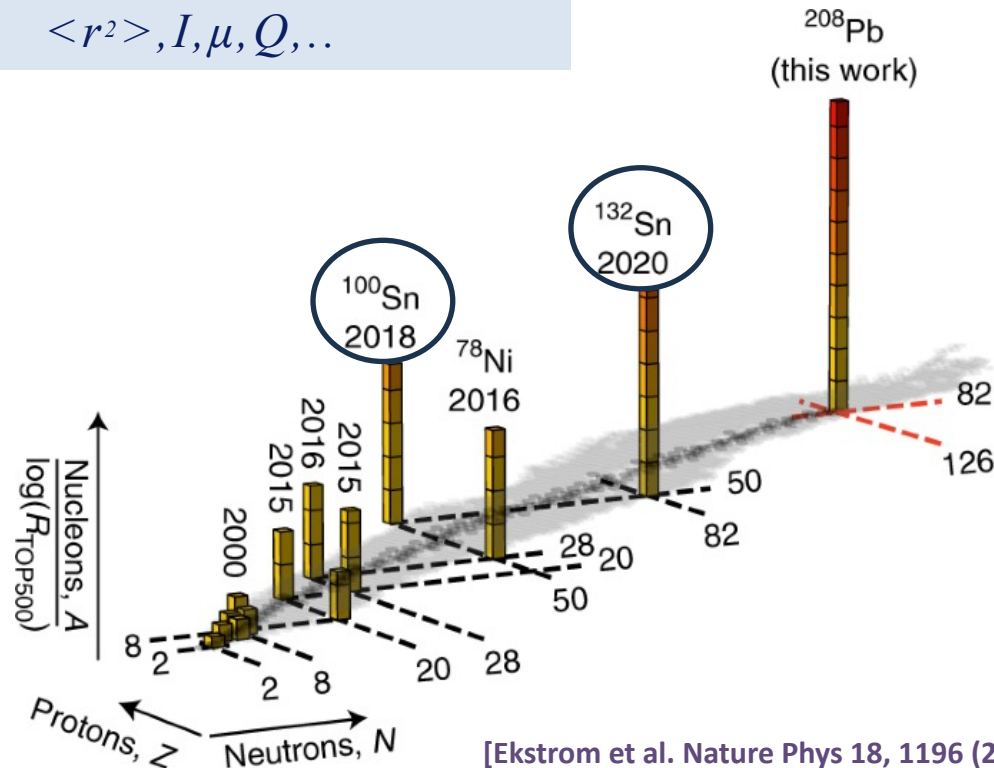
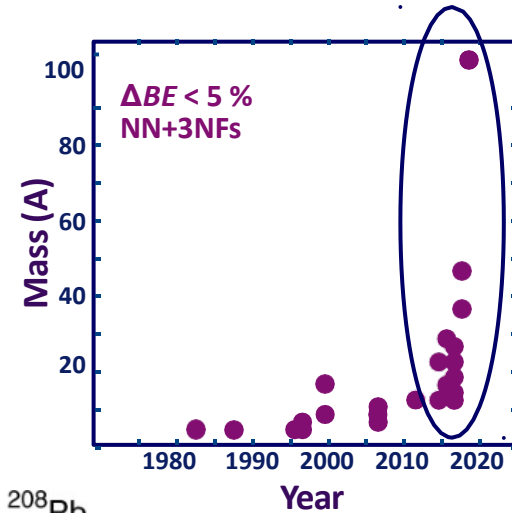
1. $\hat{H}$
2. $\hat{H}|\psi\rangle = E|\psi\rangle$
3. $\langle\psi|\hat{O}|\psi\rangle$

↓ Theory

Experiment →

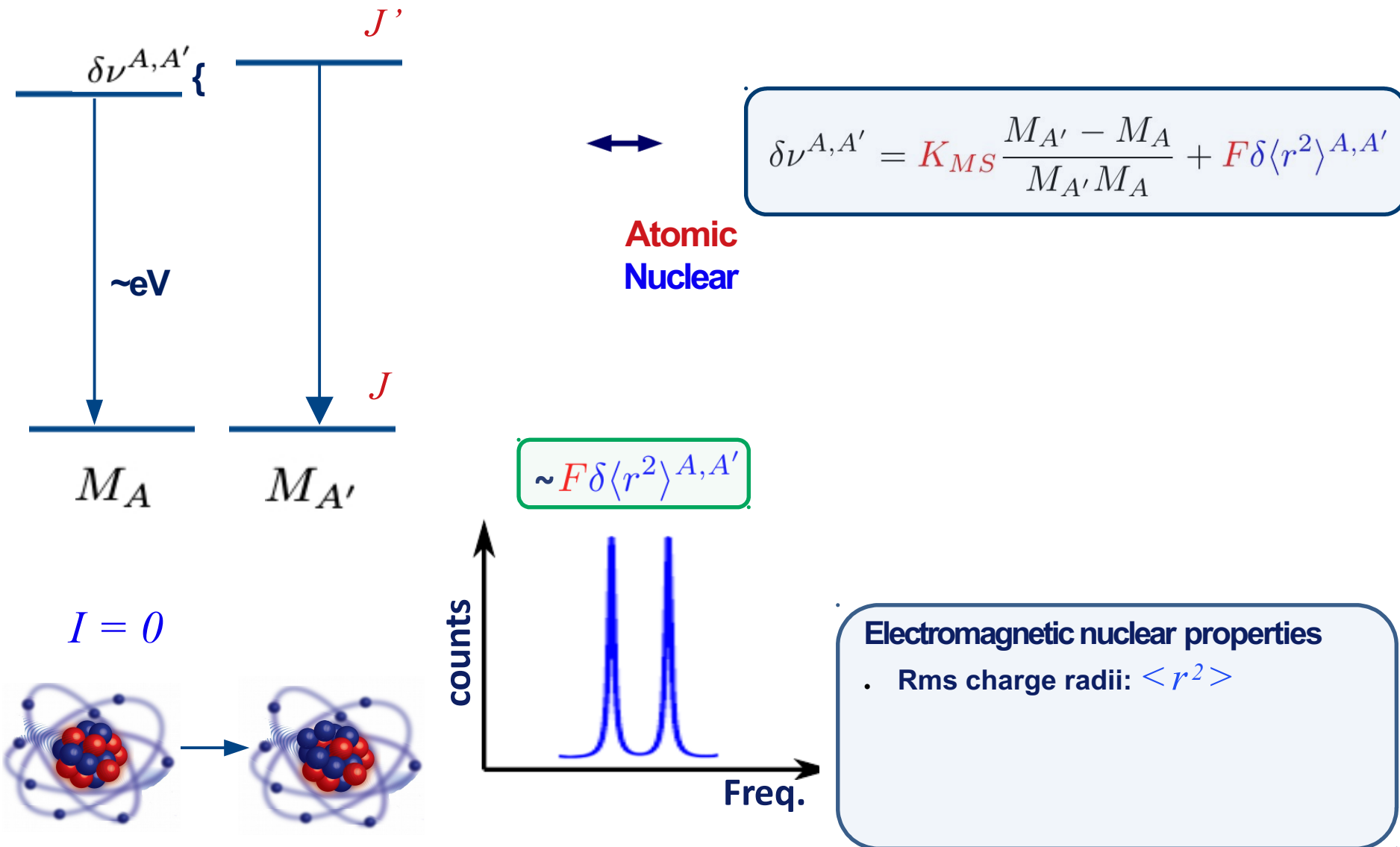
Electromagnetic nuclear properties

$\langle r^2 \rangle, I, \mu, Q, \dots$

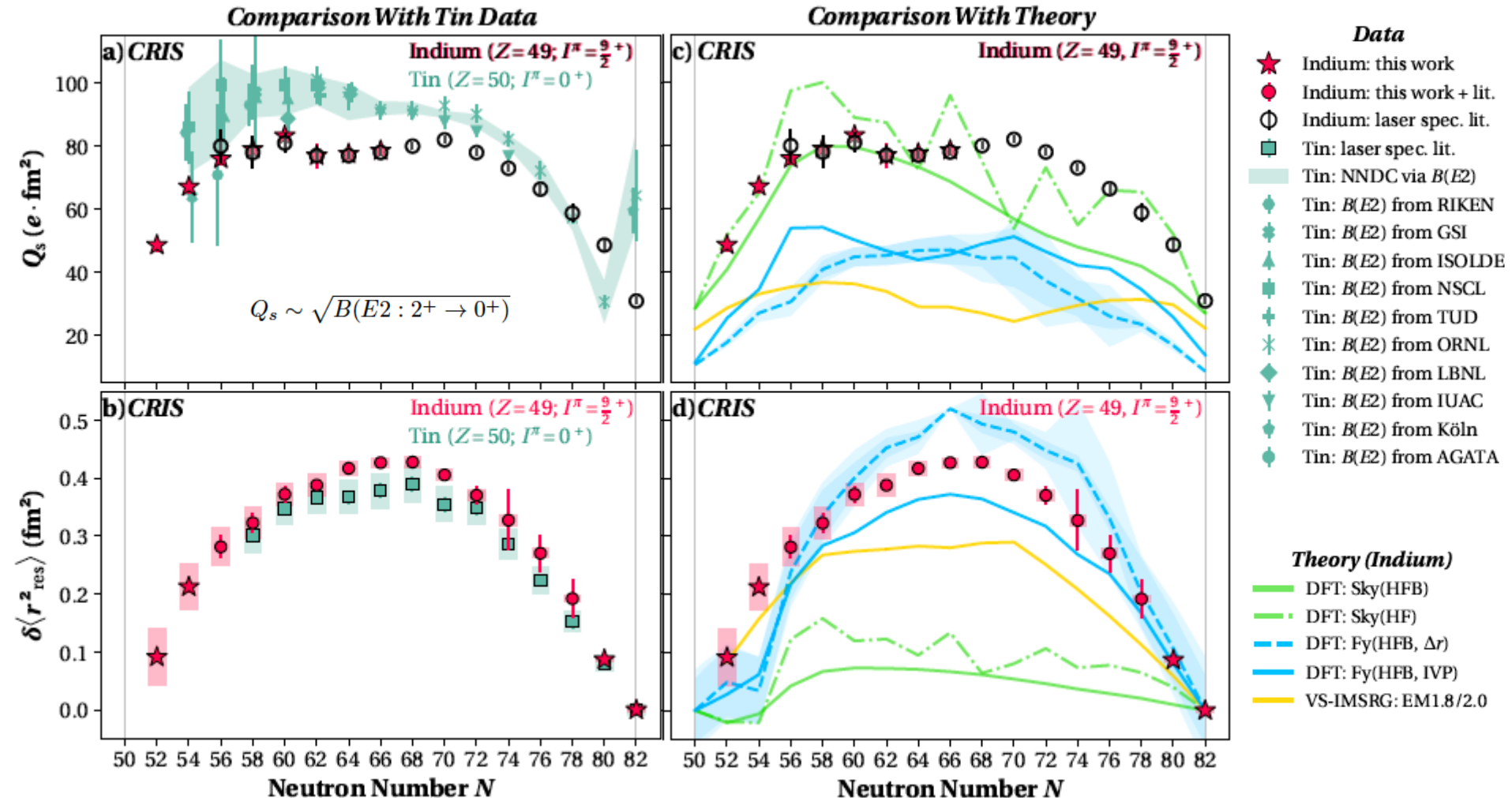


[Ekstrom et al. Nature Phys 18, 1196 (2022)]

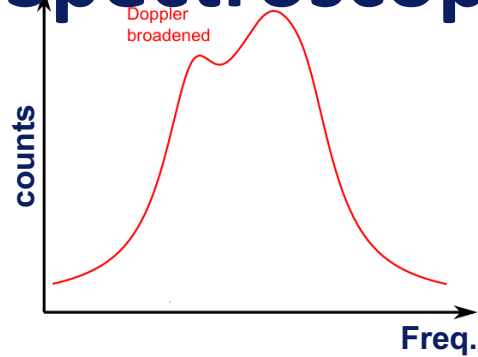
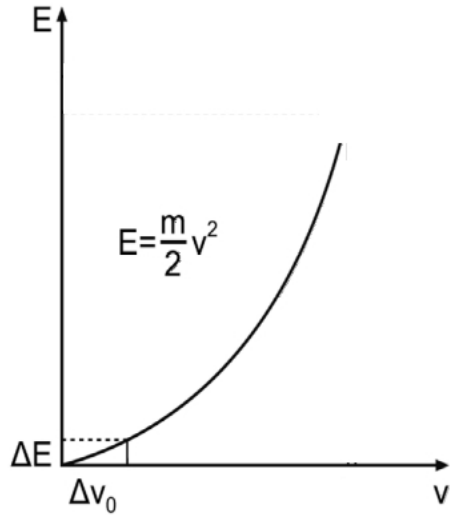
Nuclear Electromagnetic Properties from Laser Spectroscopy



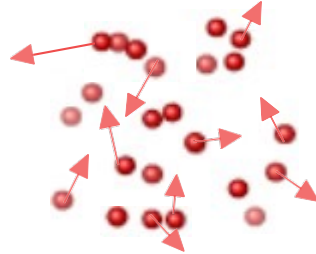
Complex Nuclei with Simple Structure



Precision Laser Spectroscopy

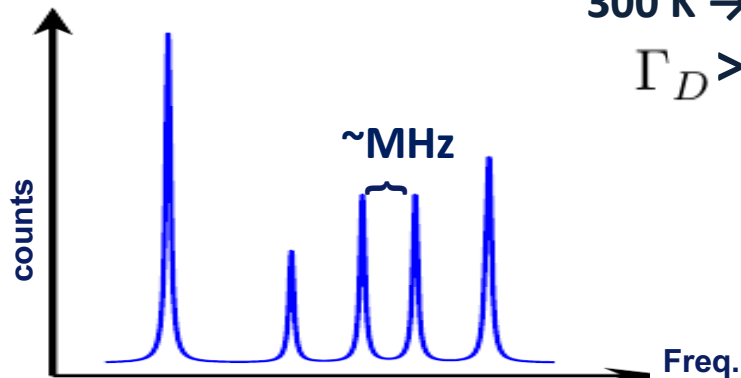


Room temperature

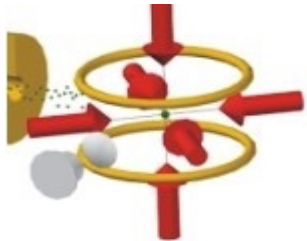
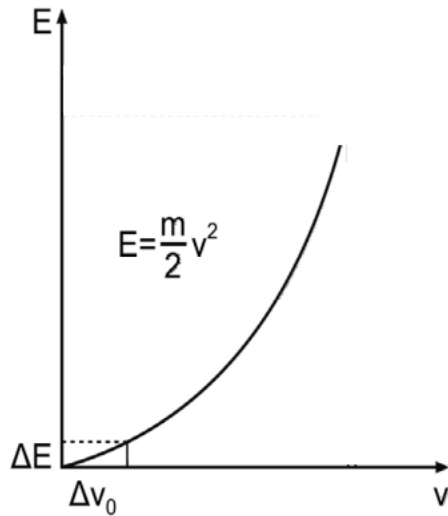


300 K $\rightarrow$ 25 meV

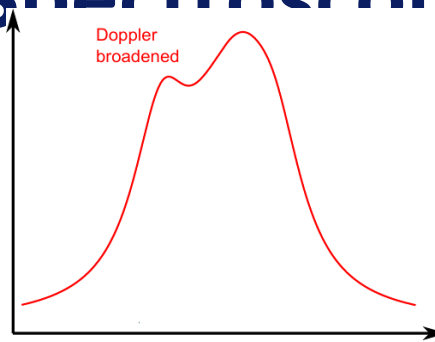
$\Gamma_D > \text{GHz}$



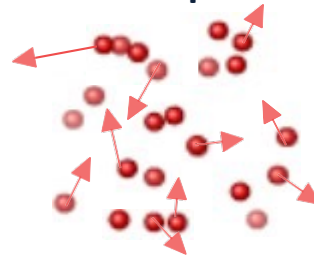
Precision Laser Spectroscopy



$T < \mu\text{K}$
 $\Gamma_D < \text{MHz}$



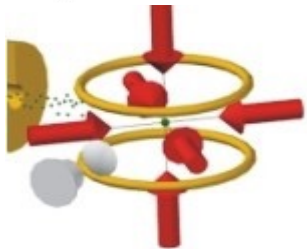
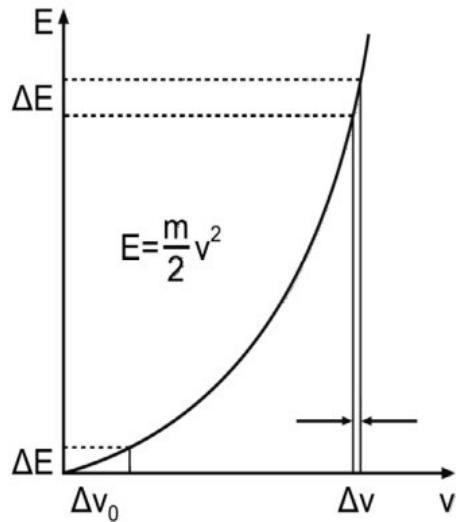
Room temperature



$300 \text{ K} \rightarrow 25 \text{ meV}$
 $\Gamma_D > \text{GHz}$

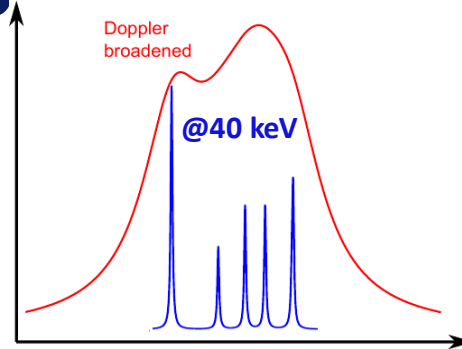
- ✓ High resolution ($< \text{MHz}$)
- High efficiency ($< 100 \text{ ions/s}$) ?
- High selectivity ($> 1/10^6$) ?
- Short time scales ($< 1 \text{ s}$) ?

Precision Laser Spectroscopy

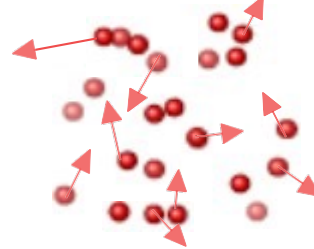


$T < \mu\text{K}$

$\Gamma_D < \text{MHz}$



Room temperature



$300 \text{ K} \rightarrow 25 \text{ meV}$

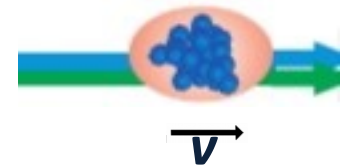
$\Gamma_D > \text{GHz}$

Energy spread

$$\Gamma_D = \nu_0 \frac{\delta E}{\sqrt{2eUm c^2}}$$

Ion beam energy

Fast beam



$@ 40 \text{ keV}$

$\Gamma_D \sim \text{MHz}$

✓ High resolution ($< \text{MHz}$)

✓ High efficiency ($< 100 \text{ ions/s}$) ?

✓ High selectivity ($> 1/10^6$) ?

✓ Short time scales ($< 1 \text{ s}$) ?

✓ High resolution ($\sim \text{MHz}$)

✓ High efficiency ($< 100 \text{ ions/s}$)

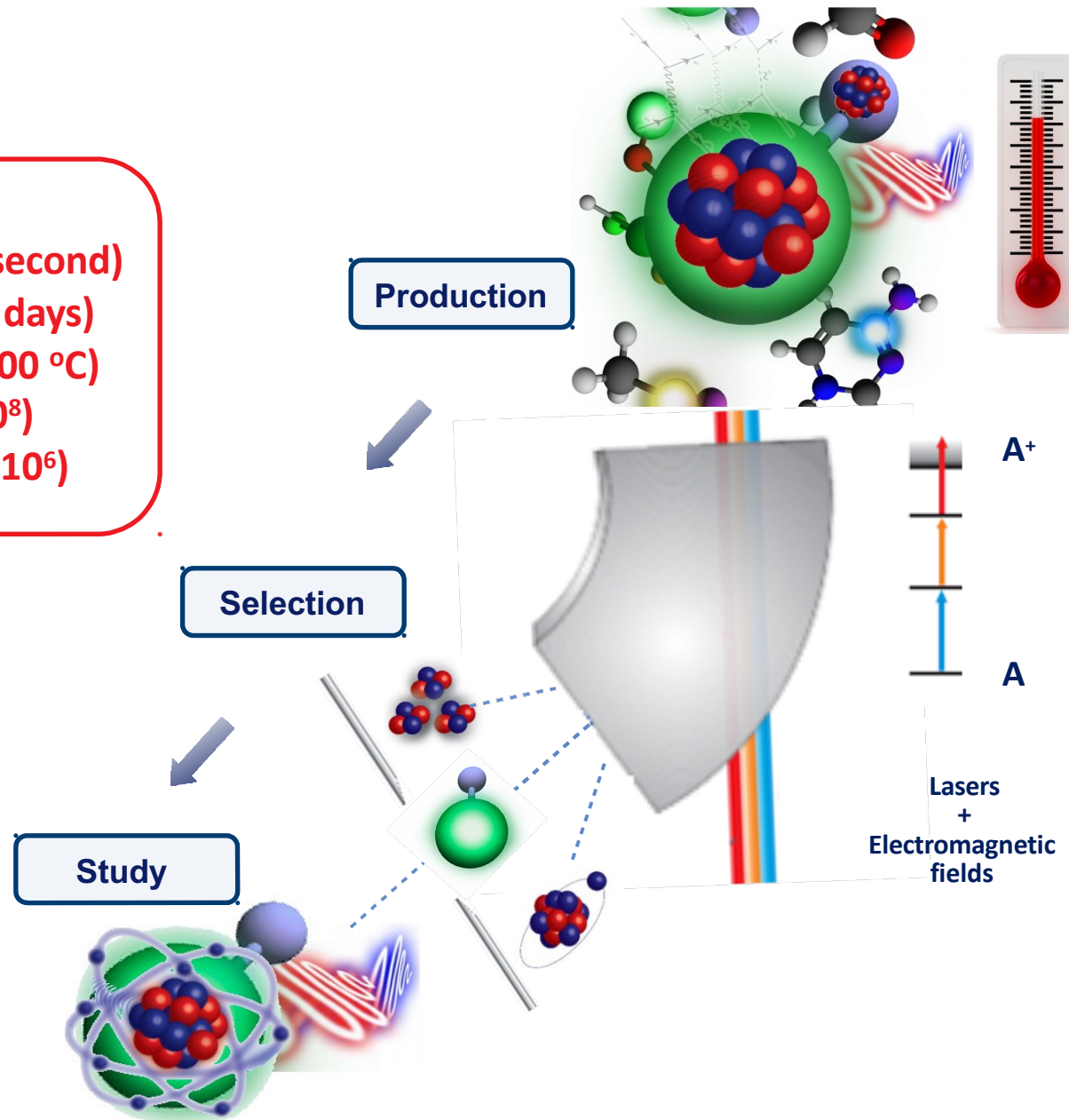
✓ High selectivity ($> 1/10^6$)

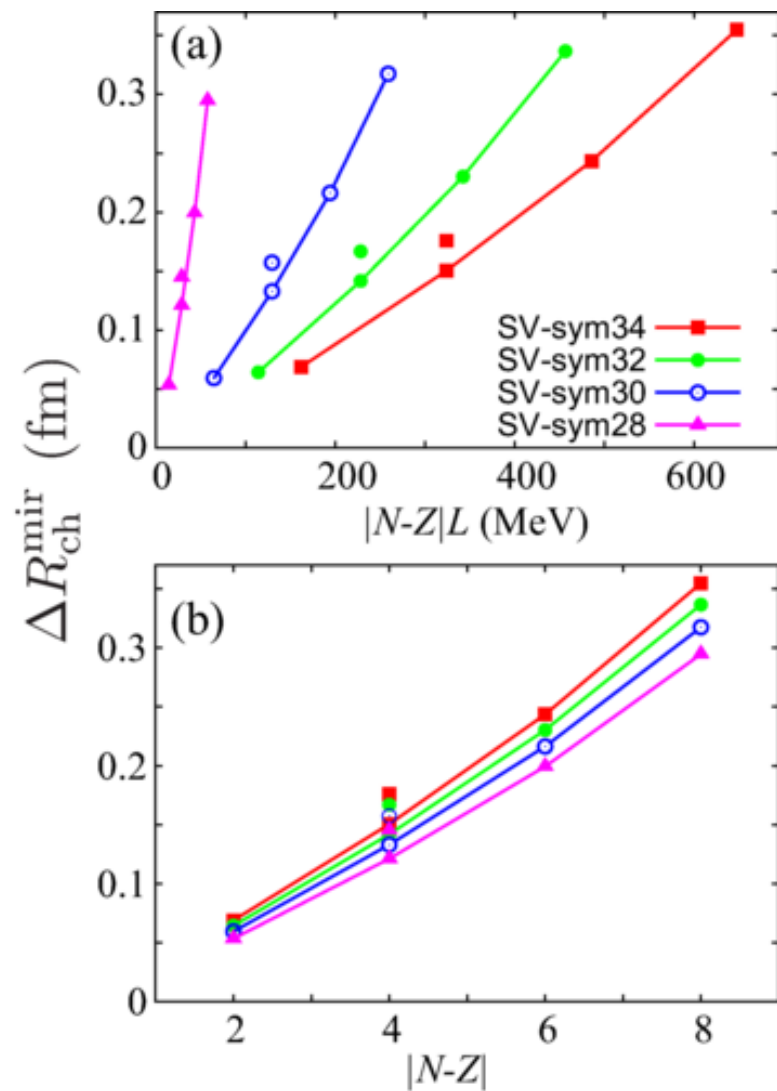
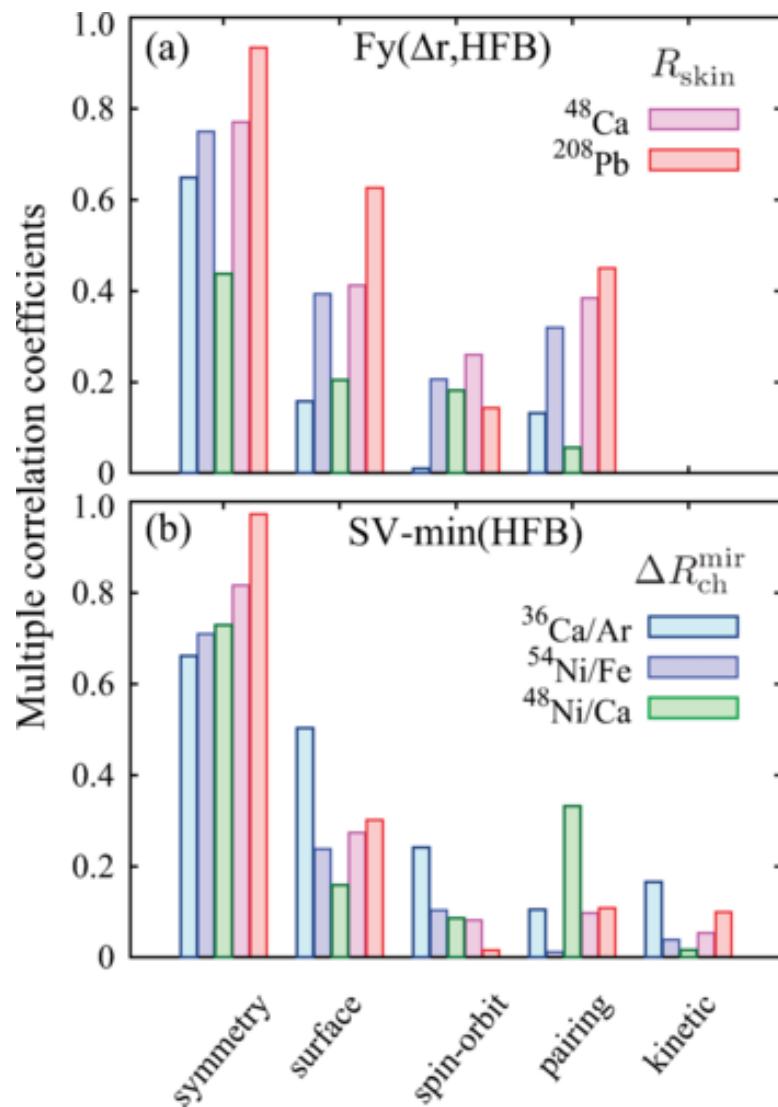
✓ Short time scales ($< 1 \text{ s}$)

Main Challenges

Experimental Challenges:

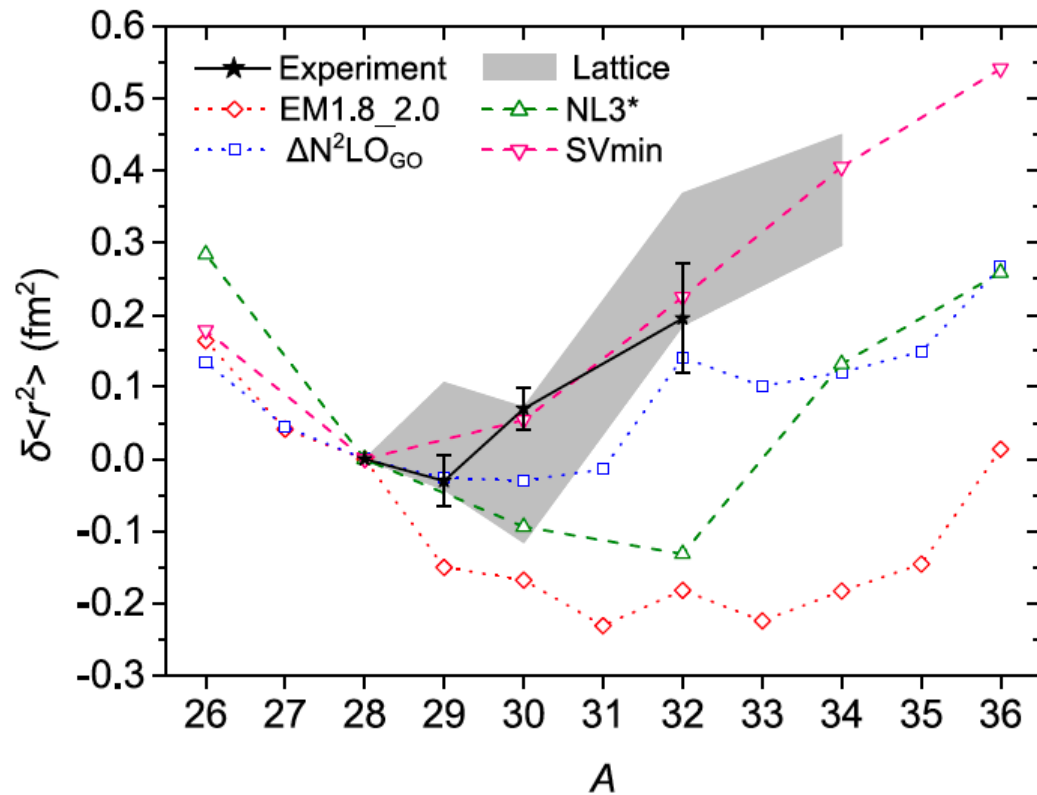
1. Small quantities (a few per second)
2. Have short lifetimes ($< 1\text{s} < \text{days}$)
3. Extreme environments ($> 2000\text{ }^{\circ}\text{C}$) & highly contaminated ($1:10^8$)
4. High precision is critical ($> 1:10^6$)



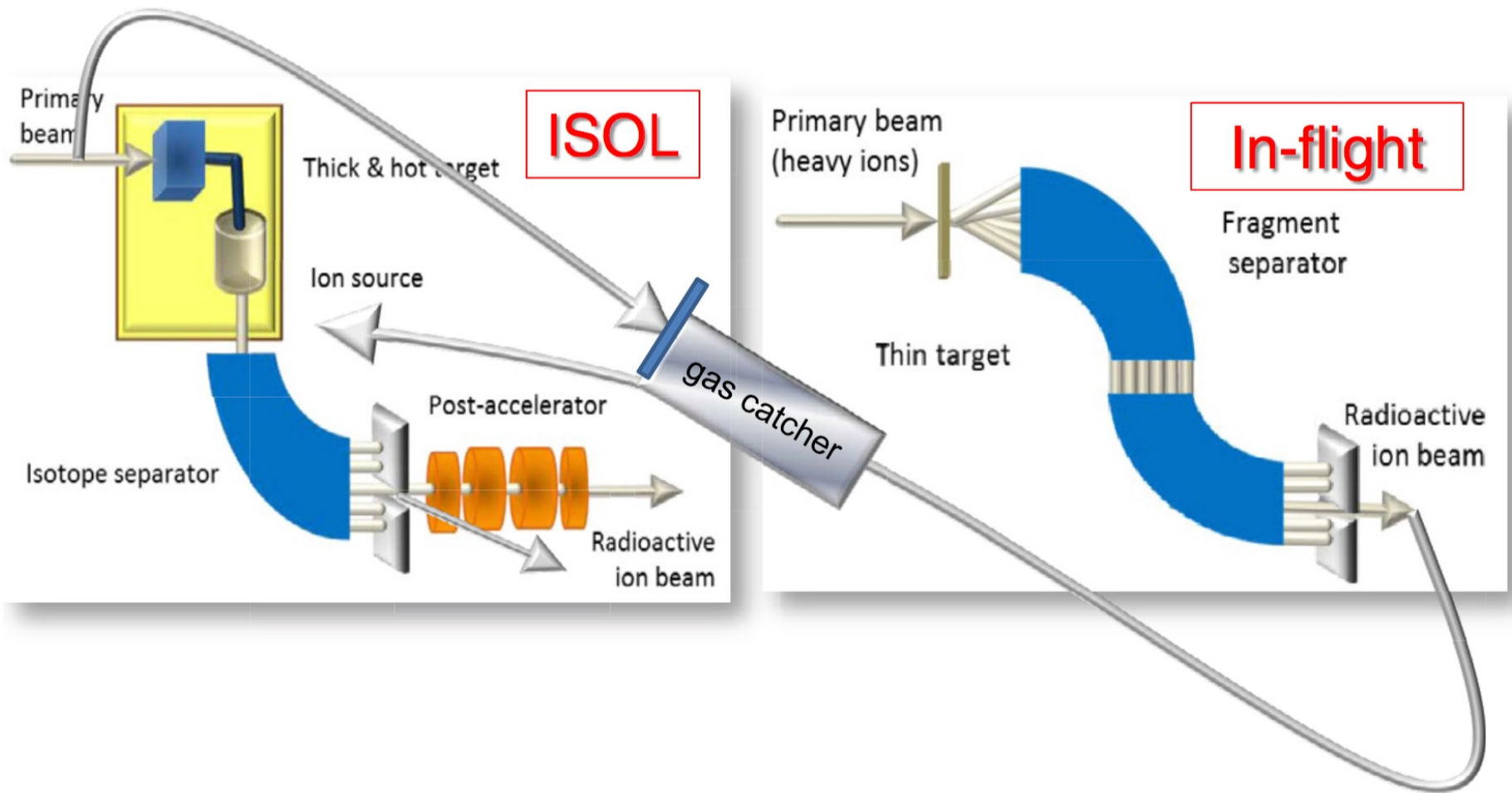


Evolution of the nuclear size away from stability

Towards a “Standard Model” of the Nucleus



[Koning et al. PRL 132, 162502 (2024)]



Recent Results (RaF)

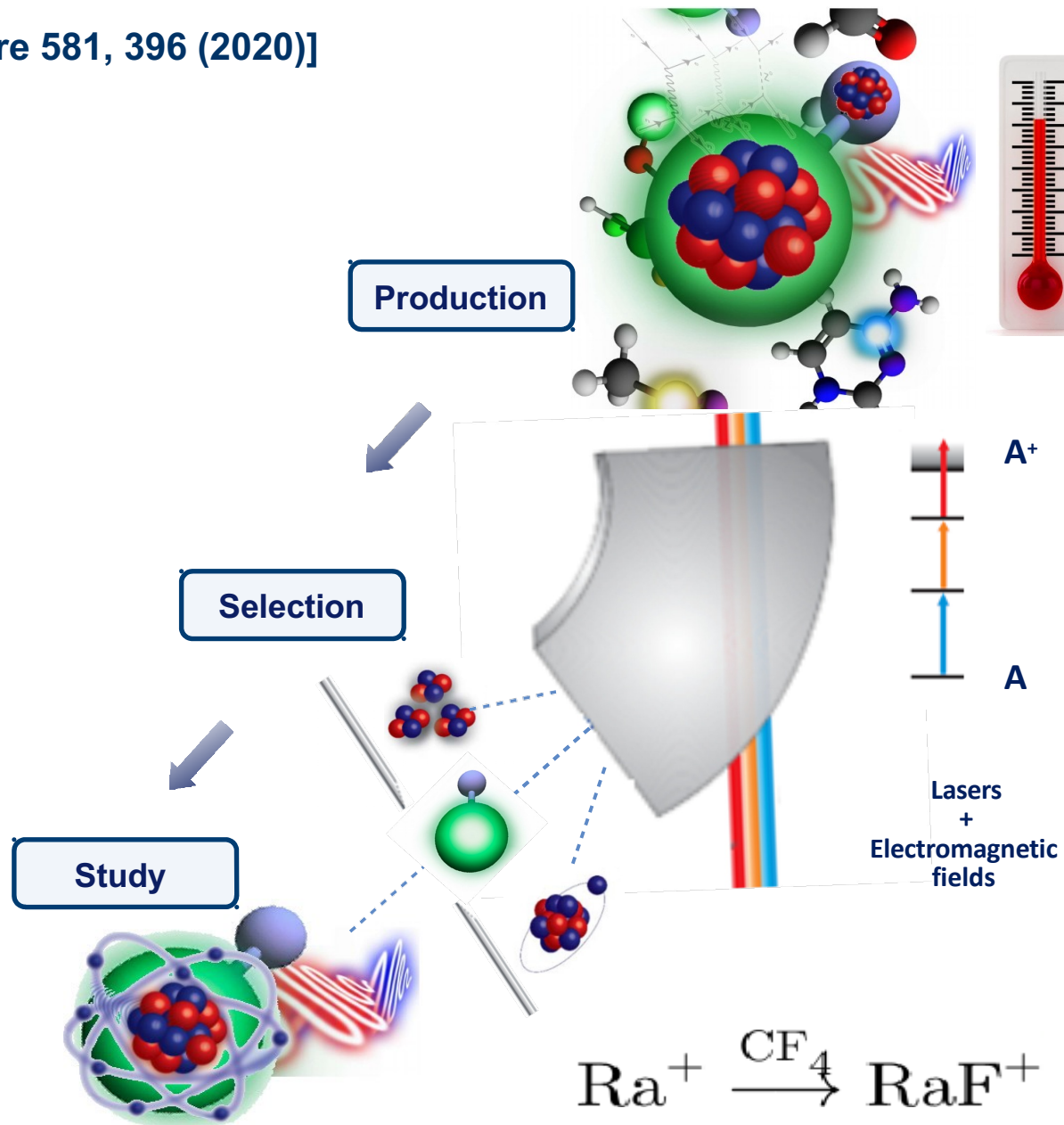
[Garcia Ruiz, Berger et al. Nature 581, 396 (2020)]

Traps
+
lasers

Production

Selection

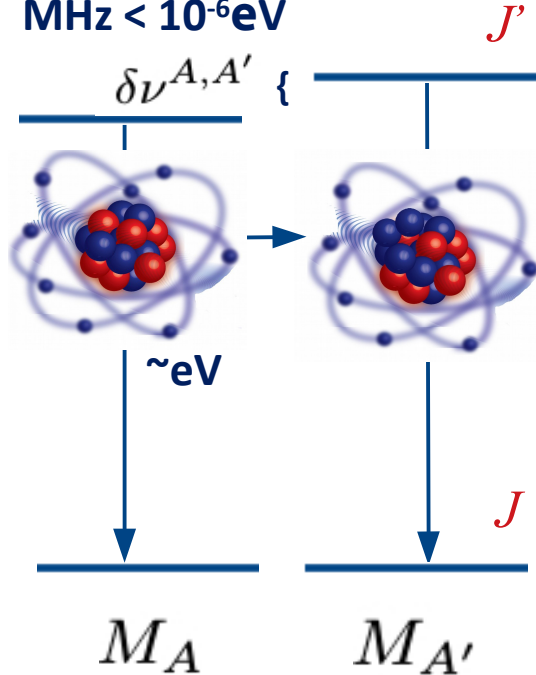
Study



How do we do it?

Isotope shift

MHz $< 10^{-6}$ eV

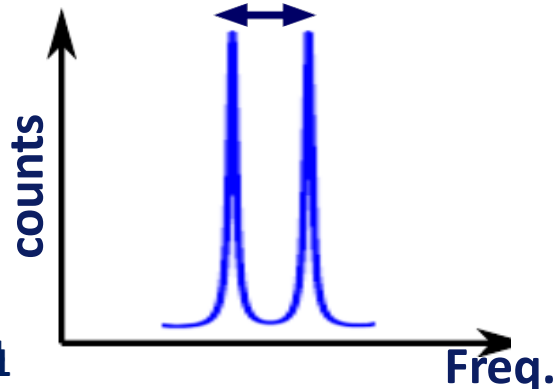


$$\delta\nu^{A,A'} = K_{MS} \frac{M_{A'} - M_A}{M_{A'} M_A} + F \delta\langle r^2 \rangle^{A,A'}$$

$I = 0$

$$\sim F \delta\langle r^2 \rangle^{A,A'}$$

Atom/molecule
Nuclear



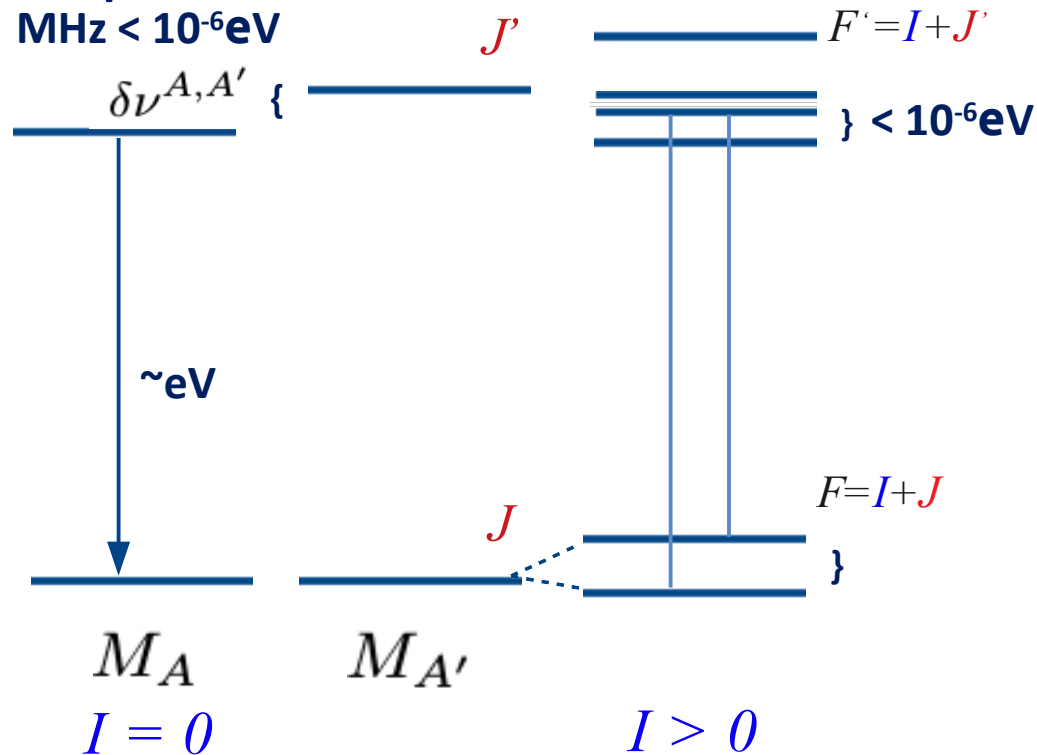
Electromagnetic structure

Rms charge radii: $\langle r^2 \rangle$

How do we do it?

Isotope shift

$\text{MHz} < 10^{-6} \text{eV}$



$$\sim \mu_B + Q \nabla E$$

Atom/molecule
Nuclear

Electromagnetic structure

Rms charge radii: $\langle r^2 \rangle$

Nuclear spin: I

Magnetic moment: μ

Quadrupole moment: Q

