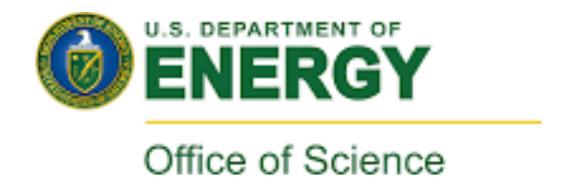
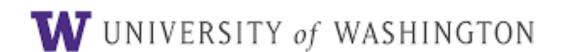
# New opportunities for beyond-the-Standard Model searches at the EIC Center for Frontiers in Nuclear Science, Stony Brook July 21-24 2025

# The Standard Model Effective Field Theory and low-energy experiments

Vincenzo Cirigliano







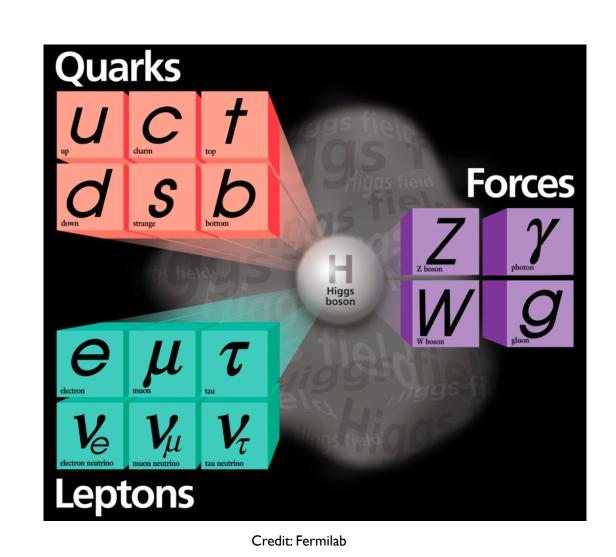
#### Outline

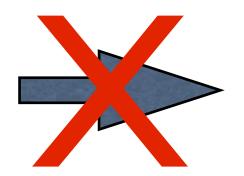
- BSM searches at low-energy: landscape and theoretical tools
- Worked example: SMEFT analysis of charged current weak interactions and the "Cabibbo angle anomaly"
- Conclusions and outlook

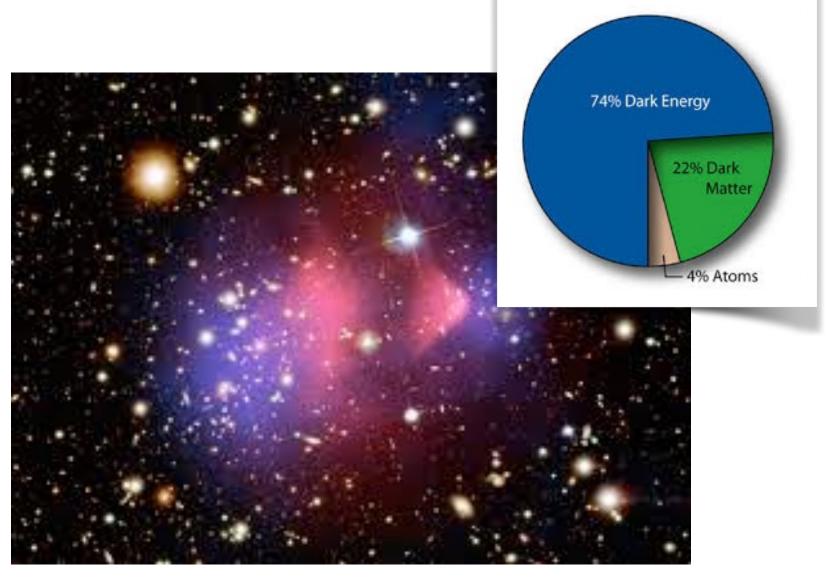
#### Searching for new physics at low-energy

Low-energy measurements can shed light on shortcomings of the Standard Model

No Neutrino Mass, no Baryon Asymmetry, no Dark Matter, no Dark Energy, ...







Credit: X-ray: NASA/CXC/CfA/M.Markevitch et al.; Optical: NASA/STScI; Magellan/U.Arizona/D.Clowe et al.; Lensing Map: NASA/STScI; ESO WFI; Magellan/U.Arizona/D.Clowe et al.

#### Searching for new physics at low-energy

- Low-energy measurements can shed light on shortcomings of the Standard Model
- Precision / sensitivity frontiers:

Precision tests of SM-allowed processes

- Weak decays
- PV electron scattering
- muon g-2
- -

Search for rare / forbidden processes that violate exact or approximate symmetries of the SM

- L and B non conservation
- CP & T violation
- Flavor violation in quarks & leptons

• •

New force mediators, from dark sectors to multi-TeV

Connection to Sakharov conditions for baryogenesis

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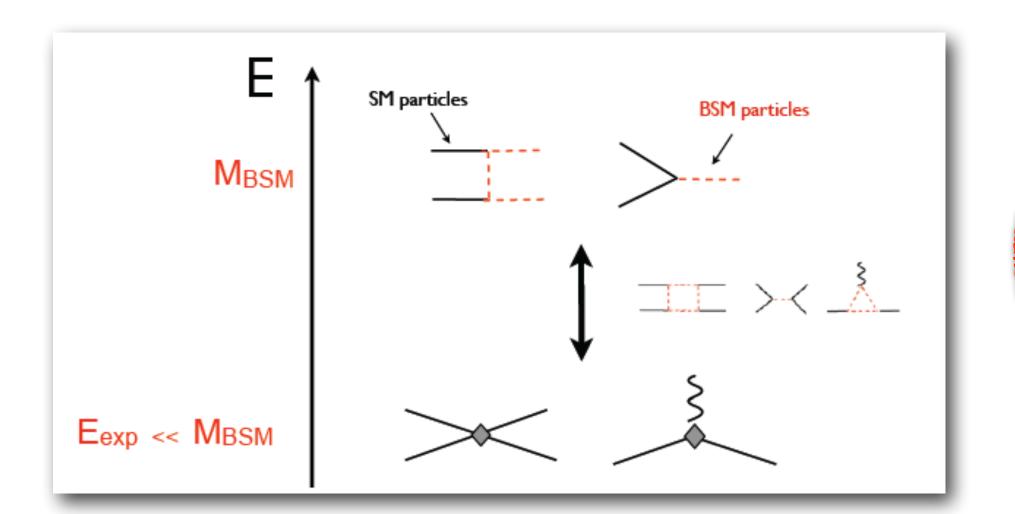
New force mediators, from dark sectors to multi-TeV

Connection to Sakharov conditions for baryogenesis

Implications of high-scale BSM physics at low-energy are efficiently analyzed with EFT methods (scale separation!)

#### General framework

• Describe new physics originating at  $\Lambda >> v_{ew}$  through local operators of increasing mass dimension



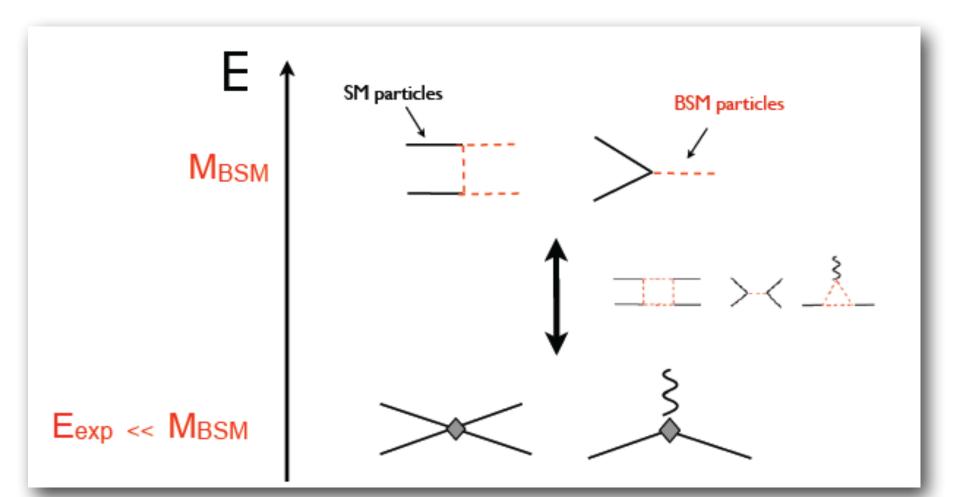
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Buchmuller-Wyler 1986,

- "Standard Model EFT" (SMEFT):
  - ★ Build operators out of SM fields
  - ★ Impose Lorentz + SM gauge symmetry
  - \* Organize operators according to mass dimension: power counting in  $E/\Lambda$ ,  $M_W/\Lambda$ . At a given order the EFT is renormalizable and predictive

#### General framework

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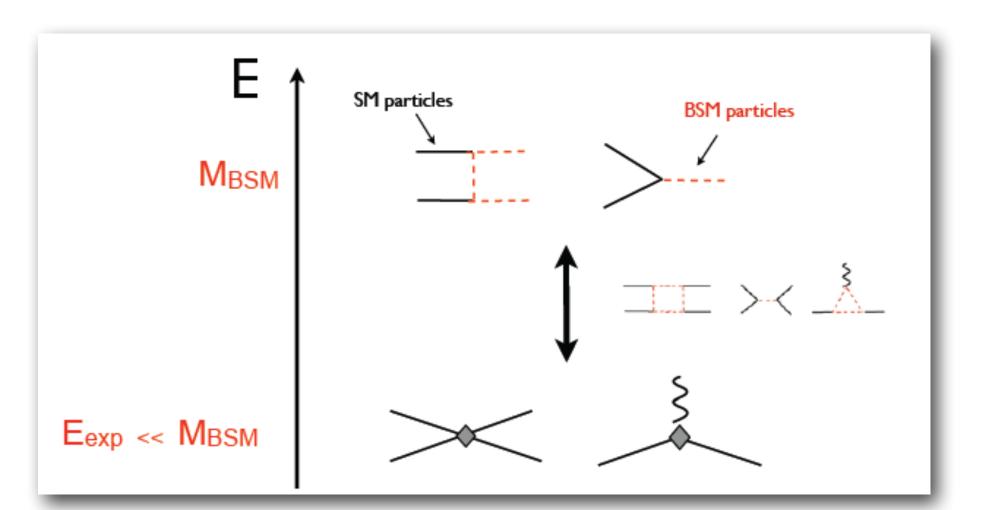


$$\left[\begin{array}{cccc} \Lambda \leftrightarrow \mathsf{M}_{\mathsf{BSM}} \end{array}\right] & C_i \left[g_{\mathsf{BSM}}, \ M_a/M_b\right] \\ \\ \mathcal{L}_{\mathrm{eff}} = \mathcal{L}_{SM} & + \frac{C^{(5)}}{\Lambda} \ O^{(5)} & + \sum_i \frac{C_i^{(6)}}{\Lambda^2} \ O_i^{(6)} & + \ \ldots \\ \\ \Delta \mathsf{L=2} & \Delta \mathsf{B=I, CPV, FCNC, \ldots} \end{array}$$

- Symmetries in SMEFT:
  - B, L,  $L_{e,\mu,\tau}$  not enforced: per Weinberg's definition, they are "accidental" in the SM, i.e. consequence of keeping operators of dimension  $\leq 4$  built out of SM fields & SM gauge group

#### General framework

• Describe new physics originating at  $\Lambda >> v_{ew}$  through local operators of increasing mass dimension



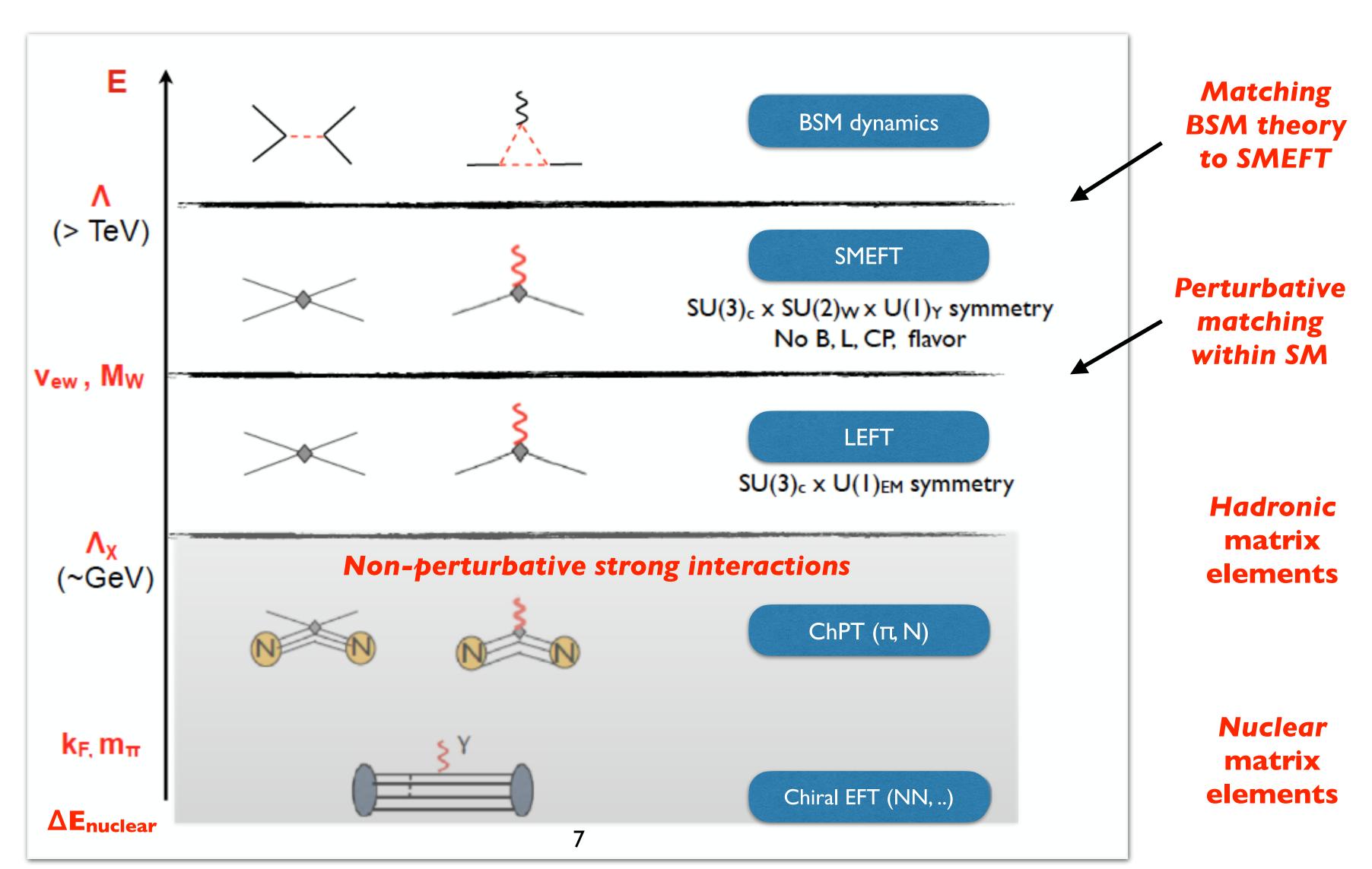
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- Beyond SMEFT: other EFTs differ in the assumptions about particle content and/or symmetry realization
  - VSMEFT: SMEFT + VR
  - HEFT: Higgs h is an SU(2) singlet. More general Higgs potential
  - •

#### Connecting scales

To connect new physics to low-energy, use a tower of EFTs in which SMEFT is the SM-BSM link

- Use appropriate degrees of freedom in each range of energies
- Write down all interactions consistent with the given symmetries
- At each threshold, need appropriate perturbative or non-perturbative matching conditions: Ahi = Alow
- Expand amplitudes to a given order in mhow/mhi

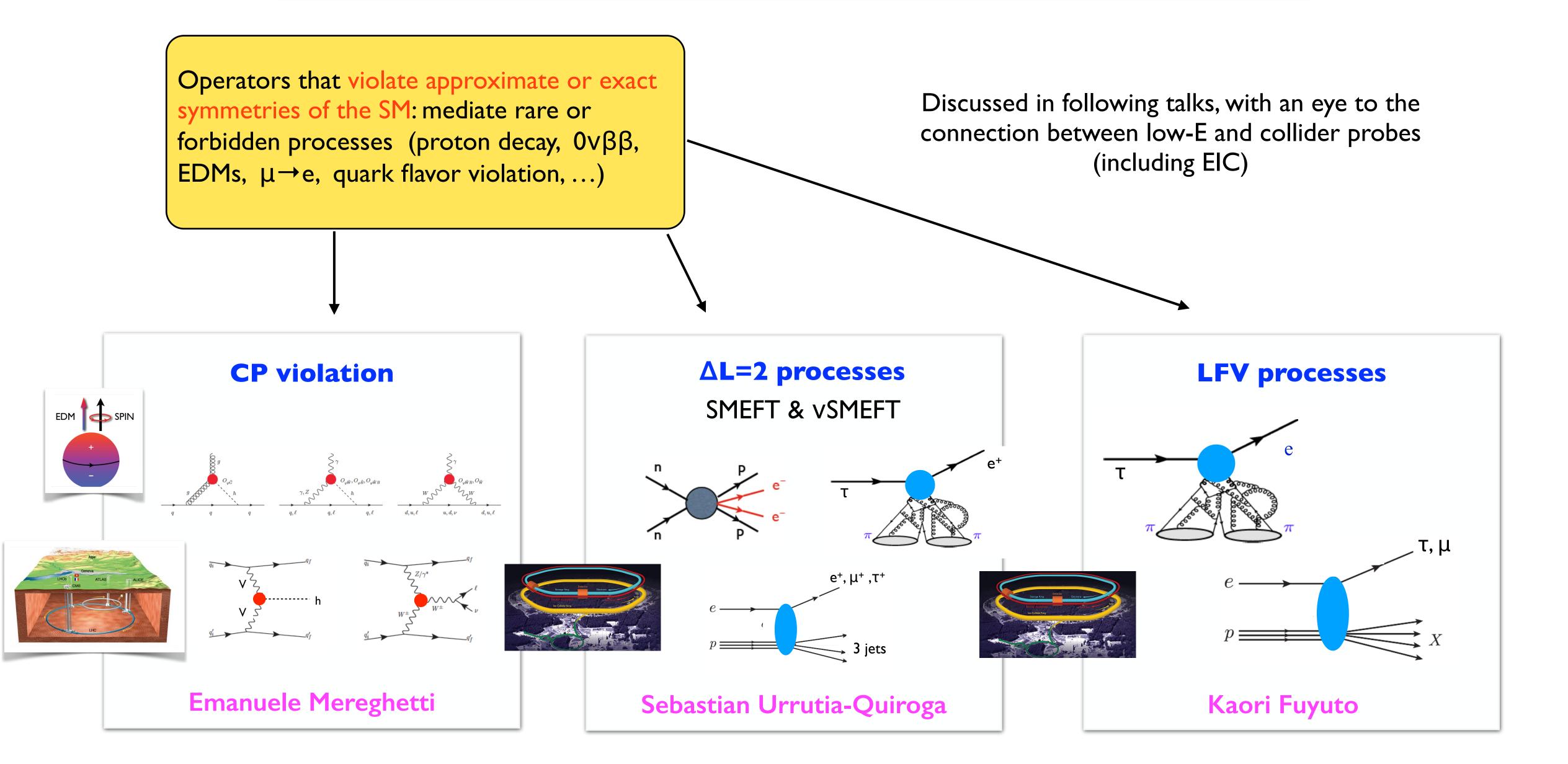


#### Two classes of SMEFT operators (↔ probes)

Operators that violate approximate or exact symmetries of the SM: mediate rare or forbidden processes (proton decay,  $0V\beta\beta$ , EDMs,  $\mu\rightarrow e$ , quark flavor violation, ...)

Operators that give corrections to SM "allowed" processes: probe them with precision measurements (muon g-2, weak decays, electron scattering ...)

#### Two classes of SMEFT operators (↔ probes)

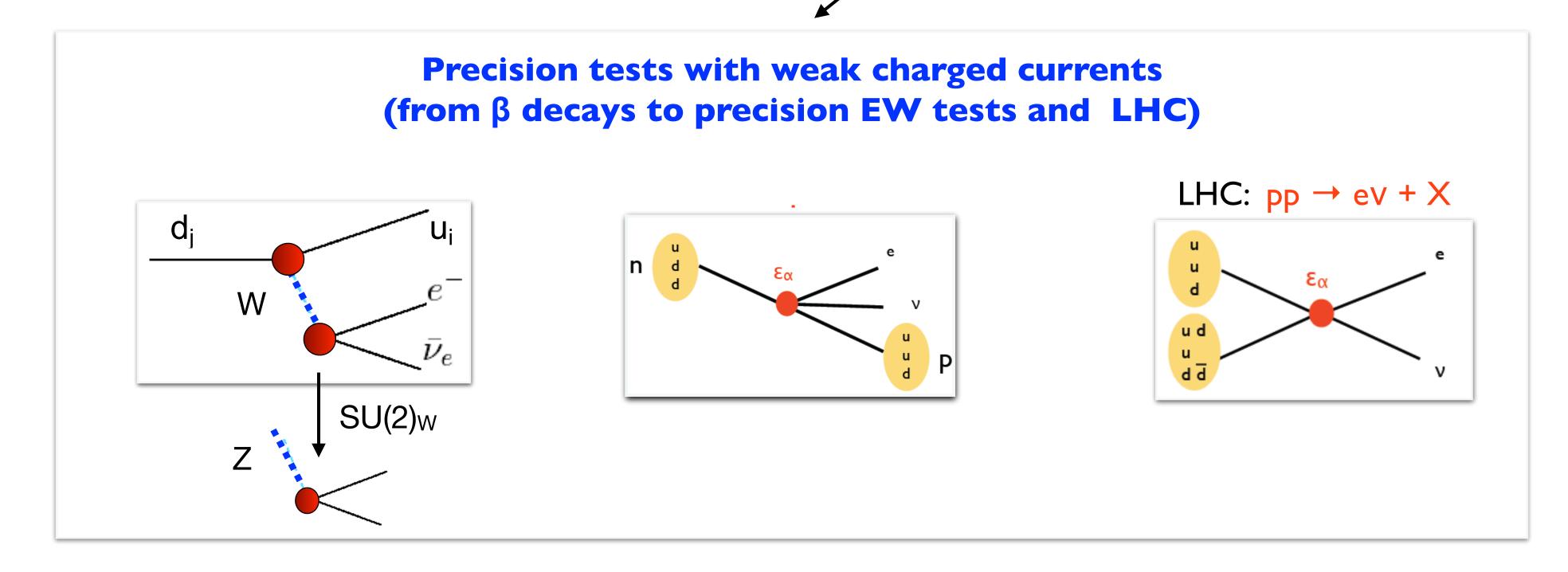


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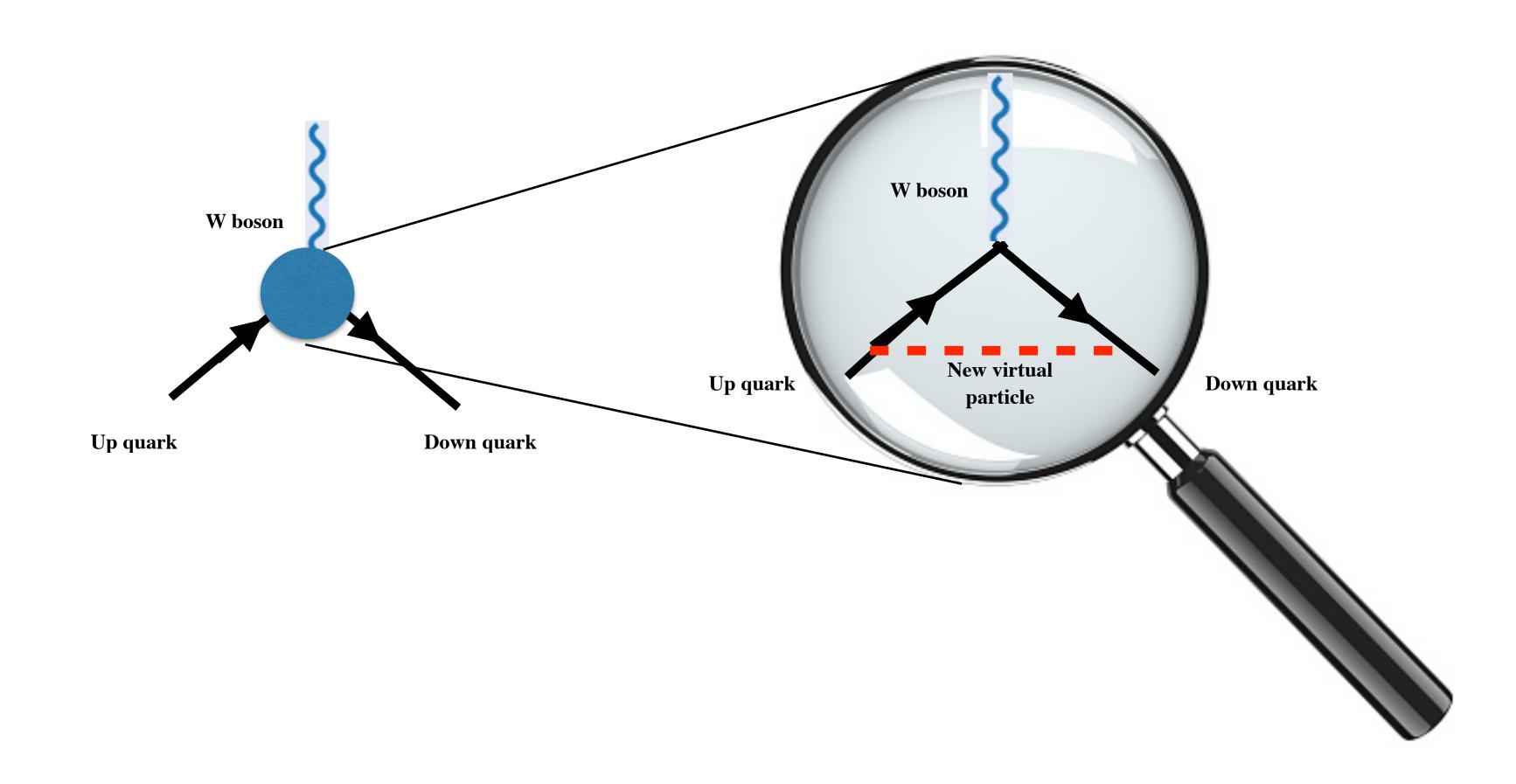
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In the rest of this talk

Operators that give corrections to SM "allowed" processes: probe them with precision measurements (muon g-2, weak decays, electron scattering ...)

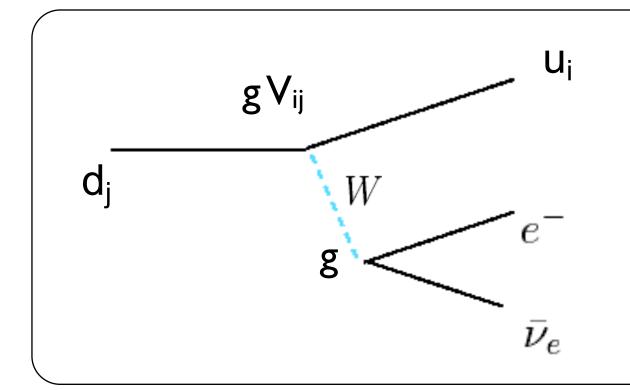


# Precision tests with weak charged currents



#### Charged current at low energy: 'B decays'

• In the SM, W exchange ⇒ only "V-A" + Cabibbo and lepton universality



$$G_F(\beta) \sim G_F(\mu) V_{ij} \sim I/v^2 V_{ij}$$

$$\begin{pmatrix}
V_{ud} & V_{us} & V_{ub} \\
V_{cd} & V_{cs} & V_{cb} \\
V_{td} & V_{ts} & V_{tb}
\end{pmatrix}$$

Cabibbo-Kobayashi-Maskawa

#### Cabibbo Universality

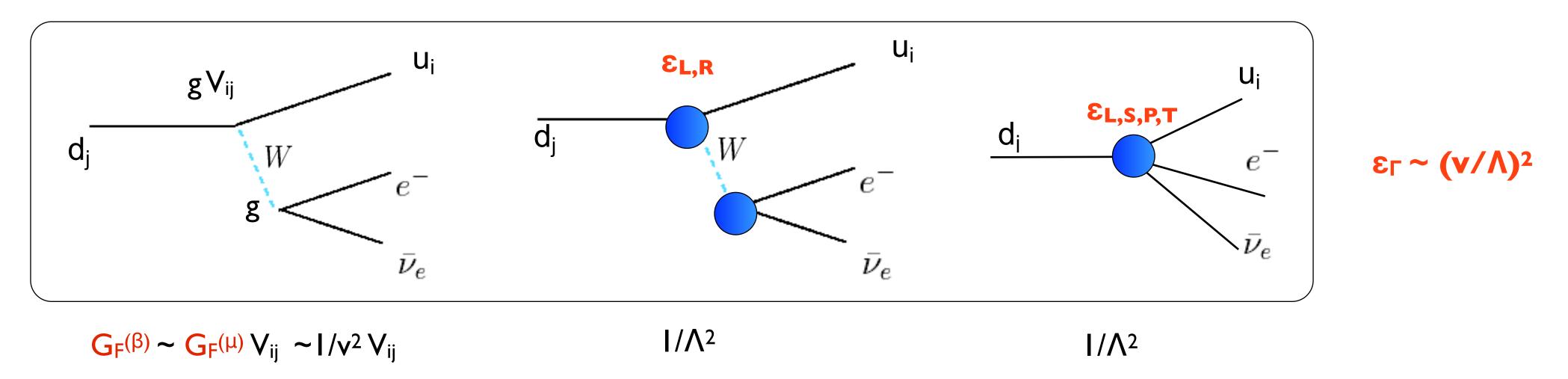
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

$$[G_F]_e/[G_F]_\mu = 1$$

Lepton Flavor Universality (LFU)

#### Charged current at low energy: 'B decays'

• In the SM, W exchange ⇒ only "V-A" + Cabibbo and lepton universality



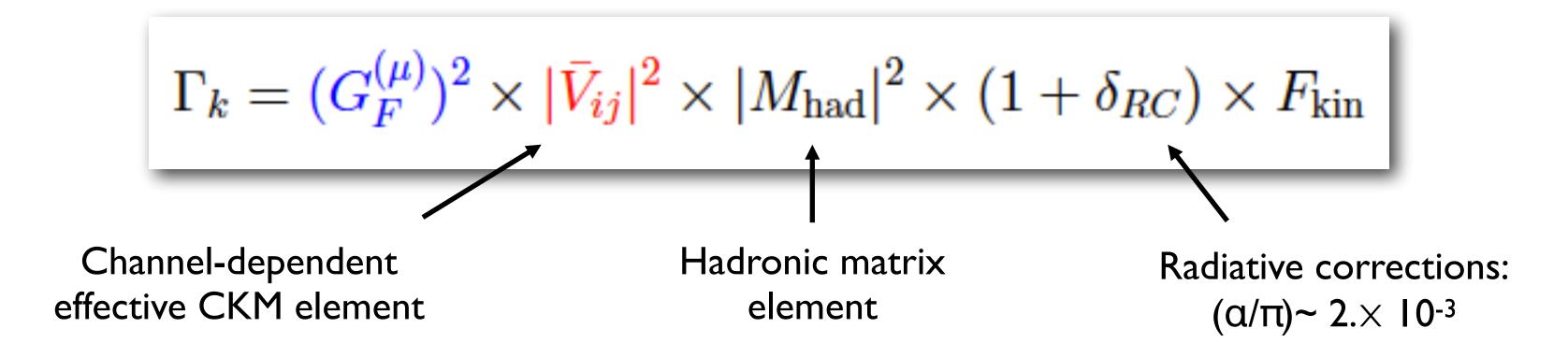
• New physics can spoil universality. With current precision of 0.1-0.01% we can probe  $\Lambda > 10$  TeV

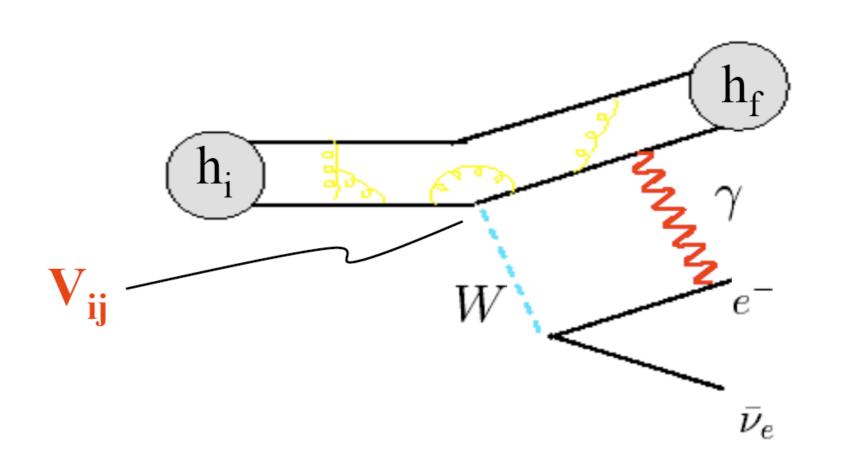
~0..95 ~0.05 ~1.5 × 10-5 
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$
  $\delta V_{ud} / V_{ud} \sim 0.02\% \qquad \delta V_{us} / V_{us} \sim 0.2\% \qquad \delta V_{ub} / V_{ub} \sim 5\%$ 

$$R_{e/\mu} = \Gamma (\pi \rightarrow e \nu) / \Gamma (\pi \rightarrow \mu \nu)$$
  $R_{e/\mu} (SM) = 1.23524 (015) \times 10^{-4}$  0.01%  $R_{e/\mu} (Exp) = 1.23270 (230) \times 10^{-4}$  0.18%

#### Cabibbo universality tests

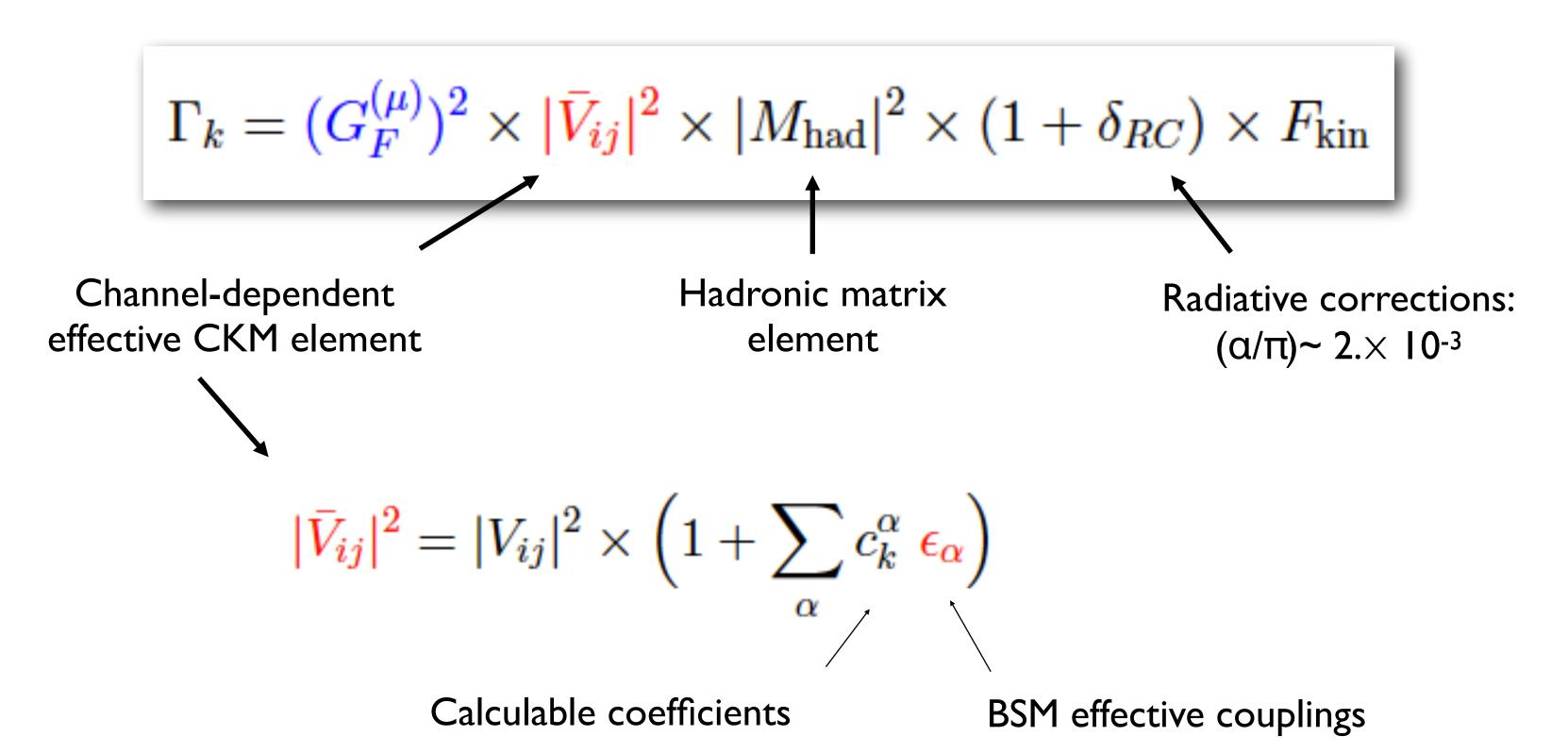
Extract  $V_{ud} = Cos\theta_C$  and  $V_{us} = Sin\theta_C$  from meson, neutron & nuclear decays





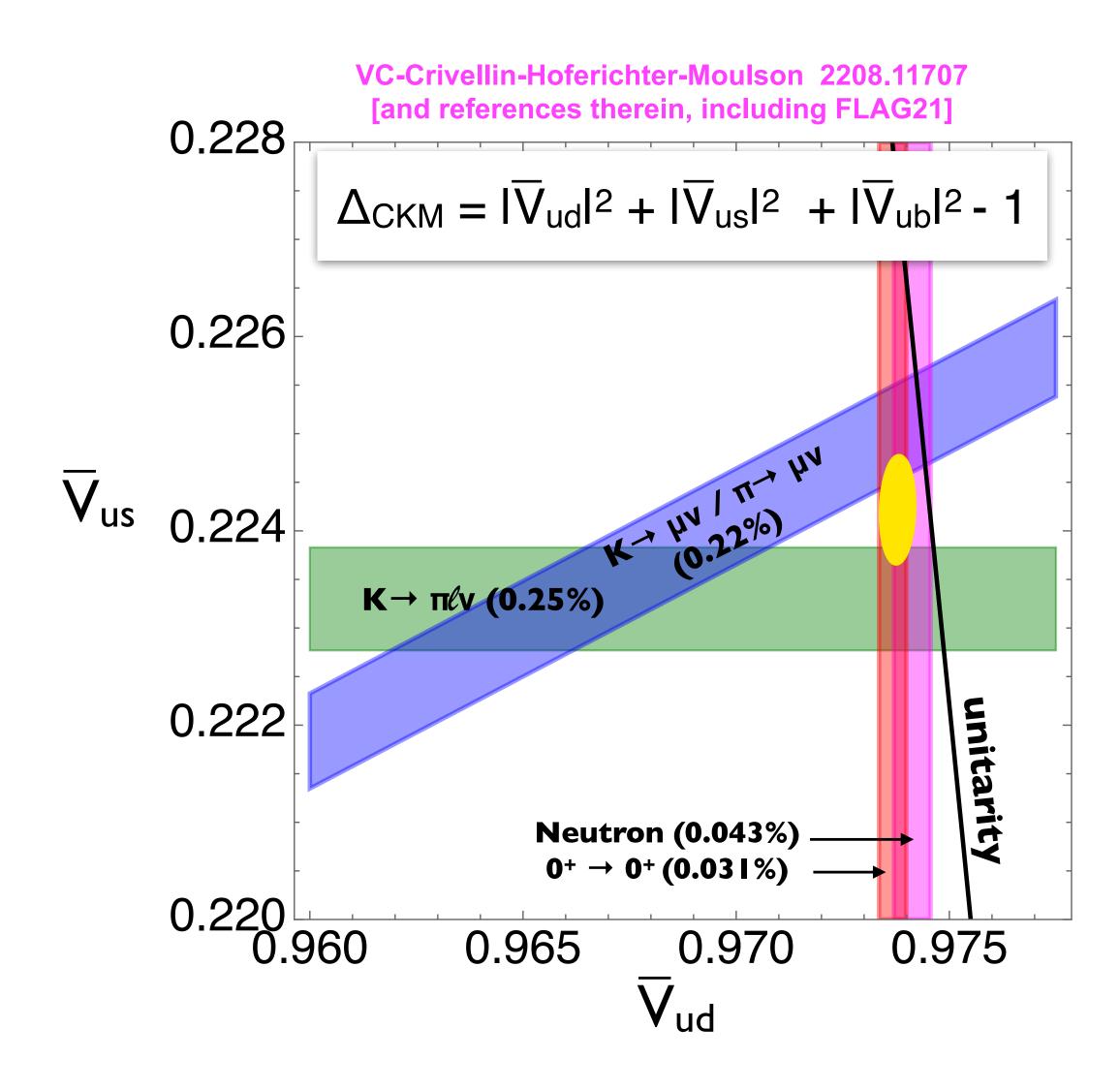
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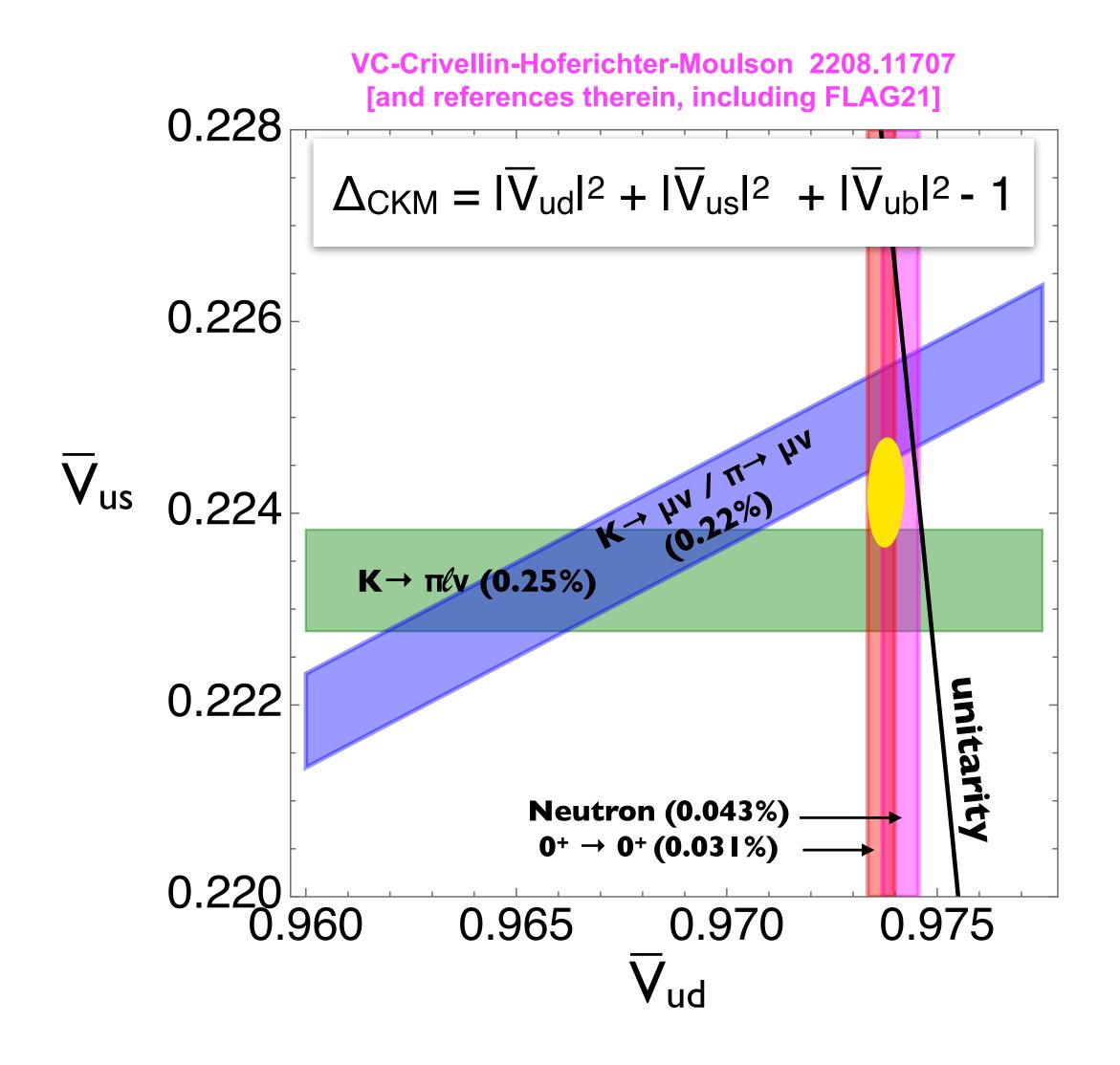
$$|\bar{V}_{ud}|^2 + |\bar{V}_{us}|^2 + |\bar{V}_{ub}|^2 = 1 + \Delta_{\text{CKM}}(\epsilon_i)$$

#### The Cabibbo Angle Anomaly



- Bands should intersect in a single region and that region should overlap with the unitarity circle
- $\sim 3\sigma$  problem even in meson sector (KI2 vs KI3)
- ~3 $\sigma$  effect in global fit ( $\Delta_{CKM}$ = -1.48(53)  $\times$  10-3)

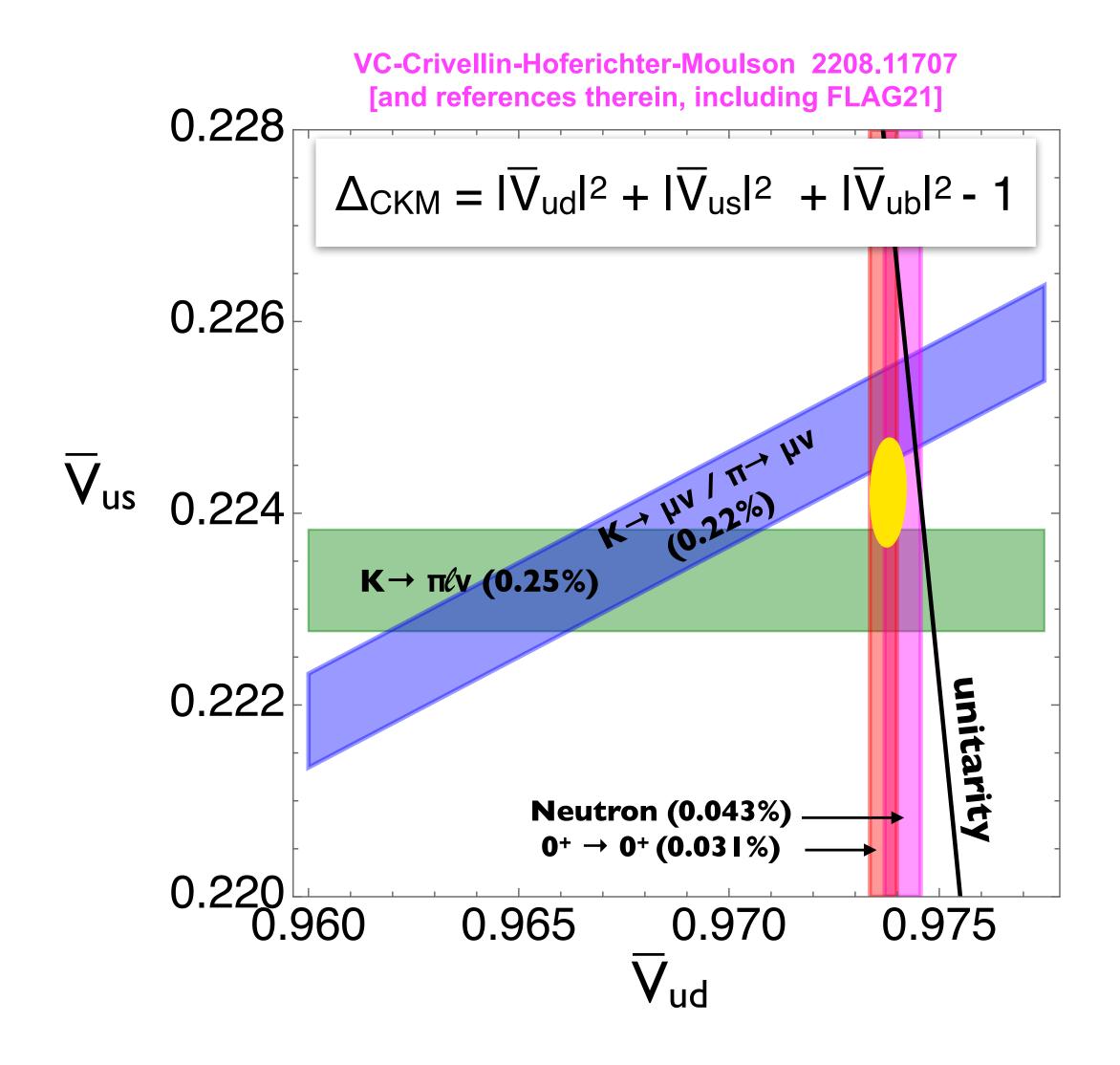
#### The Cabibbo Angle Anomaly



#### Expected experimental improvement:

- neutron decay (will match nominal nuclear uncertainty)
- pion beta decay (6x to 10x at PIONEER phases II, III)
- new  $K_{\mu 3}/K_{\mu 2}$  BR measurement at NA62
- Expected theoretical scrutiny
  - Lattice:  $K \rightarrow \pi$  vector f.f. and rad. corr. for KI3
  - EFT for neutron and nuclei, with goal  $\delta\Delta_{RC}$  ~ 2× 10-4
  - Ab-initio nuclear structure calculations
  - •
- Possible BSM explanations

#### The Cabibbo Angle Anomaly

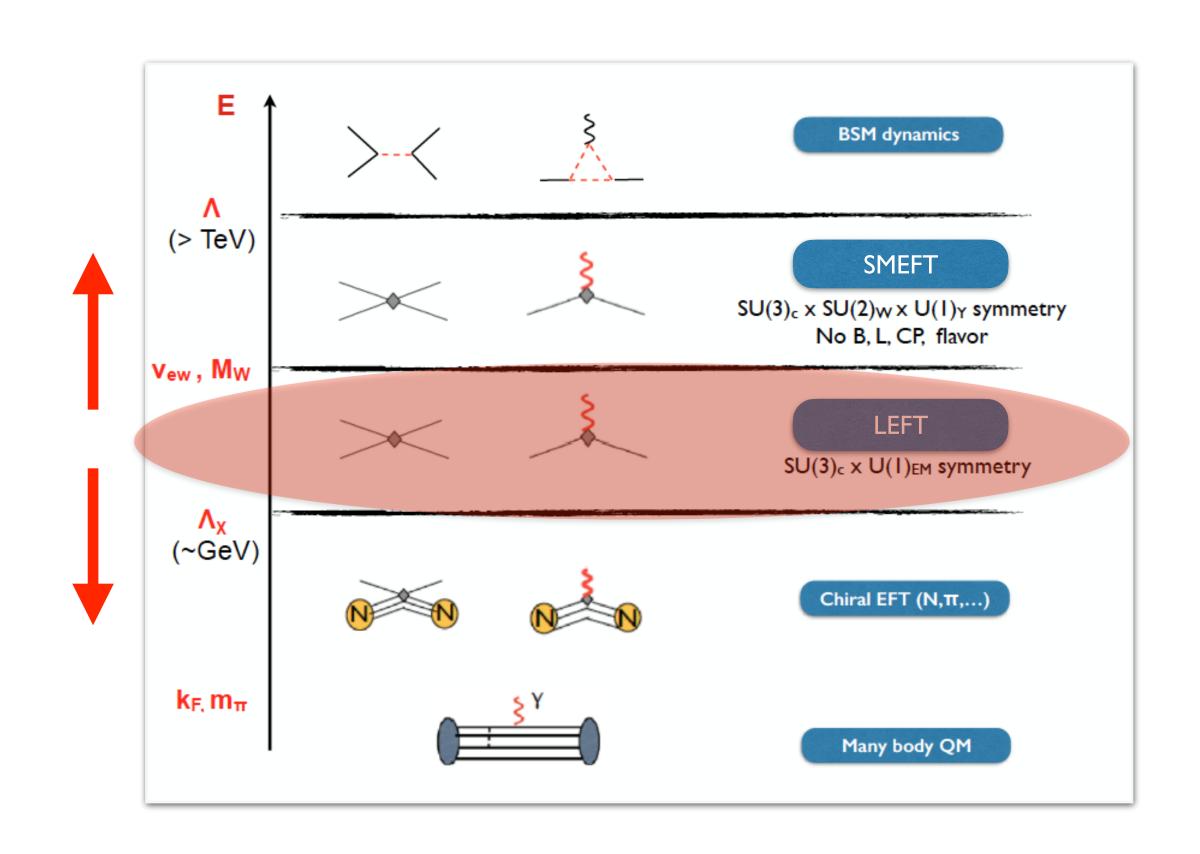


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  - •
- Possible BSM explanations

Will discuss in the SMEFT framework

# Connecting scales & processes (I)

To connect UV physics to beta decays, use EFT



- Start with GeV scale effective Lagrangian
  - Leading (dim-6) new physics effects are encoded in 5 quark-level operators (up to flavor indices)
  - Quark-level version of Lee-Yang effective Lagrangian

## GeV-scale effective Lagrangian (LEFT)

VC, Gonzalez-Alonso, Jenkins 0908.1754, NPB

VC, Graesser, Gonzalez-Alonso 1210.4553, JHEP

Leptonic interactions

$$\mathcal{L}_{CC}^{(\mu)} = -\frac{G_F^{(0)}}{\sqrt{2}} \left( 1 + \epsilon_L^{(\mu)} \right) \bar{e} \gamma^{\rho} (1 - \gamma_5) \nu_e \cdot \bar{\nu}_{\mu} \gamma_{\rho} (1 - \gamma_5) \mu + \dots$$

Semi-leptonic interactions

$$\mathcal{L}_{CC} = -\frac{G_F^{(0)} V_{uD}}{\sqrt{2}} \times \left[ \left( 1 + \epsilon_L^{\ell D} \right) \ \bar{e} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d \right]$$

$$+ \epsilon_R^D \ \bar{\ell} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 + \gamma_5) d$$

$$+ \epsilon_S^{\ell D} \ \bar{\ell} (1 - \gamma_5) \nu_\ell \cdot \bar{u} d$$

$$\epsilon_{i} \sim (v/\Lambda)^2$$

$$\ell = e, \mu$$

D = d, s

$$- \epsilon_P^{\ell D} \bar{\ell} (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma_5 d$$

+ 
$$\epsilon_T^{\ell D} \bar{\ell} \sigma_{\mu\nu} (1 - \gamma_5) \nu_{\ell} \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) d$$
 + h.c.

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$$\frac{G_F^{(\mu)} V_{ud}}{\sqrt{2}} \left(1 - \epsilon_L^{(\mu)}\right) \qquad \text{Semi-leptonic interactions}$$

$$\mathcal{L}_{CC} = -\frac{G_F^{(0)} V_{uD}}{\sqrt{2}} \times \left[ \left(1 + \epsilon_L^{\ell D}\right) \bar{e} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d \right]$$

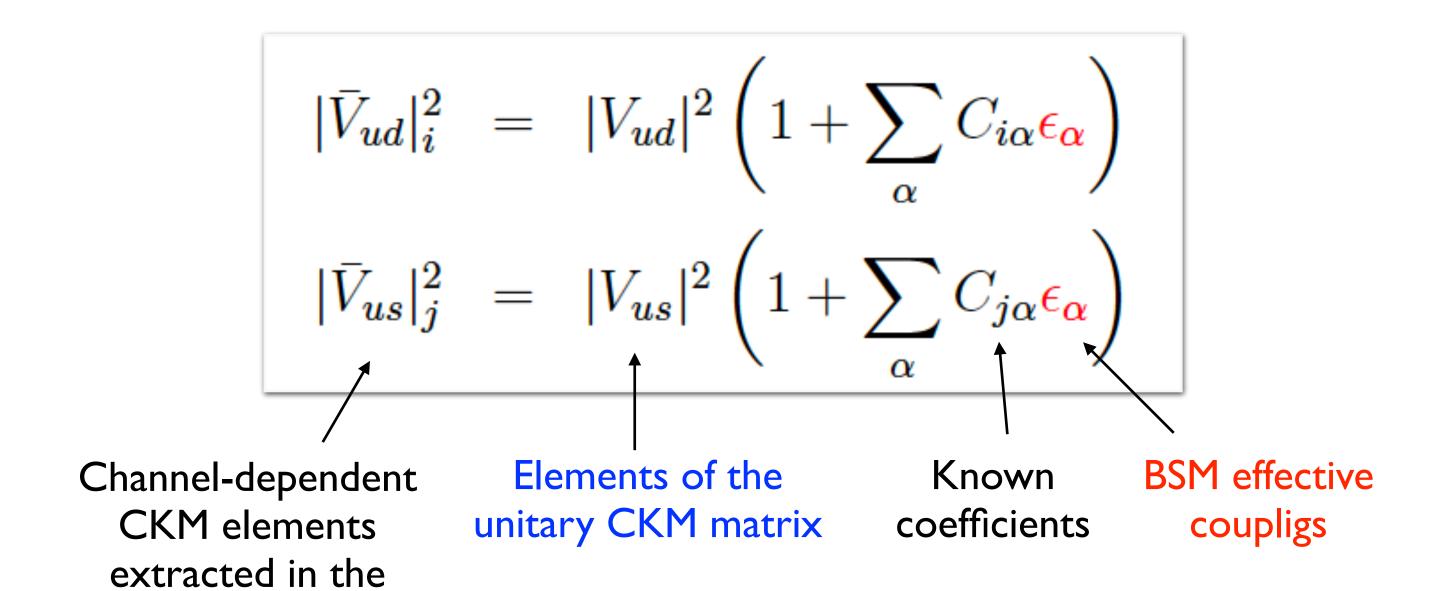
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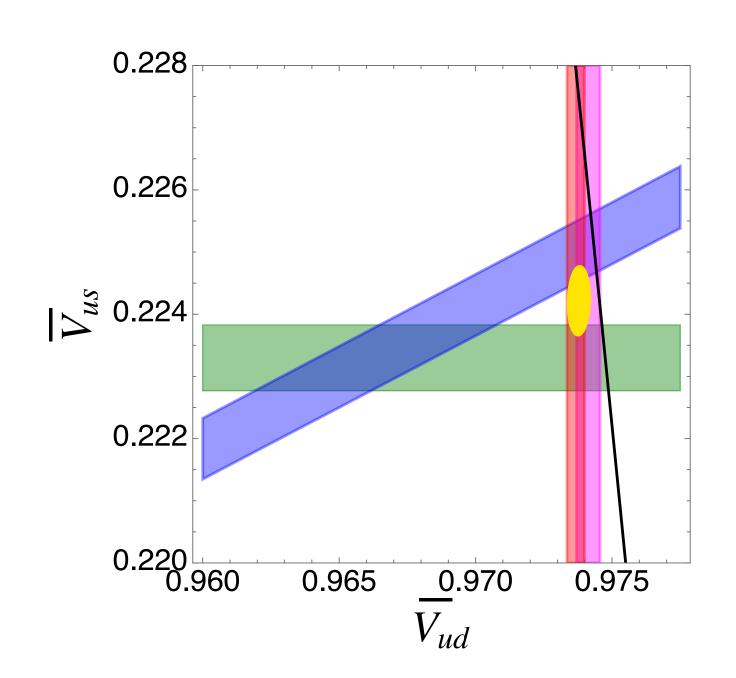
$$- \epsilon_P^{\ell D} \bar{\ell} (1 - \gamma_5) \nu_\ell \cdot \bar{u} \gamma_5 d$$

$$+ \epsilon_T^{\ell D} \bar{\ell} \sigma_{\mu\nu} (1 - \gamma_5) \nu_\ell \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) d \right] + \text{h.c.}$$

#### Corrections to V<sub>ud</sub> and V<sub>us</sub>



'SM-like analysis'

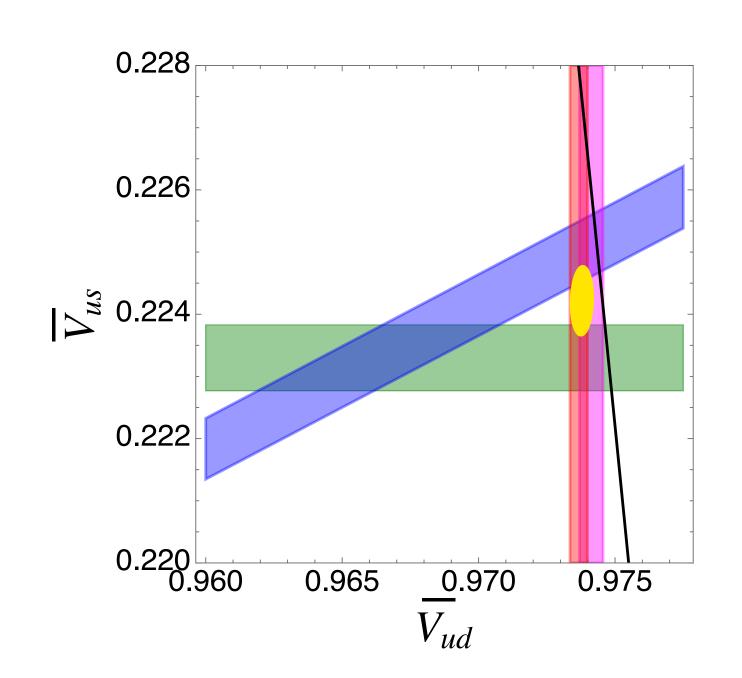


Find set of  $\varepsilon$ 's so that  $V_{ud}$  and  $V_{us}$  bands meet on the unitarity circle

#### Corrections to V<sub>ud</sub> and V<sub>us</sub>

$$|\bar{V}_{ud}|_i^2 = |V_{ud}|^2 \left(1 + \sum_{\alpha} C_{i\alpha} \epsilon_{\alpha}\right)$$
 
$$|\bar{V}_{us}|_j^2 = |V_{us}|^2 \left(1 + \sum_{\alpha} C_{j\alpha} \epsilon_{\alpha}\right)$$
 Channel-dependent CKM elements of the unitary CKM matrix coefficients extracted in the

'SM-like analysis'

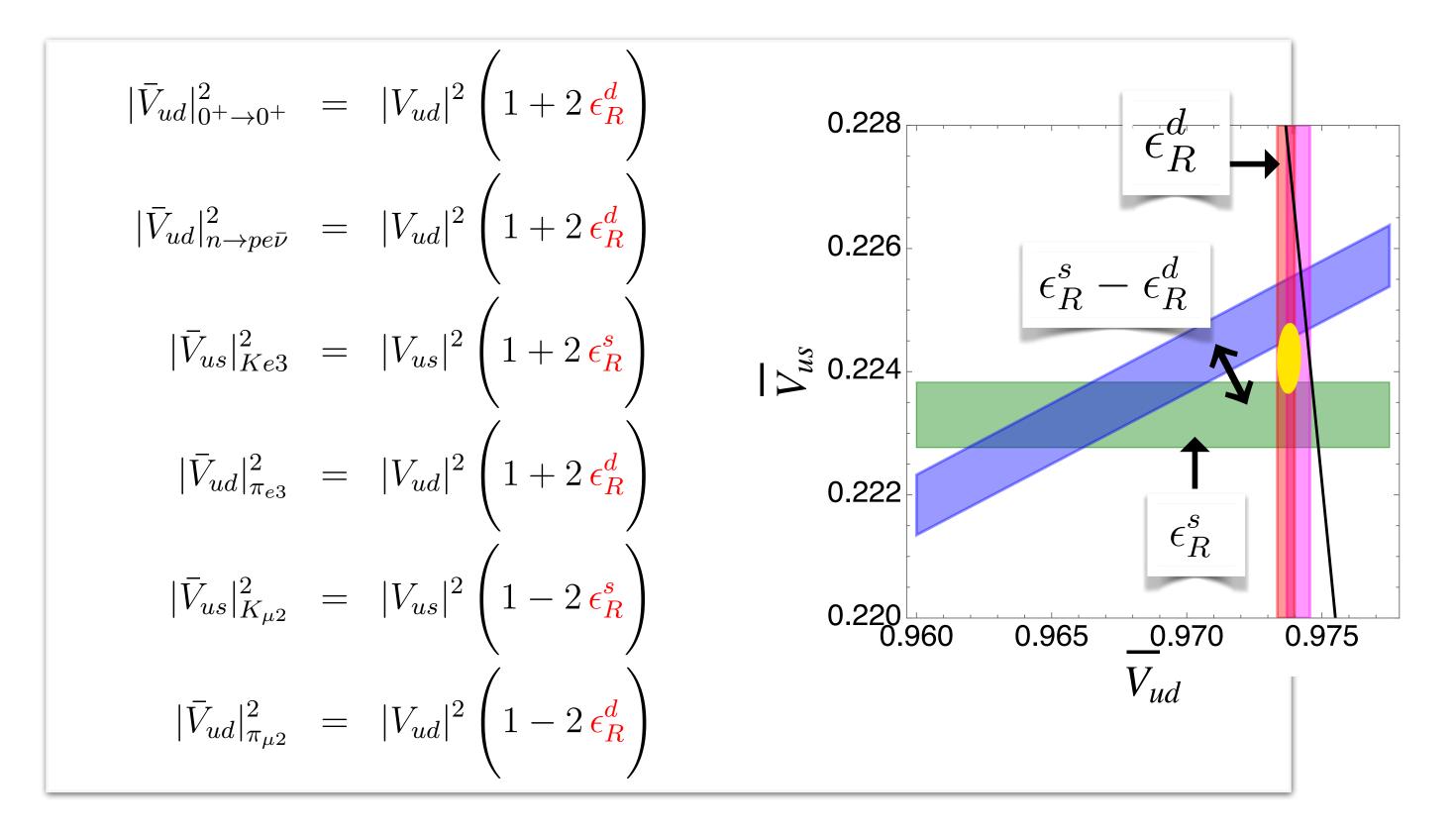


Find set of  $\varepsilon$ 's so that  $V_{ud}$  and  $V_{us}$  bands meet on the unitarity circle

Simplest 'solution': right-handed (V+A) quark currents

#### Right-handed quark couplings

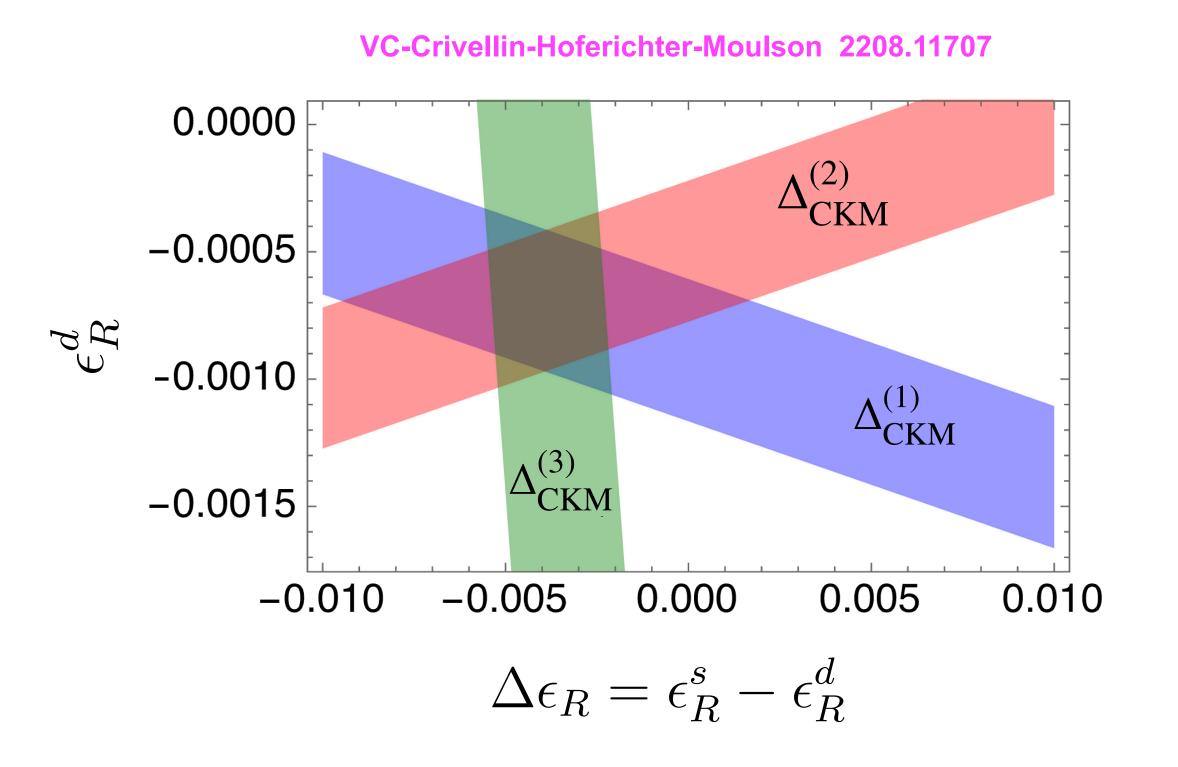
• Right-handed currents (in the 'ud' and 'us' sectors)



Alioli et al 1703.04751
Grossman-Passemar-Schacht
1911.07821
VC-Crivellin-HoferichterMoulson 2208.11707
VC, W. Dekens, J. De Vries, E.
Mereghetti, T. Tong, 2311.00021

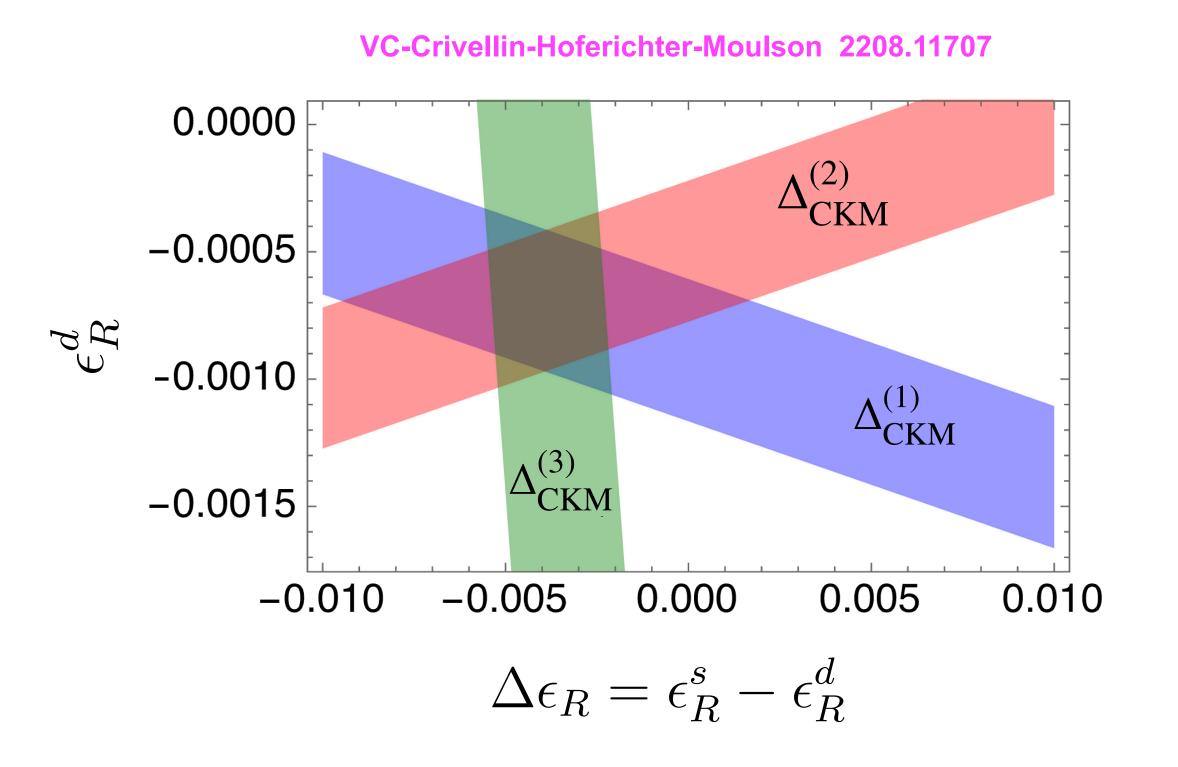
• CKM elements from vector (axial) channels are shifted by  $1+\epsilon_R$   $(1-\epsilon_R) \Rightarrow V_{us}/V_{ud}$ ,  $V_{ud}$  and  $V_{us}$  shift in anti-correlated way, can resolve all tensions!

#### Unveiling R-handed quark currents?



- Preferred ranges are not in conflict with constraints from other low-E probes
- Does the R-handed current explanation survive after taking into account high energy data?

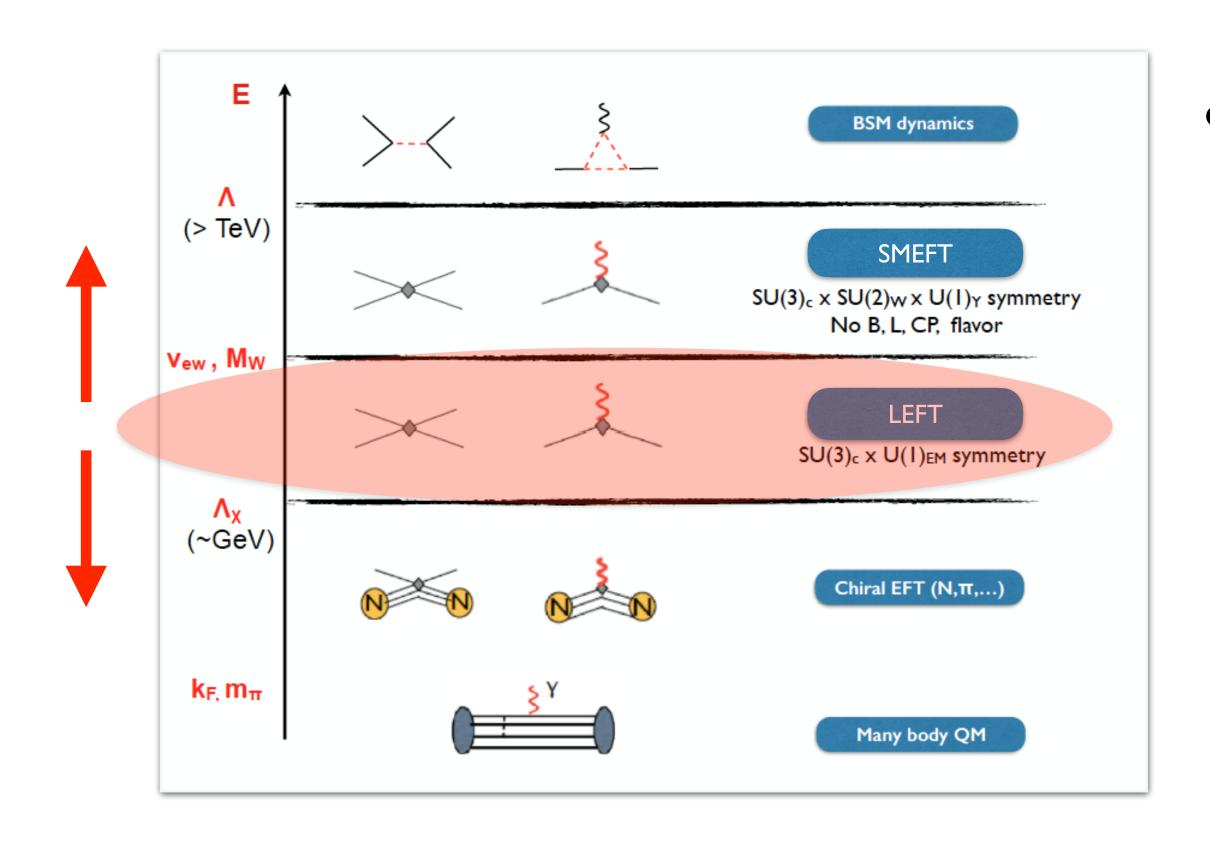
#### Unveiling R-handed quark currents?



- Preferred ranges are not in conflict with constraints from other low-E probes
- Does the R-handed current explanation survive after taking into account high energy data? Yes!

## Connecting scales & processes (2)

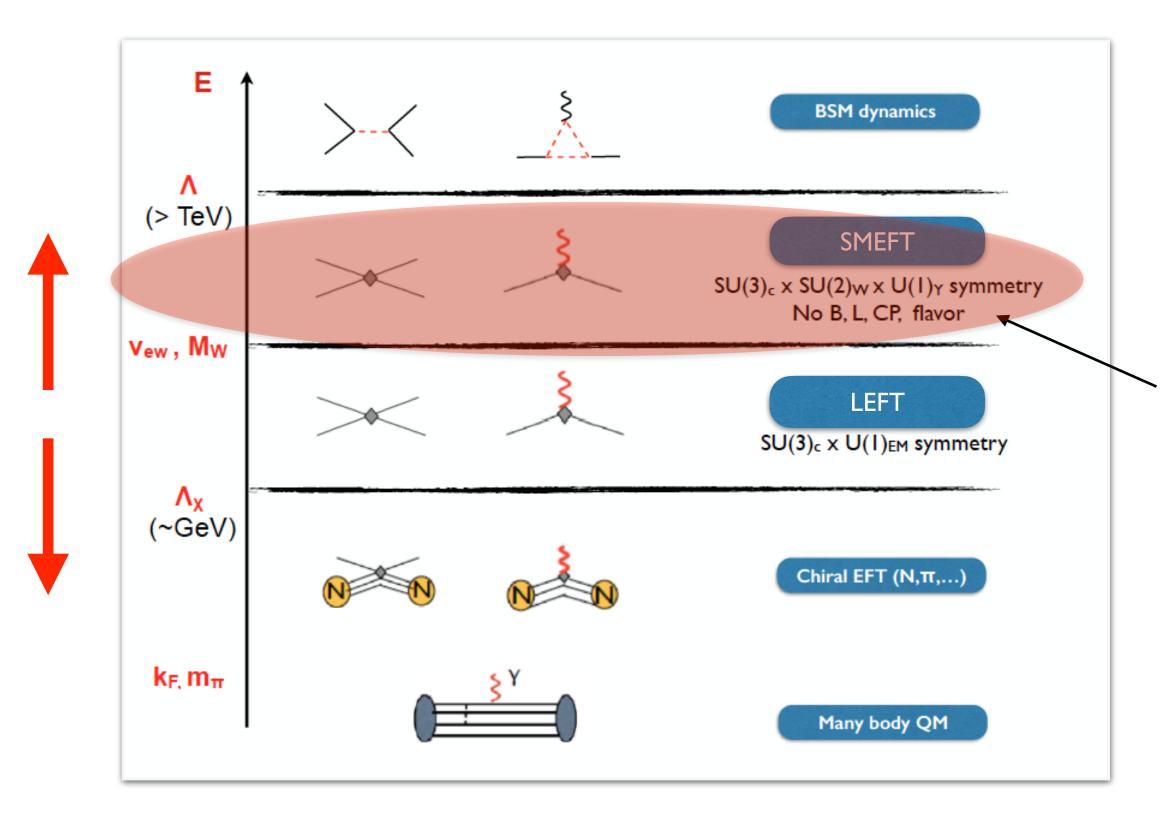
To connect UV physics to beta decays, use EFT



• Need to know high-scale origin of the various  $\varepsilon_{\alpha}$ 

## Connecting scales & processes (2)

To connect UV physics to beta decays, use EFT



- Need to know high-scale origin of the various  $\epsilon_{\alpha}$
- Tree-level LEFT-SMEFT (dim-6) matching at scale  $\mu_W$  ~ 246 GeV
- Leading-log SMEFT (dim-6) running between  $\Lambda$  and  $\mu_W$  is known R. Alonso, E. Jenkins, A. Manohar, M. Trott, 1308.2627, 1310.4838, 1312. 2014

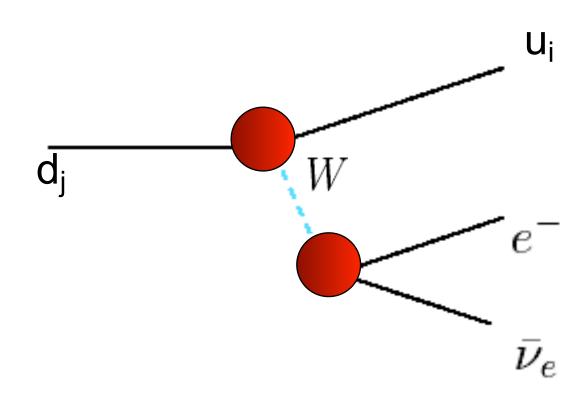
M. Dawid, VC, W. Dekens 2402.06723

One loop SMEFT-LEFT matching also known

W. Dekens, P, Stoffer 1908.05295

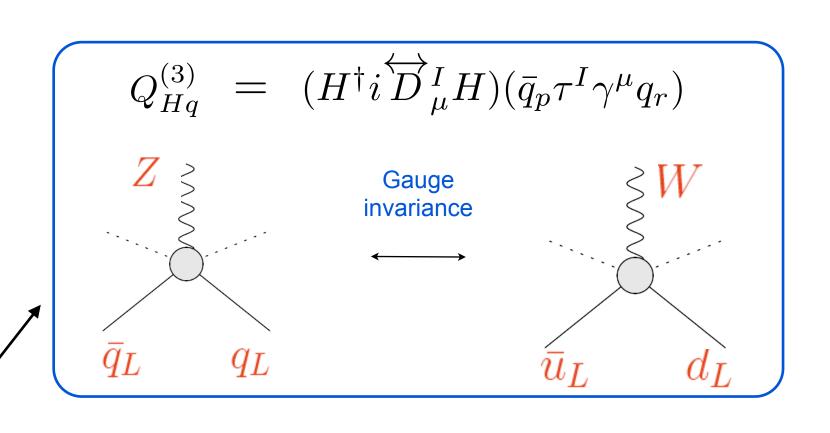
#### Weak scale effective Lagrangian (SMEFT)

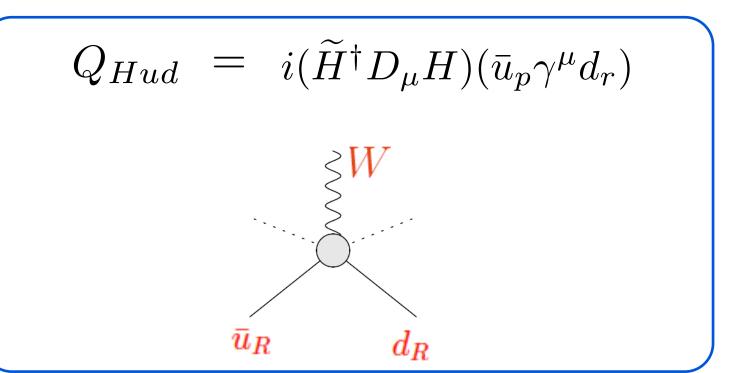
ε<sub>L,R</sub> originate from SU(2)xU(1) invariant vertex corrections



Building blocks

$$l^i = \begin{pmatrix} \nu_L^i \\ e_L^i \end{pmatrix} \qquad q^i = \begin{pmatrix} u_L^i \\ d_L^i \end{pmatrix} \qquad H) = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix}$$





Can be generated by  $W_L$ - $W_R$  mixing in Left-Right symmetric models or by exchange of vector-like quarks

Dekens, Andreoli, de Vries, Mereghetti, Oosterhof, 2107.10852 Belfatto-Berezhiani 2103.05549 Belfatto-Trifinopoulos 2302.14097

2L

 $\epsilon_{R}$ 

#### Weak scale effective Lagrangian (SMEFT)

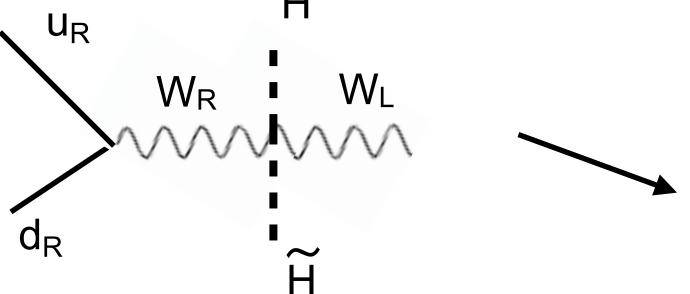
**EL,R** originate from SU(2)xU(1) invariant vertex corrections

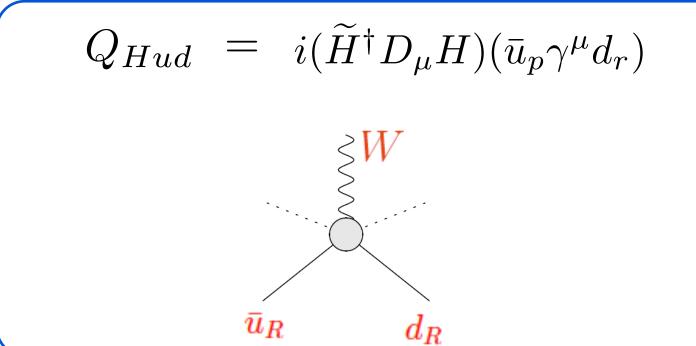


εL

W<sub>L</sub>-W<sub>R</sub> mixing in LRSM

Dekens, Andreoli, de Vries, Mereghetti, Oosterhof, 2107.10852





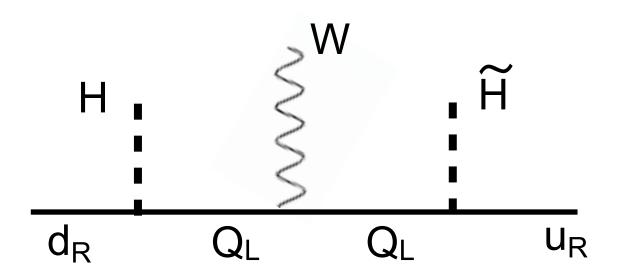
invariance

 $(H^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}H)(\bar{q}_{p}\tau^{I}\gamma^{\mu}q_{r})$ 

 $\epsilon_{R}$ 

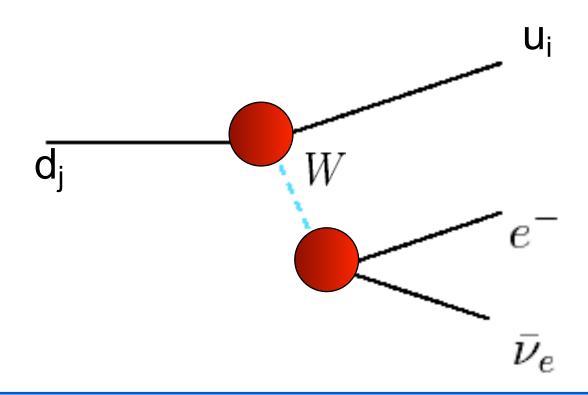
Vector-like quarks

Belfatto-Berezhiani 2103.05549. ... Belfatto-Trifinopoulos 2302.14097



#### Weak scale effective Lagrangian (SMEFT)

ε<sub>L,R</sub> originate from SU(2)xU(1) invariant vertex corrections



$$\epsilon_{\text{R}}$$

EL

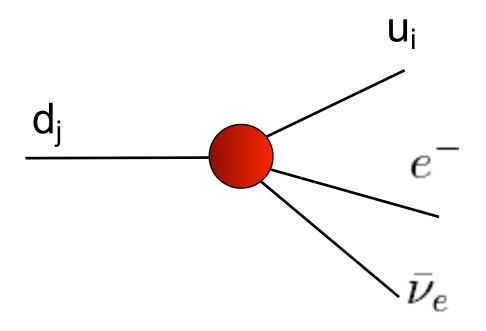
2L

$$Q_{Hud} = i(\widetilde{H}^{\dagger}D_{\mu}H)(\overline{u}_{p}\gamma^{\mu}d_{r})$$

$$Q_{Hq}^{(3)} = (H^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}H)(\overline{q}_{p}\tau^{I}\gamma^{\mu}q_{r})$$

$$Q_{Hl}^{(3)} = (H^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}H)(\overline{l}_{p}\tau^{I}\gamma^{\mu}l_{r})$$

**Es,P,T** and one contribution to **EL** arise from SU(2)xU(1) invariant 4-fermion operators



$$Q_{ledq} = (\bar{l}e)(\bar{d}q) + \text{h.c.}$$

$$Q_{lequ}^{(1)} = (\bar{l}_a e)\epsilon^{ab}(\bar{q}_b u) + \text{h.c.}$$

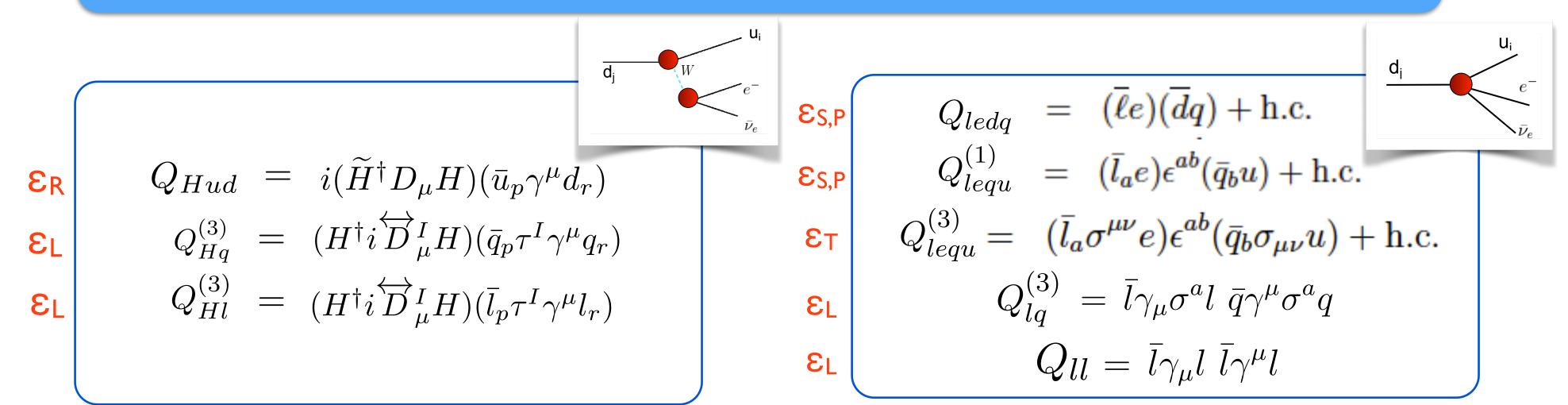
$$Q_{lequ}^{(3)} = (\bar{l}_a \sigma^{\mu\nu} e)\epsilon^{ab}(\bar{q}_b \sigma_{\mu\nu} u) + \text{h.c.}$$

$$Q_{lequ}^{(3)} = \bar{l}\gamma_{\mu}\sigma^a l \ \bar{q}\gamma^{\mu}\sigma^a q$$

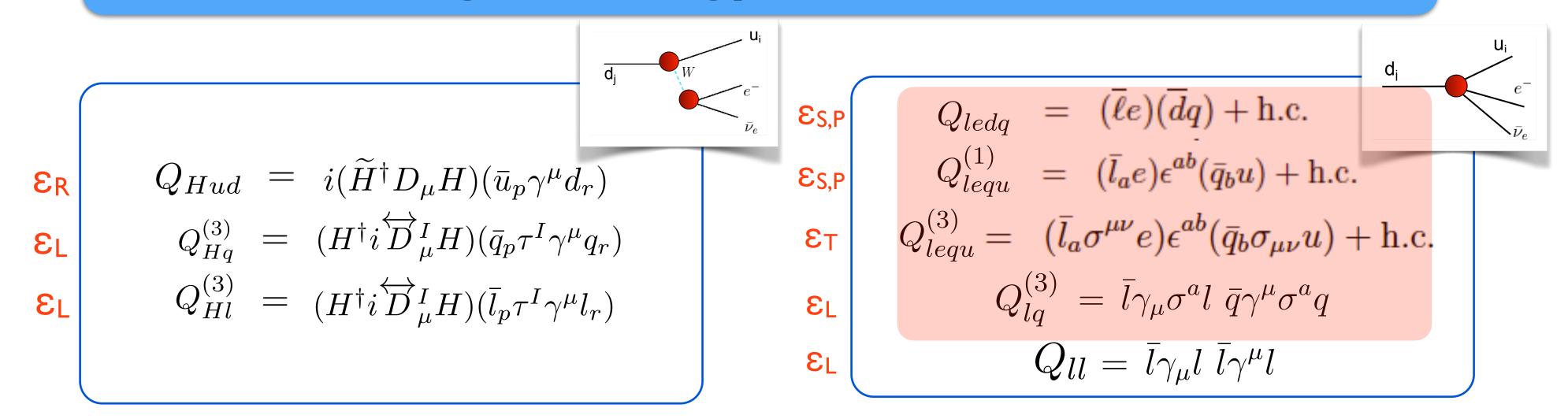
$$Q_{ll} = \bar{l}\gamma_{\mu}l \ \bar{l}\gamma^{\mu}l$$

$$\mathcal{E}_{L}$$

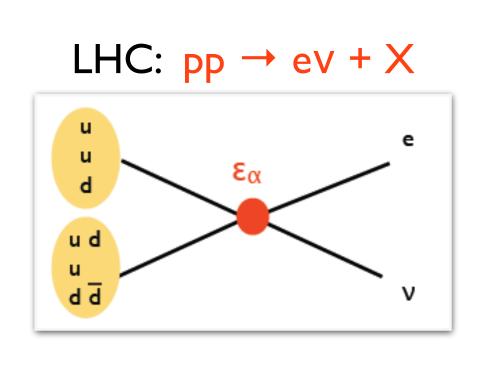
#### High Energy constraints

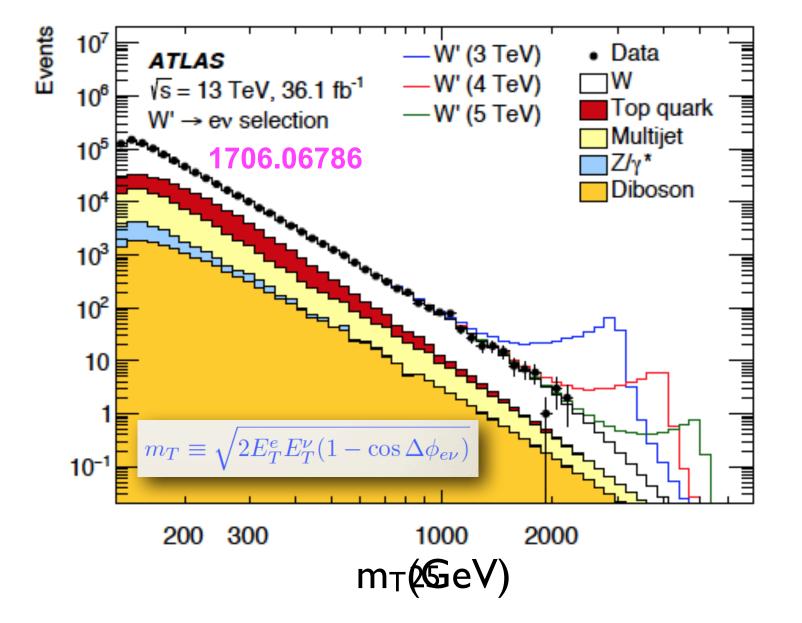


#### High Energy constraints



#### Contribute tp pp $\rightarrow$ ev+X and pp $\rightarrow$ e<sup>+</sup>e<sup>-</sup> +X at the LHC



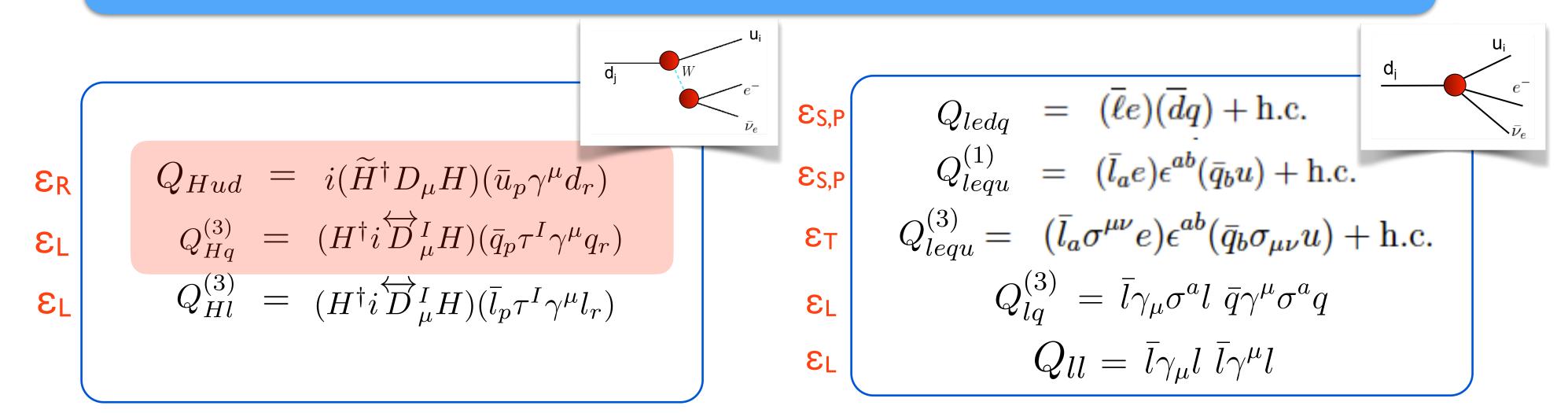


 $\epsilon_{\alpha} \sim 10^{-3} - 10^{-4}$ 

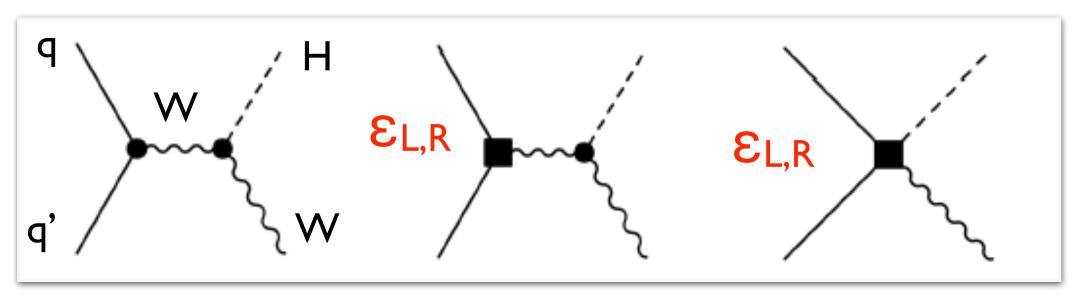
VC, Graesser, Gonzalez-Alonso 1210.4553 Alioli-Dekens-Girard-Mereghetti 1804.07407 Gupta et al. 1806.09006 Boughezal-Mereghetti-Petriello 2106.05337

• • • •

#### High Energy constraints



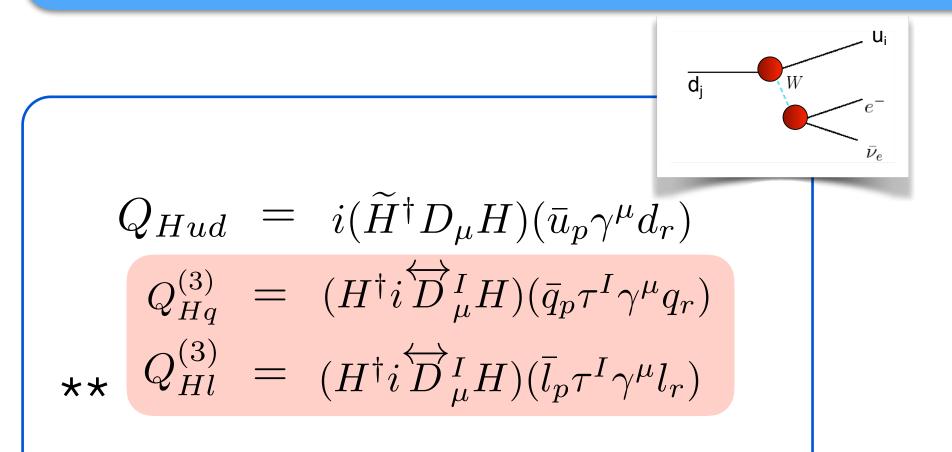
#### Can be probed at the LHC by associated Higgs + W production



S. Alioli, VC, W. Dekens, J. de Vries, E. Mereghetti 1703.04751

Current LHC results allow for to  $\varepsilon_{L,R} \sim 5\%$ 

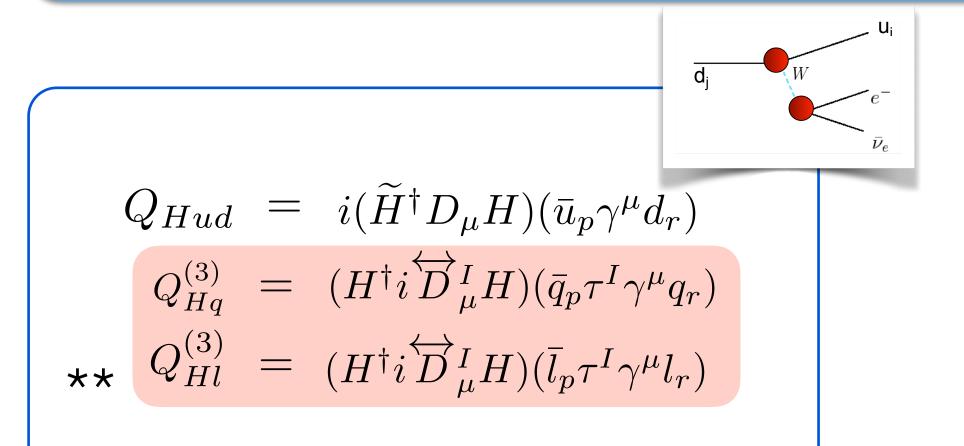
### High Energy constraints



$$Q_{ledq} = (\bar{l}e)(\bar{d}q) + \mathrm{h.c.}$$
 $Q_{lequ}^{(1)} = (\bar{l}_a e)\epsilon^{ab}(\bar{q}_b u) + \mathrm{h.c.}$ 
 $Q_{lequ}^{(3)} = (\bar{l}_a \sigma^{\mu\nu} e)\epsilon^{ab}(\bar{q}_b \sigma_{\mu\nu} u) + \mathrm{h.c.}$ 
 $Q_{lq}^{(3)} = \bar{l}\gamma_{\mu}\sigma^a l \ \bar{q}\gamma^{\mu}\sigma^a q$ 
 $\psi \star \qquad Q_{ll} = \bar{l}\gamma_{\mu} l \ \bar{l}\gamma^{\mu} l$ 

Contribute to Z-pole and other precision electroweak (EW) observables, including\*\* Mw

### High Energy constraints



$$Q_{ledq} = (\bar{l}e)(\bar{d}q) + \text{h.c.}$$

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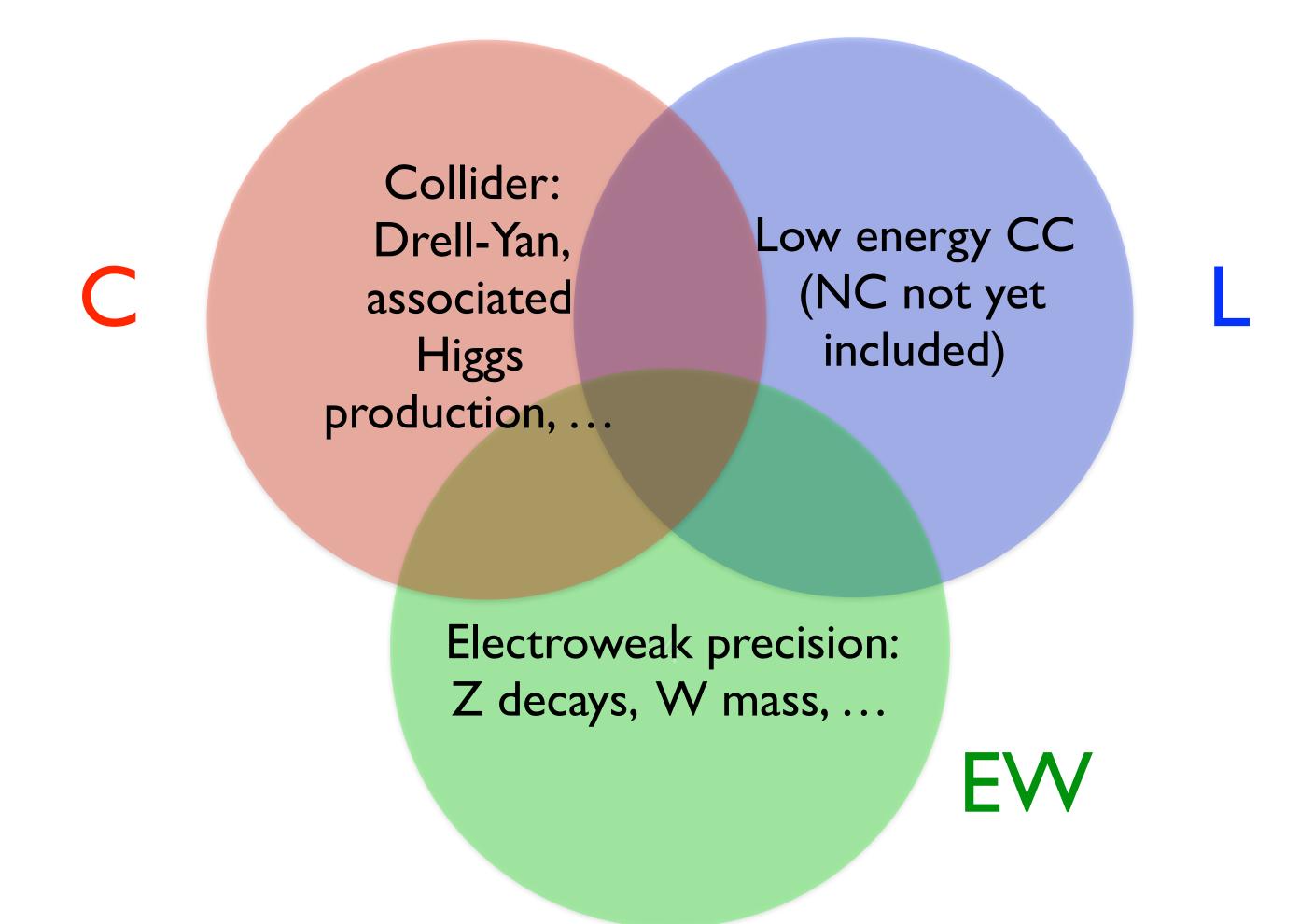
$$Q_{lq}^{(3)} = \bar{l}\gamma_{\mu}\sigma^a l \ \bar{q}\gamma^{\mu}\sigma^a q$$

$$\star \star \qquad Q_{ll} = \bar{l}\gamma_{\mu} l \ \bar{l}\gamma^{\mu} l$$

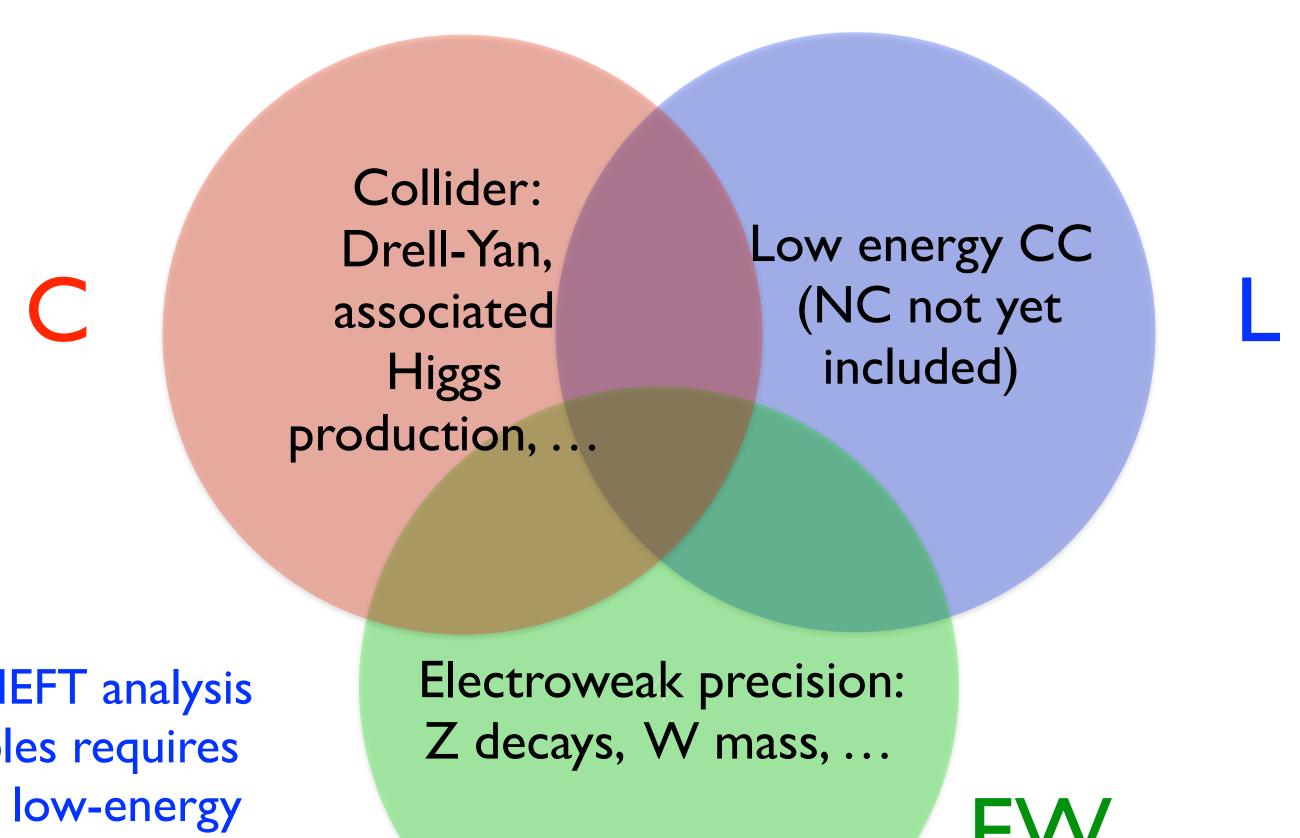
Contribute to Z-pole and other precision electroweak (EW) observables, including  $^{**}$   $M_W$ 

Example:  $\frac{\delta m_W^2}{m_W^2} = v^2 \; \frac{s_w c_w}{s_w^2 - c_w^2} \left[ 2 \, C_{HWB} + \frac{c_w}{2 s_w} \, C_{HD} + \frac{s_w}{c_w} \left( 2 \, \frac{C_{Hl}^{(3)}}{c_w} - \hat{C}_{ll} \right) \right]$  'Oblique corrections'  $\frac{\delta m_W^2}{m_W^2} = v^2 \; \frac{s_w c_w}{s_w^2 - c_w^2} \left[ 2 \, C_{HWB} + \frac{c_w}{2 s_w} \, C_{HD} + \frac{s_w}{c_w} \left( 2 \, \frac{C_{Hl}^{(3)}}{c_w} - \hat{C}_{ll} \right) \right]$  'Oblique corrections'

• A consistent analysis of β-decays in SMEFT requires data from, Collider, Low energy, and ElectroWeak tests



• A consistent analysis of β-decays in SMEFT requires data from, Collider, Low energy, and ElectroWeak tests



Corollary: a consistent SMEFT analysis of precision EW observables requires including constraints from low-energy CC processes (β-decays)

• A consistent analysis of β-decays in SMEFT requires data from, Collider, Low energy, and ElectroWeak tests

Minimal set of operators involved \*\*

$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum C$	$Q_i$
i	

Operators			EW	C		
	$H^4D^2$					
$Q_{HD}$	$\left(H^{\dagger}D^{\mu}H\right)^{*}\left(H^{\dagger}D_{\mu}H\right)$	pa	parameter shift $(m_Z)$			
	$X^2H^2$					
$Q_{HWB}$	$H^\dagger  au^I H  W^I_{\mu  u} B^{\mu  u}$	par	ramete	r shift $(\sin \theta_W)$		
	$\psi^2 H^2 D$					
$Q_{Hl}^{(1)}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\overline{l}_{p}\gamma^{\mu}l_{r})$	X	1	<b>✓</b>		
$Q_{Hl}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}_{\mu}^I H) (\bar{l}_p \tau^I \gamma^{\mu} l_r)$	1	<b>✓</b>	<b>✓</b>		
$Q_{He}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{e}_{p}\gamma^{\mu}e_{r})$		<b>✓</b>	<b>✓</b>		
$Q_{Hq}^{(1)}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{q}_{p}\gamma^{\mu}q_{r})$	X	<b>✓</b>	<b>✓</b>		
$Q_{Hq}^{(3)}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}H)(\bar{q}_{p}\tau^{I}\gamma^{\mu}q_{r})$	/	<b>✓</b>	<b>✓</b>		
$Q_{Hu}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{u}_{p}\gamma^{\mu}u_{r})$	X	<b>✓</b>	<b>✓</b>		
$Q_{Hd} \qquad H^{\dagger} i \overleftrightarrow{D}_{\mu} H) (\bar{d}_p \gamma^{\mu} d_r) \qquad $			<b>✓</b>	<b>✓</b>		
$Q_{Hud}$ + h.c.	$i(\widetilde{H}^{\dagger}D_{\mu}H)(\bar{u}_{p}\gamma^{\mu}d_{r})$	1	X	✓		

Operators			EW	C		
	$(ar{L}L)(ar{L}L)$					
$Q_{ll}$	$(\bar{l}_p\gamma^\mu l_r)(\bar{l}_s\gamma_\mu l_t)$	p	parameter shift $(G_F)$			
$Q_{lq}^{(1)}$	$(ar{l}_p \gamma^\mu l_r)(ar{q}_s \gamma_\mu q_t)$	X	X			
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma^\mu \tau^I l_r)(\bar{q}_s \gamma_\mu \tau^I q_t)$	<b>✓</b>	<b>✓</b>	<b>✓</b>		
$(ar{L} F_0)$	$(ar{L}R)(ar{R}L) +  ext{h.c.}$					
$Q_{ledq}$ $(\bar{l}_p^j e_r)(\bar{d}_s q_{tj})$		<b>✓</b>	X	<b>✓</b>		
$(ar{L}R)(ar{L}R) +  ext{h.c.}$						
$Q_{lequ}^{(1)} \qquad (\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$		<b>✓</b>	×	<b>✓</b>		
$Q_{lequ}^{(3)} \qquad (\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$		<b>✓</b>	X	✓		

• A consistent analysis of β-decays in SMEFT requires data from, Collider, Low energy, and ElectroWeak tests

Minimal set of operators involved \*\*

$$\mathcal{L} = \mathcal{L}_{\mathrm{SM}} + \sum_{i} C_{i} Q_{i}$$

	Operators		L	EW	C	
	$H^4D^2$					
$Q_{HD}$	$\left(H^{\dagger}D^{\mu}H\right)^{st}\left(H^{\dagger}D_{\mu}H\right)^{st}$	I)	parameter shift $(m_Z)$			
	$X^2H^2$					
$Q_{HWB}$	$H^{\dagger}  au^I H W^I_{\mu  u} B^{\mu  u}$		par	amete:	r shift $(\sin \theta_W)$	
	$\psi^2 H^2 D$					
$Q_{Hl}^{(1)}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{l}_{p}\gamma^{\mu}l_{r})$		X	<b>√</b>	✓	
$Q_{Hl}^{(3)}$	$\left  \begin{array}{c} (H^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}H)(\overline{l}_{p} au^{I}\gamma^{\mu}l_{r}) \end{array} \right $			<b>√</b>	✓	
$Q_{He}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{e}_{p}\gamma^{\mu}e_{r})$			<b>√</b>	✓	
$Q_{Hq}^{(1)}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{q}_{p}\gamma^{\mu}q_{r})$		X	<b>✓</b>	✓	
$Q_{Hq}^{(3)}$	$\left( H^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}H)(ar{q}_{p} au^{I}\gamma^{\mu}q_{p} ight) $	r)	<b>√</b>	<b>√</b>	✓	
$Q_{Hu}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{u}_{p}\gamma^{\mu}u_{r})$			<b>✓</b>	✓	
$Q_{Hd}$	$(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)(\bar{d}_{p}\gamma^{\mu}d_{r})$			<b>✓</b>	✓	
$Q_{Hud} + \text{h.c.}$	$   i(\widetilde{H}^{\dagger}D_{\mu}H)(\bar{u}_{p}\gamma^{\mu}d_{r}) $	$i(\widetilde{H}^{\dagger}D_{\mu}H)(\overline{u}_{p}\gamma^{\mu}d_{r})$			✓	

	Operators	$oxed{L}$	EW	$\mathbf{C}$		
	$(ar{L}L)(ar{L}L)$					
$Q_{ll}$	$(\overline{l}_p \gamma^\mu l_r)(\overline{l}_s \gamma_\mu l_t)$	p	parameter shift $(G_F)$			
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma^\mu l_r)(\bar{q}_s \gamma_\mu q_t)$	X				
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma^\mu \tau^I l_r)(\bar{q}_s \gamma_\mu \tau^I q_t)$	1	<b>✓</b>	<b>✓</b>		
$(ar{L}F$	$(ar{L}R)(ar{R}L)+ ext{h.c.}$					
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_{tj})$	1	X	<b>✓</b>		
$(ar{L}R)(ar{L}R) +  ext{h.c.}$						
$Q_{lequ}^{(1)} \qquad (\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$		1	X	<b>✓</b>		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	<b>/</b>	X	<b>✓</b>		

<sup>\*\*</sup> We are not including 'ld, lu, ed, eu, qe' 4-fermion operators that affect Drell-Yan (included in our analysis), NC processes at low-E & DIS (not included in our analysis). Inclusion of such operators would lead to a ~ closed set of observables  $\otimes$  operators. Do not expect big impact on the operators kept in our current analysis.

#### What about flavor?

- Most analyses impose flavor symmetry to reduce number of couplings (e.g. only 9 Wilson Coefficients in the CLEW analysis if assume U(3)<sup>5</sup>). However:
  - Lead to model-dependence (e.g. excludes classes of operators / models such as LRSM)
  - Results depend strongly on flavor assumptions

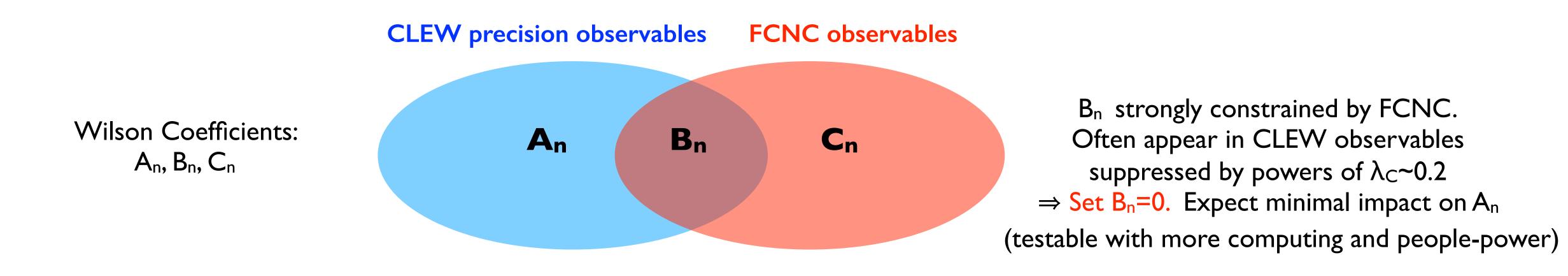
L. Bellafronte, S. Dawson, P. P. Giardino 2304.00029

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We perform a flavor-assumption-independent analysis: exploit approximate decoupling of CLEW and FCNC



$$\mathcal{L}_{tot} = \mathcal{L}_{CLEW}(A_n, B_n) \times \mathcal{L}_{FCNC}(B_n C_n) \times .... \rightarrow \mathcal{L}_{tot} = \mathcal{L}_{CLEW}(A_n, B_n=0) \times \mathcal{L}_{FCNC}(B_n C_n) \times ....$$

factorized likelihood

#### What about flavor?

# CLEW analysis with no assumption about flavor symmetry requires 37 couplings

	Global analysis	Indices (mass eigenstates)
	$\overline{C_{Hl}^{(1,3)}, C_{He}^{}_{pr}}$	$pr \in \{ee,  \mu\mu,  \tau\tau\}$
	$C_{Hq}^{(d)}, C_{Hd}^{}_{pr}$	$pr \in \{11, 22, 33\}$
		$pr \in \{11, 22\}$
	$C_{Hud} \atop pr$	$pr \in \{11, 12\}$
	$C_{egin{array}{c} lq \ \ell\ell pr \end{array}}^{(d)},  C_{egin{array}{c} ledq \ \ell\ell pr \end{array}}$	$\ell \in \{e, \mu\} ,  pr \in \{11, 22\}$
$\begin{pmatrix} 1 & \begin{pmatrix} 1 & 0 & 0 \end{pmatrix} & \begin{pmatrix} C_{} & 1 & C_{} & 1 & \begin{pmatrix} C_{} & 1 & C_{} & 1 & C_{} & C_{} & 1 \end{pmatrix} \end{pmatrix} \end{pmatrix}$		$\ell \in \{e, \mu\}$
	$C_{lq}^{lq},  C_{lequ}^{lequ} \ \ell\ell11  \ell\ell11 \ C_{ST}$	
	$C_{\substack{ll\2112}}$	

$$C_{Hq}^{(d)} = C_{Hq}^{(1)} + C_{Hq}^{(3)}$$

$$C_{Hq}^{(u)} = V \left[ C_{Hq}^{(1)} - C_{Hq}^{(3)} \right] V^{\dagger}$$

$$C_{lq}^{(d)} = C_{lq}^{(1)} + C_{lq}^{(3)}$$

$$C_{lq}^{(u)} = V \left[ C_{lq}^{(1)} - C_{lq}^{(3)} \right] V^{\dagger}$$

Large fits (e.g. with 37 Wilson Coefficients) not particularly enlightening

Not all operators matter for the fit!

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Not all operators matter for the fit!

Extreme example: CLEW37 fit with CDF input for mw

- Best fit W.C.'s are all consistent with zero at the  $2-\sigma$  level
- Analyze eigenvectors of the covariance matrix, their corresponding best fit values, and their (uncorrelated) variance  $\Rightarrow$  A handful of eigenvectors are non-zero at  $> 3-\sigma$  significance

$$0.51 C_{ST} + 0.33 C_{Hl}^{(3)} + 0.45 C_{ledq} - 0.40 \bar{C}_{lequ}^{(1)} - 0.34 C_{2112}^{ll} = -0.0016 \times (3.7 \pm 1) \,\text{TeV}^{-2}$$

$$0.41 C_{ST} - 0.47 C_{Hl}^{(3)} + 0.42 C_{2112}^{ll} = -0.0030 \times (6.5 \pm 1) \,\text{TeV}^{-2}$$

$$-0.83 C_{He} - 0.34 C_{Hl}^{(1)} - 0.31 C_{Hl}^{(3)} = 0.0093 \times (3 \pm 1) \,\text{TeV}^{-2}.$$

Large fits (e.g. with 37 Wilson Coefficients) not particularly enlightening

Not all operators matter for the fit!

To gain qualitative and quantitative insight on most relevant operators, use the Akaike Information Criterion

$$AIC = (\chi^2)_{min} + 2 k$$

# of estimated parameters

Minimization of AIC:

balance between goodness of fit (rewarded) and proliferation of parameters (penalized)

 Scanned model space by 'turning on' certain classes of effective couplings

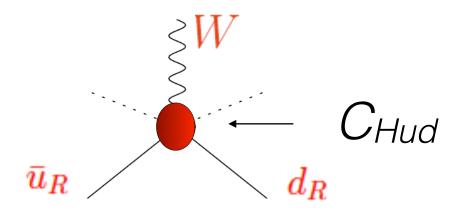
Operators grouped in 10 categories

Scanned this model space  $2^{10} = 1024$  'models'

Category	Operators	Description	# of Ops.
I.	$C_{ST}$	Oblique corrections	1
II.	$C_{Hud}$	RH charged currents	$oxed{2}$
III.	$C_{Hl}^{(1)}  C_{Hl}^{(3)}$	LH lepton vertices	6
IV.	$C_{He}$	RH lepton vertices	3
V.	$C_{Hq}^{(u)}$ $C_{Hq}^{(d)}$	LH quark vertices	5
VI.	$C_{Hu}$ $C_{Hd}$	RH quark vertices	5
VII.	$C_{ll}$	Lepton 4-fermion	1
VIII.	$egin{array}{ccc} C_{lq}^{(u)} & C_{lq}^{(d)} \end{array}$	Semileptonic 4-fermion	6
IX.	$oxed{C_{ledq}  C_{lequ}^{(1)}}$	Scalar 4-fermion	6
X.	$C_{lequ}^{(3)}$	Tensor 4-fermion	2

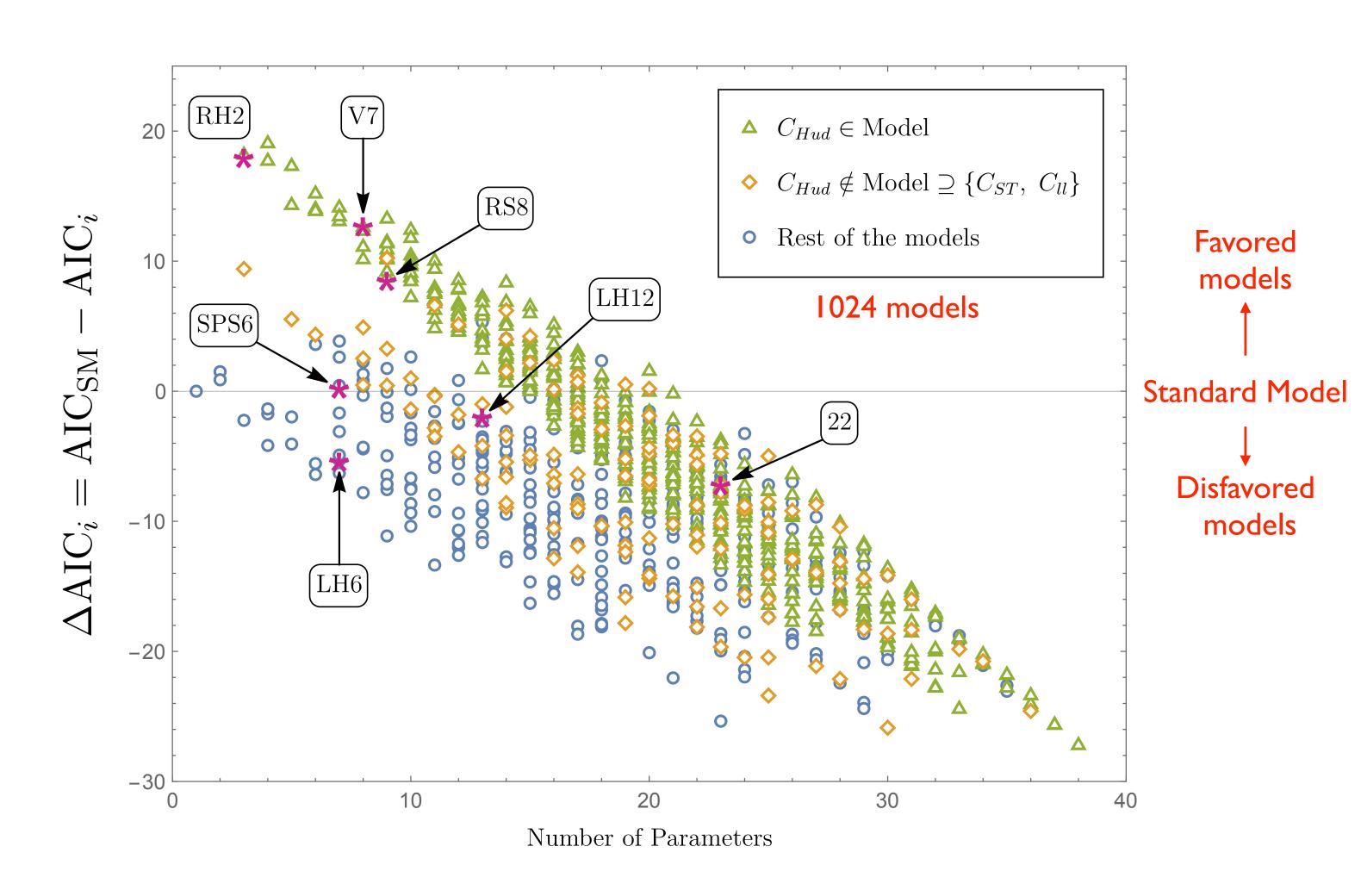
VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, JHEP 03 (24) 33, arXiv: 2311.00021

- Scanned model space by 'turning on' certain classes of effective couplings
- Akaike Information Criterion favors models with Right-Handed Charged Currents of quarks



Models with oblique corrections (C<sub>ST</sub>)
 also fare better than SM





VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, JHEP 03 (24) 33, arXiv: 2311.00021

- Scanned model space by 'turning on' certain classes of effective couplings
- Akaike Information Criterion favors models with Right-Handed Charged Currents of quarks

- $\triangle$   $C_{Hud} \in Model$
- $\diamond$   $C_{Hud} \notin \text{Model} \supseteq \{C_{ST}, C_{ll}\}$
- Rest of the models

1024 models

The winner (ΔAIC=19): two RH CC vertex corrections and a combination of oblique parameters

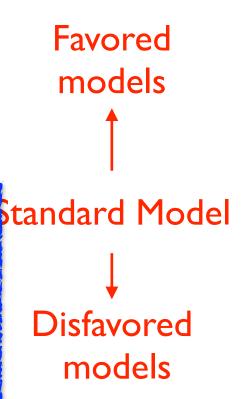
Model
Model

quarks generate RH CC at tree level
also fa
and oblique at I-loop)

$$C_{Hud} = (-0.030 \pm 0.008) \,\text{TeV}^{-2}$$

$$C_{Hud} = (-0.040 \pm 0.011) \,\text{TeV}^{-2}$$

$$C_{ST} = (-0.0038 \pm 0.0022) \,\text{TeV}^{-2}$$



VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, JHEP 03 (24) 33, arXiv: 2311.00021

**Favored** 

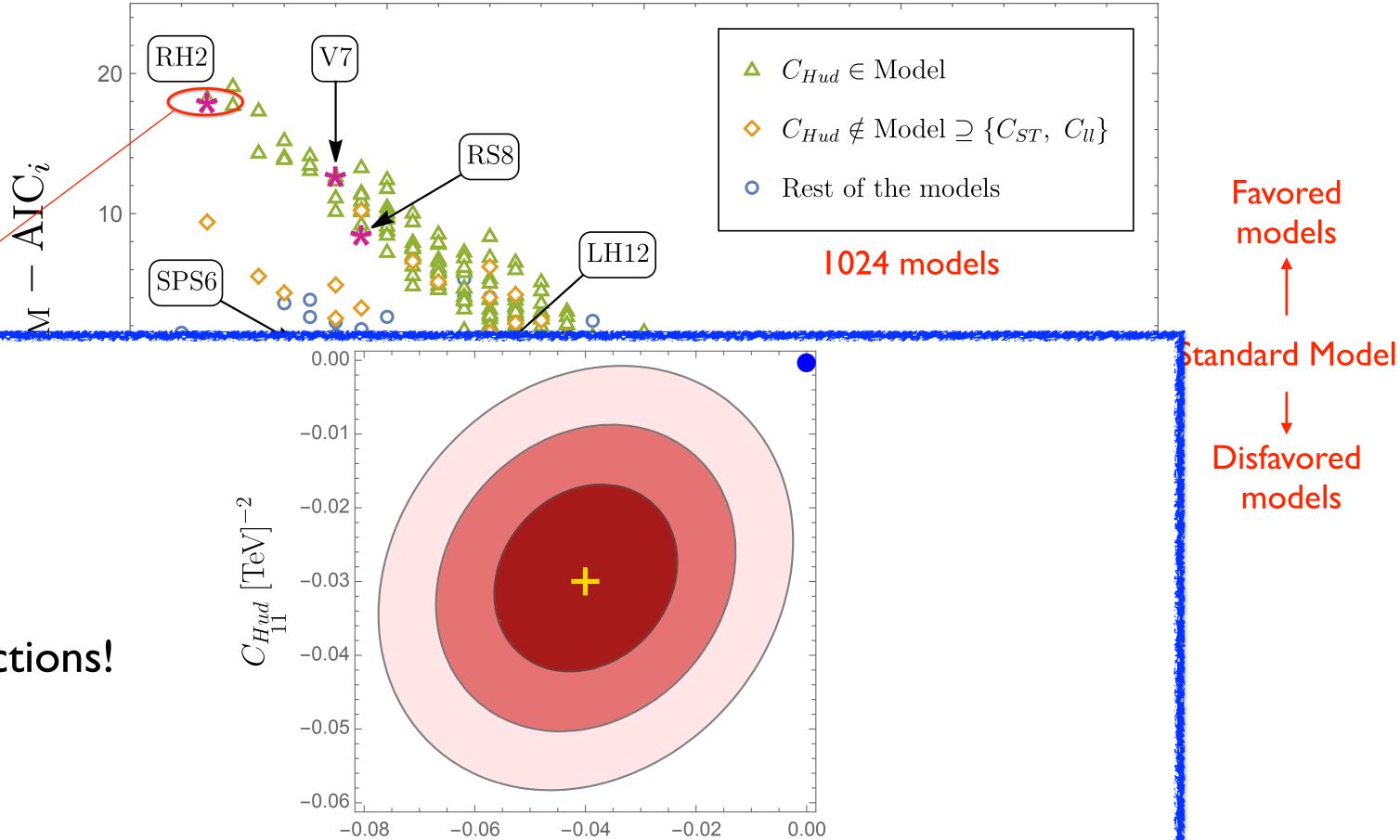
models

Disfavored

models

- Scanned model space by 'turning on' certain classes of effective couplings
- Akaike Information Criterion favors models with Right-Handed Charged Currents of quarks

The runner-up ( $\triangle$ AIC=18): just two RH CC vertex corrections!



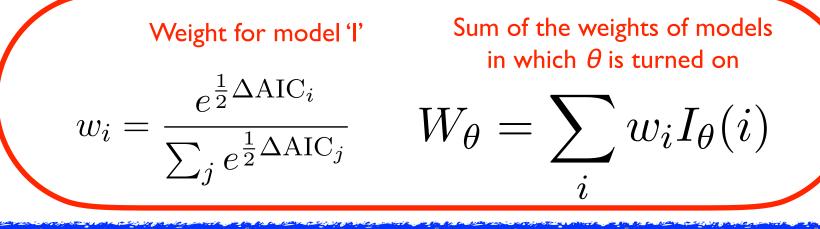
 $C_{Hud} [\text{TeV}]^{-2}$ 

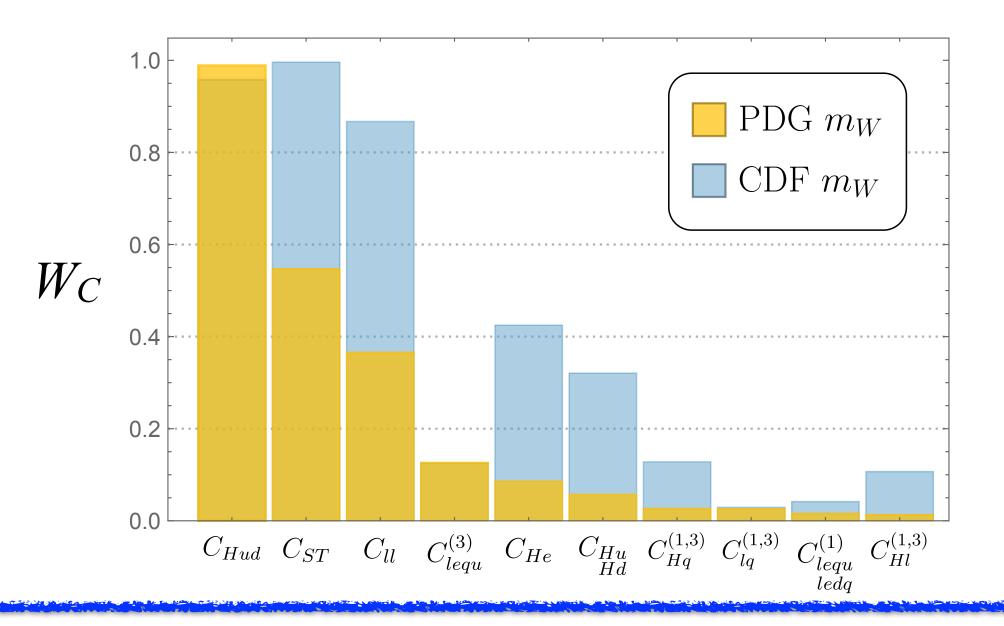
Model also fa

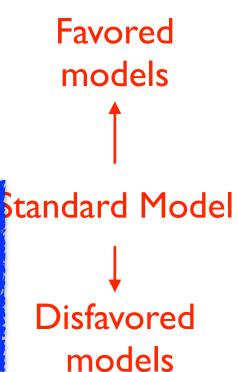
VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, JHEP 03 (24) 33, arXiv: 2311.00021

- Scanned model space by 'turning on' certain classes of effective couplings
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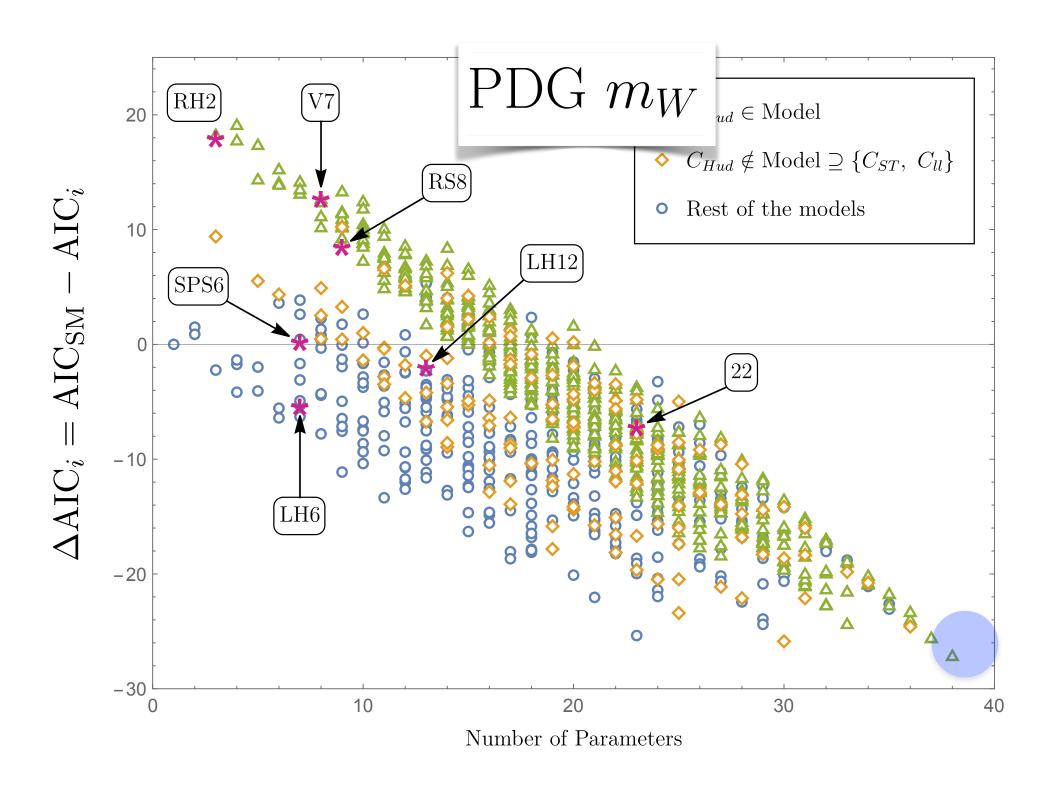
- Most important operators: R-handed CC, oblique corrections, 4-lepton
- R-handed neutral currents ( $C_{He}$ ,  $C_{Hd}$ ) appear in 'next best models': mitigate some Z-pole tensions
- Model also fa

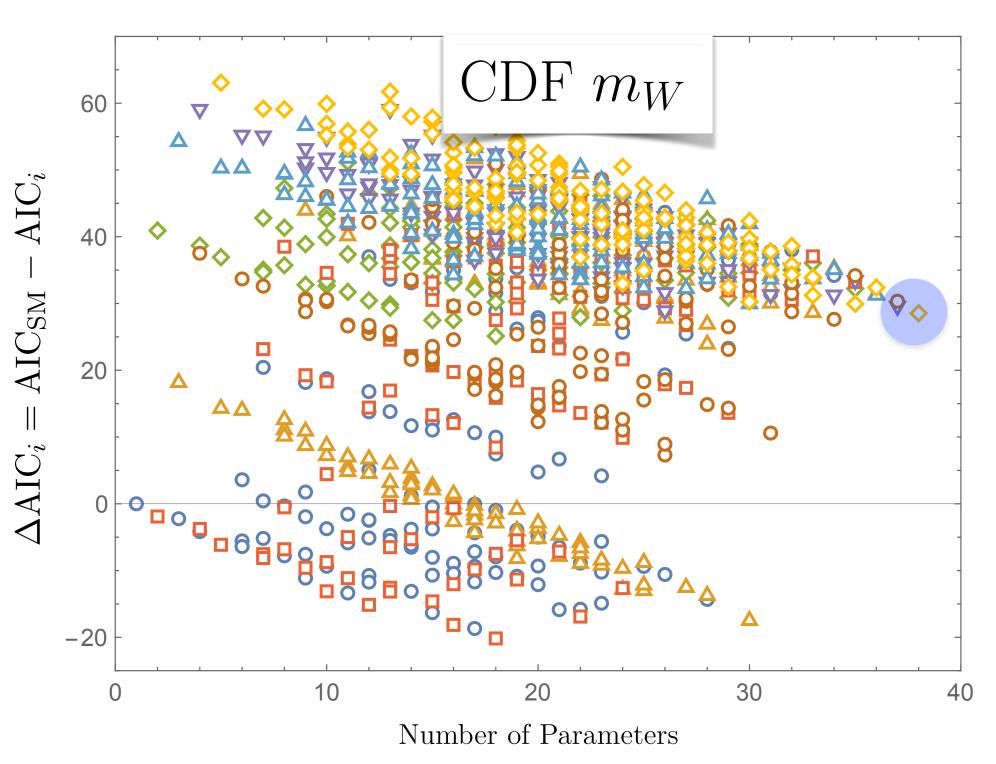






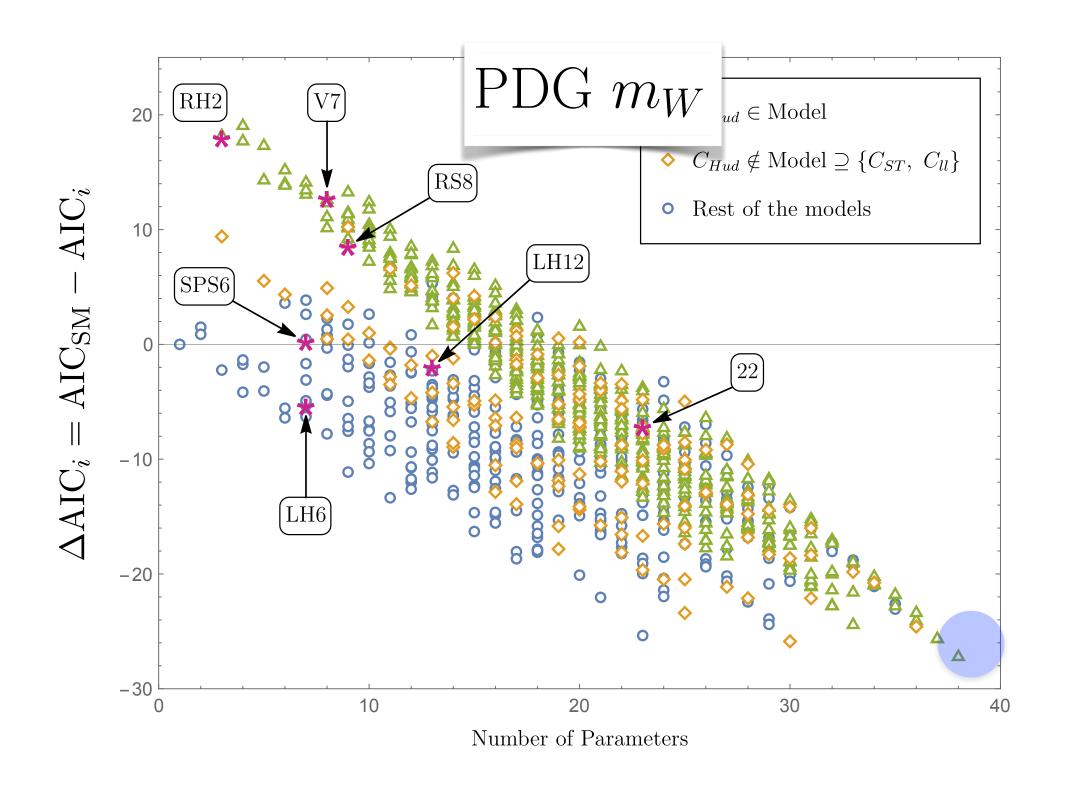
• Qualitatively similar\*\* conclusions if one includes the CDF mw measurement

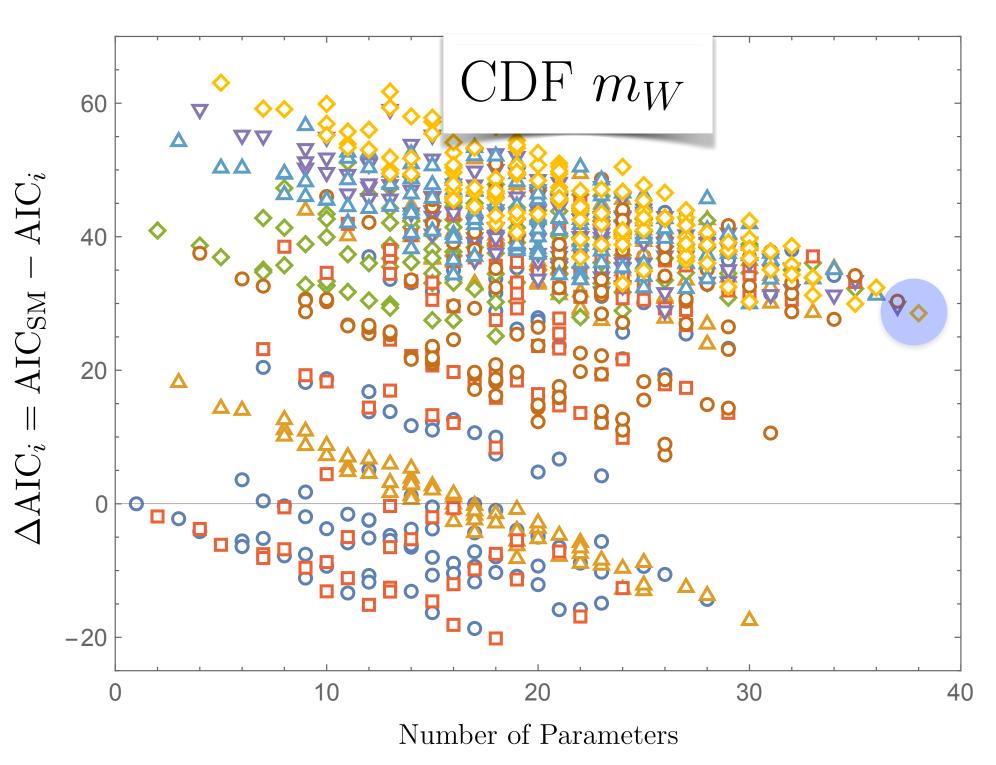




- $\diamond$  Model  $\supseteq \{C_{Hud}, C_{ST}, C_{ll}\}$
- $\triangle$   $C_{Hud} \notin \text{Model} \supseteq \{C_{ST}, C_{ll}\}$
- $\circ$   $C_{ST} \notin \text{Model} \supseteq \{C_{Hud}, C_{ll}\}$
- $abla C_{ll} \notin \text{Model} \supseteq \{C_{Hud}, C_{ST}\}$
- $\square \{C_{Hud}, C_{ST}\} \notin \text{Model} \ni C_{ll}$
- $C_{Hud}, \ C_{ll} \} \notin \text{Model} \ni C_{ST}$
- $\triangle$   $\{C_{ST}, C_{ll}\} \notin \text{Model} \ni C_{Hud}$
- Rest of the models

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- $\diamond$  Model  $\supseteq \{C_{Hud}, C_{ST}, C_{ll}\}$
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- $\triangle$   $\{C_{ST}, C_{ll}\} \notin \text{Model} \ni C_{Hud}$
- Rest of the models

CKM "anomaly" not ruled out by other data!

Unitarity test provides relevant input to unravel possible new physics.

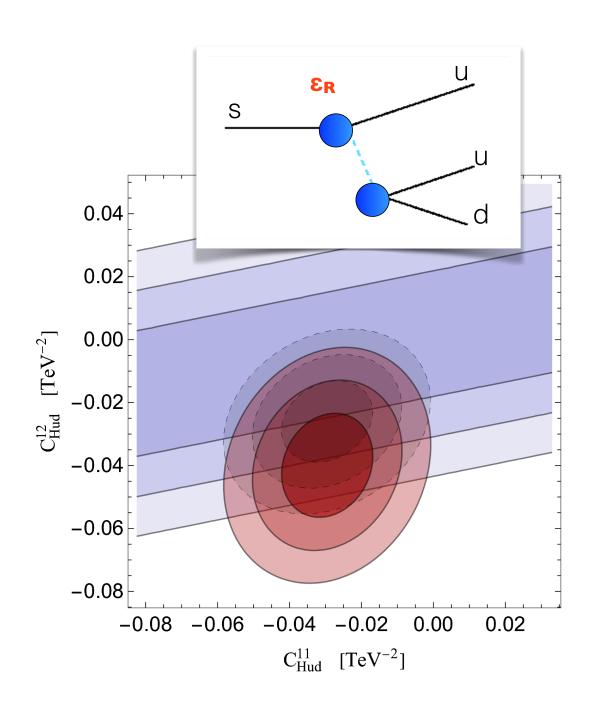
# Falsifying R-handed current hypothesis

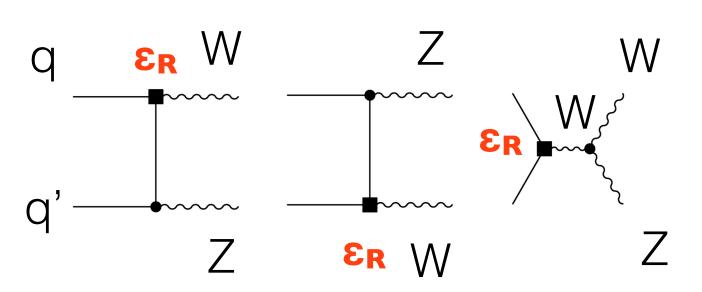
VC, W. Dekens, J. De Vries, E. Mereghetti, T. Tong, 2311.00021

- Currently less-sensitive probes of R-handed couplings
  - $g_A/g_V$ : neutron decay vs Lattice QCD (need ~ order of magnitude theoretical improvement)

•  $K \rightarrow (\Pi\Pi)_{l=2}$  decay amplitude: experiment vs Lattice QCD (difficult to improve)

 WH & WZ production at the High Luminosity LHC will reach sensitivity need to test the R-handed current solution to the Cabibbo angle anomaly



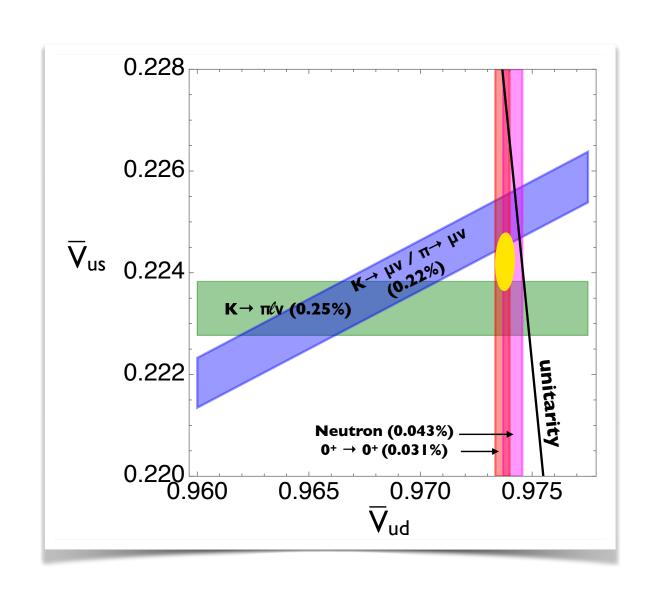


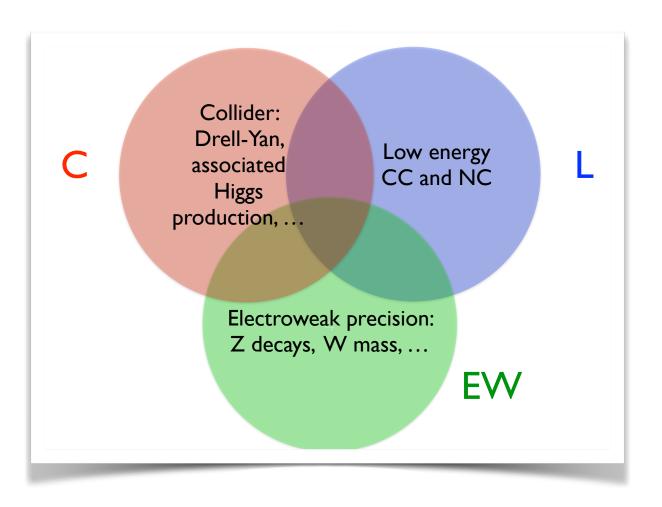
#### Summary and outlook

• The Cabibbo angle anomaly is one of few low-energy "cracks" in the SM, probing new physics up to  $\Lambda \sim 20\,\text{TeV}$  — big deal if confirmed, requires both experimental and theoretical scrutiny

Simplest BSM explanations of Cabibbo anomaly given by "right-handed vertex corrections" in the SMEFT language

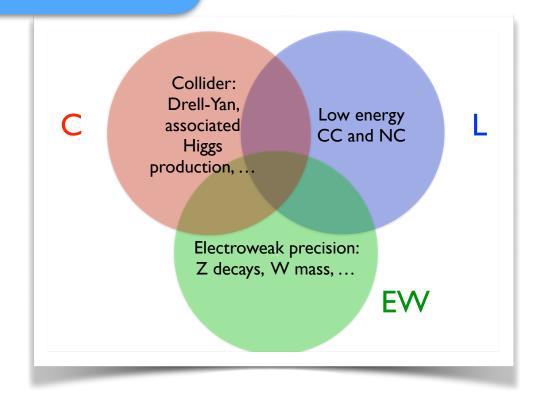
• CLEW framework is necessary for consistent analysis and RH CC 'explanation' of the Cabibbo anomaly survives CLEWed analysis





### Summary and outlook

• The traditional set of EWPO considered in the literature should be extended (both in the U(3)<sup>5</sup> and general flavor case) to include at least low-energy CC processes & Drell-Yan: they constrain subset of couplings at similar precision!



- Flavor symmetry assumptions reintroduce model-dependence in the SMEFT approach. Flavor symmetries can make the analysis 'blind' to simple BSM scenarios (e.g. U(3)<sup>5</sup> and RH currents). We argued that likelihood can be approximately factorized.
- A SMEFT-based 'model selection' analysis (with AIC or other metric) can be quite insightful and ultimately should help unraveling the underlying new physics if anomalies arise / survive

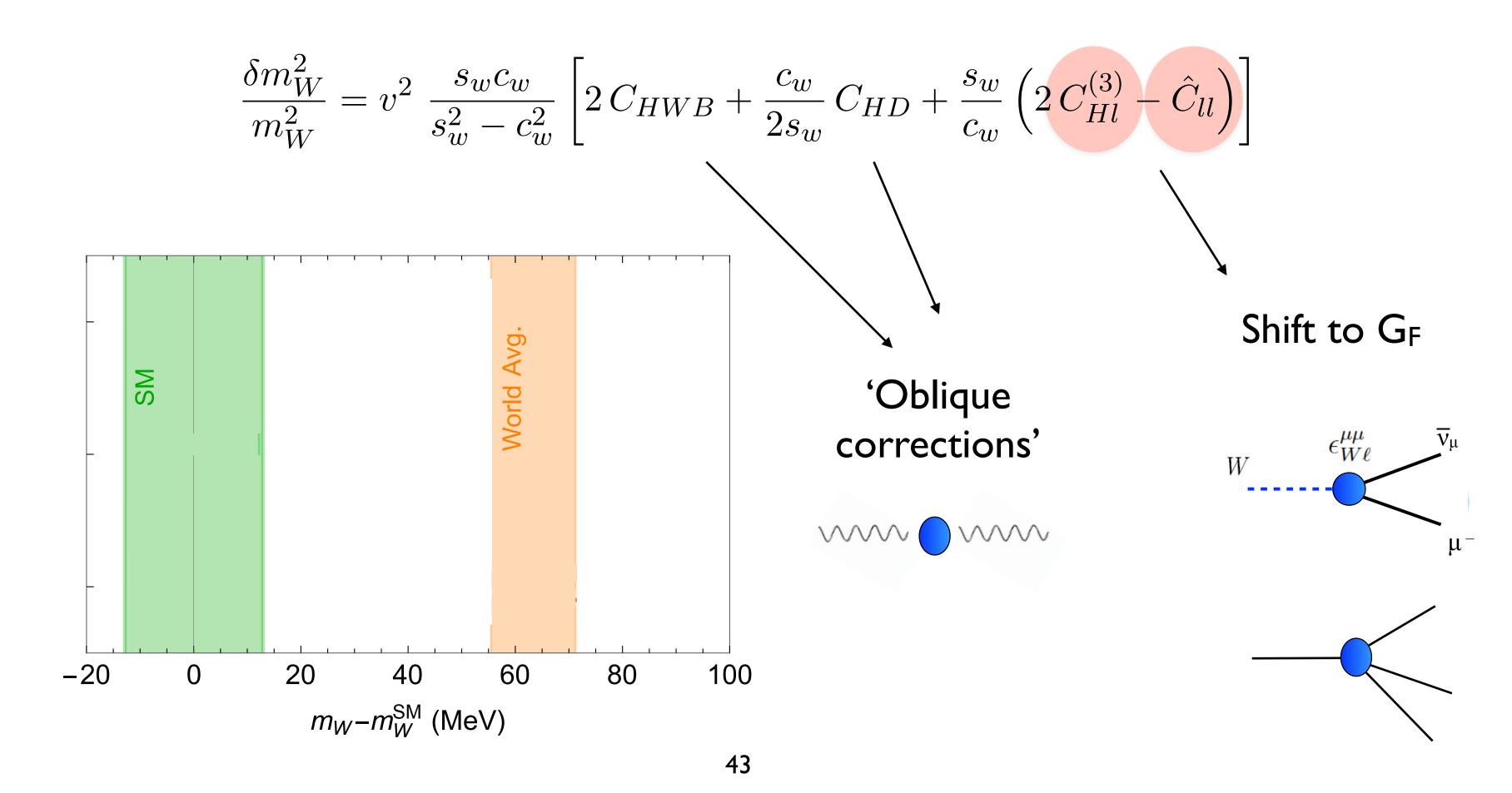
- Towards a complete (tree-level) SMEFT analysis of precision observables that do not involve FCNC and CPV:
  - Observables that currently have weaker sensitivity: K decays; HW, ZW production at the LHC
  - NC processes: PVES, APV, DIS (→ EIC)

# Backup

# $\Delta_{\text{CKM}}$ and EW precision fits (I)

VC, Dekens, deVries, Mereghetti, Tong 2204.08440, 2311.00021

- Cabibbo universality test quantitatively and qualitatively affects global fits to precision EW observables
- Example: explanations of mw 'anomaly' in SMEFT + U(3)<sup>5</sup>

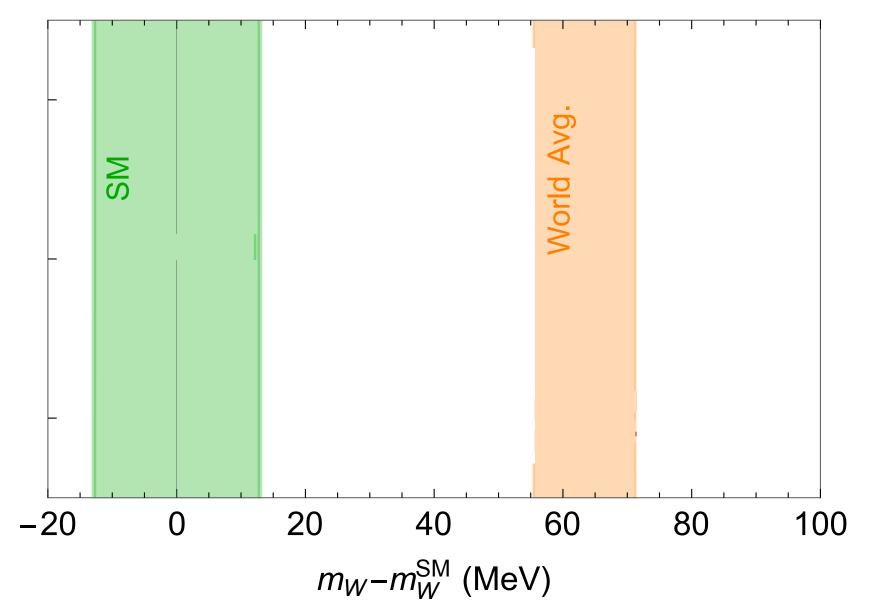


# Δckm and EW precision fits (I)

VC, Dekens, deVries, Mereghetti, Tong 2204.08440, 2311.00021

- Cabibbo universality test quantitatively and qualitatively affects global fits to precision EW observables
- Example: explanations of mw 'anomaly' in SMEFT + U(3)<sup>5</sup>

$$\frac{\delta m_W^2}{m_W^2} = v^2 \frac{s_w c_w}{s_w^2 - c_w^2} \left[ 2C_{HWB} + \frac{c_w}{2s_w} C_{HD} + \frac{s_w}{c_w} \left( 2C_{Hl}^{(3)} - \hat{C}_{ll} \right) \right]$$



$$\Delta_{\text{CKM}} = v^2 \left[ C_{\Delta} - 2 C_{lq}^{(3)} \right]$$

$$C_{\Delta} = 2 \left[ C_{Hq}^{(3)} - C_{Hl}^{(3)} + \hat{C}_{ll} \right]$$

$$Q_{\perp}$$

$$W$$

$$Q_{\perp}$$

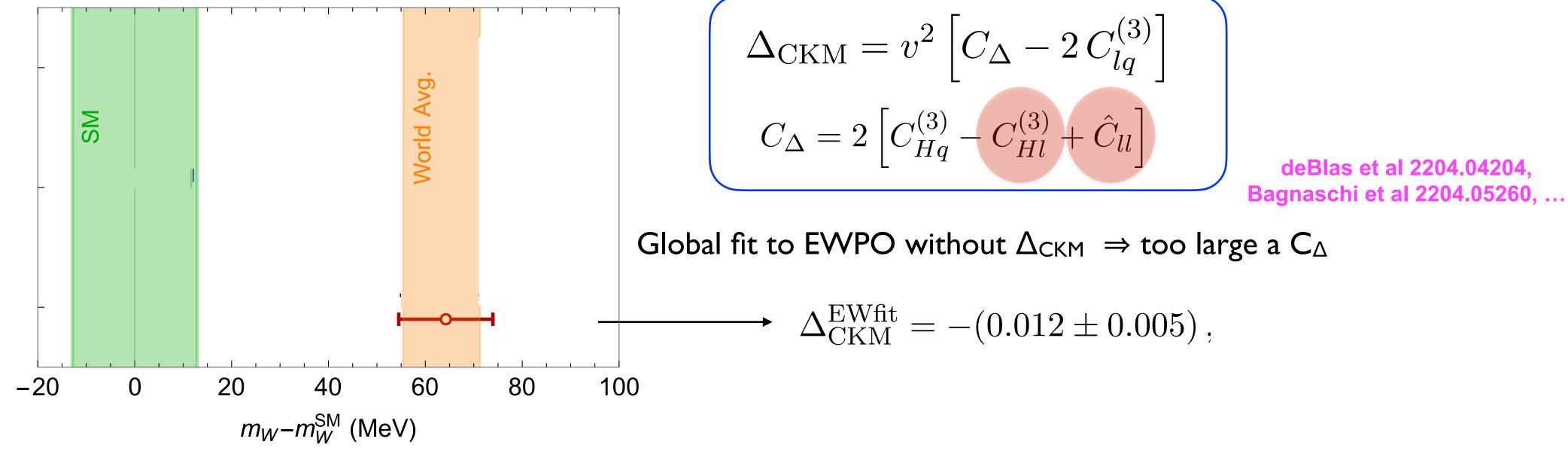
$$Q_{\perp}$$

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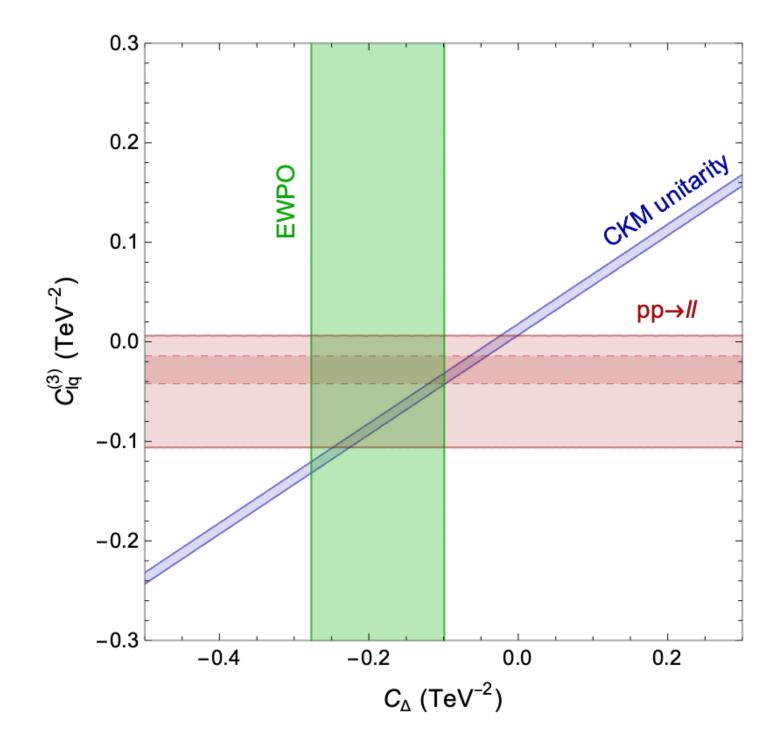


# Δckm and EW precision fits (2)

VC, Dekens, deVries, Mereghetti, Tong 2204.08440, 2311.00021

- Cabibbo universality test quantitatively and qualitatively affects global fits to precision EW observables
- Example: explanations of mw anomaly in SMEFT + U(3)<sup>5</sup>

$$\frac{\delta m_W^2}{m_W^2} = v^2 \frac{s_w c_w}{s_w^2 - c_w^2} \left[ 2 C_{HWB} + \frac{c_w}{2s_w} C_{HD} + \frac{s_w}{c_w} \left( 2 C_{Hl}^{(3)} - \hat{C}_{ll} \right) \right]$$



$$\Delta_{\text{CKM}} = v^2 \left[ C_{\Delta} - 2 C_{lq}^{(3)} \right]$$

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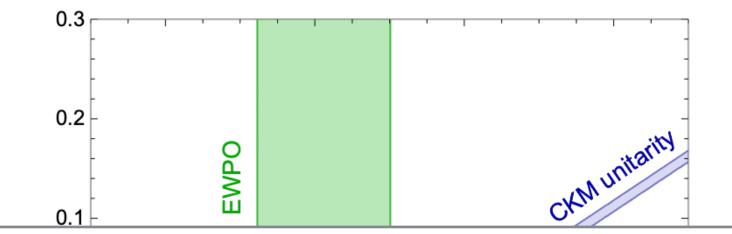
• Include  $\Delta_{CKM}$  & decouple from  $m_W$  by turning on  $C_{lq}^{(3)}$ : but constraints from Drell-Yan at the LHC can't be ignored!

# Δckm and EW precision fits (2)

VC, Dekens, deVries, Mereghetti, Tong 2204.08440, 2311.00021

- Cabibbo universality test quantitatively and qualitatively affects global fits to precision EW observables
- Example: explanations of mw anomaly in SMEFT + U(3)<sup>5</sup>

$$\frac{\delta m_W^2}{m_W^2} = v^2 \frac{s_w c_w}{s_w^2 - c_w^2} \left[ 2C_{HWB} + \frac{c_w}{2s_w} C_{HD} + \frac{s_w}{c_w} \left( 2C_{Hl}^{(3)} - \hat{C}_{ll} \right) \right]$$



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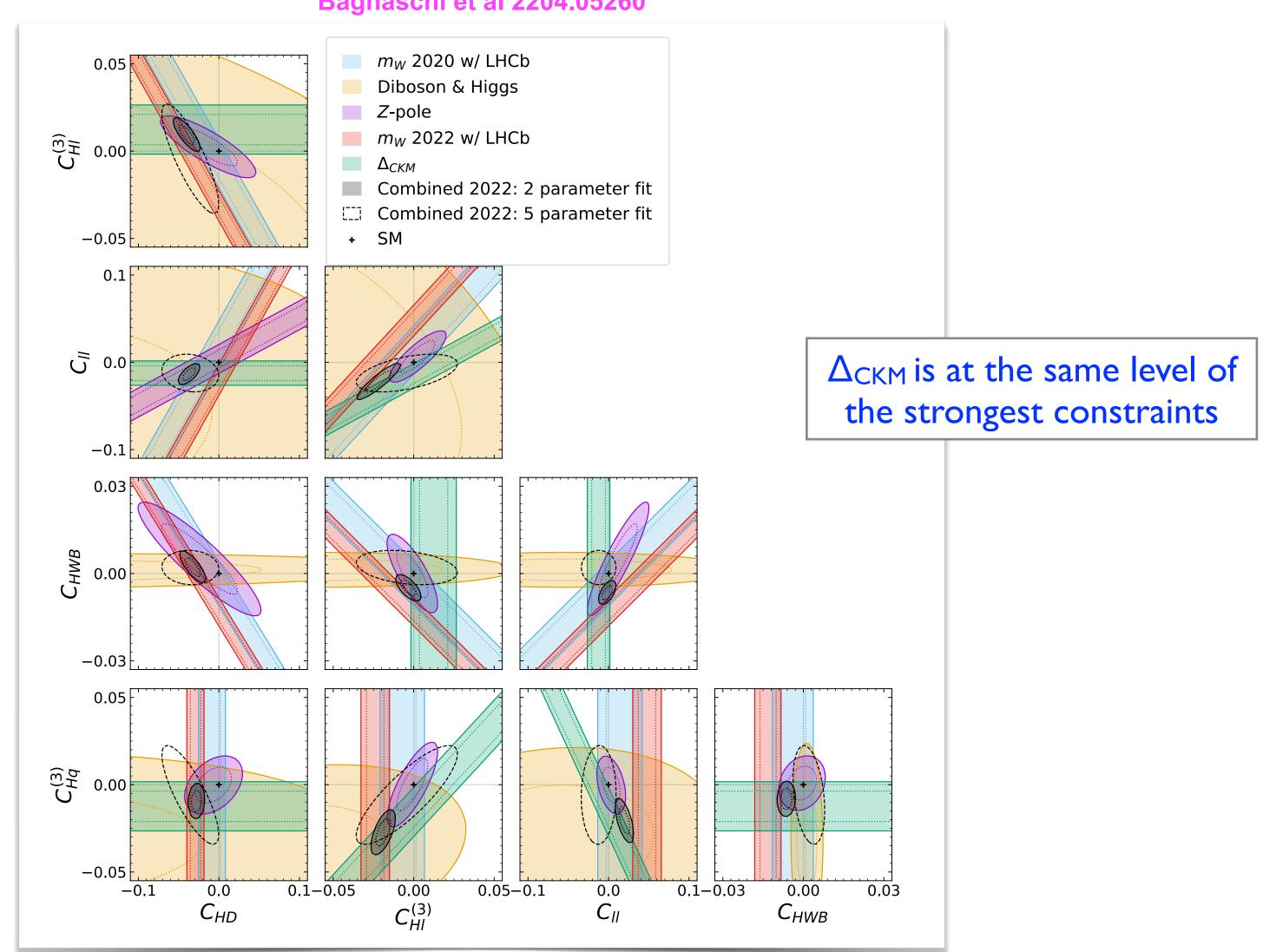
Quantitative point: best fit values for effective couplings with or without  $\Delta_{\mathsf{CKM}}$  change

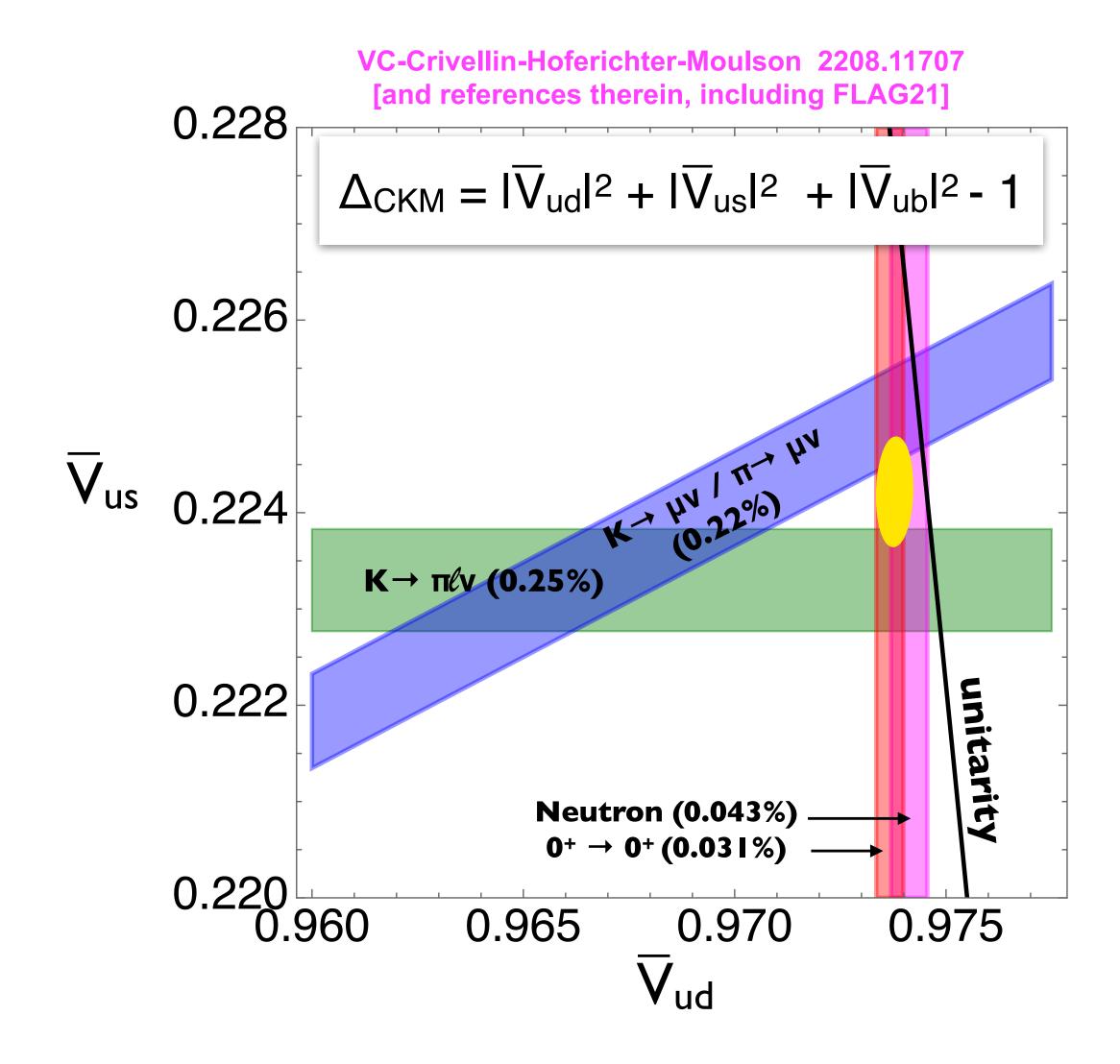
Qualitative point: global analyses of 'electroweak precision observables' should be extended to include low-energy (such as  $\Delta_{CKM}$ ) and collider (such as Drell-Yan) observables

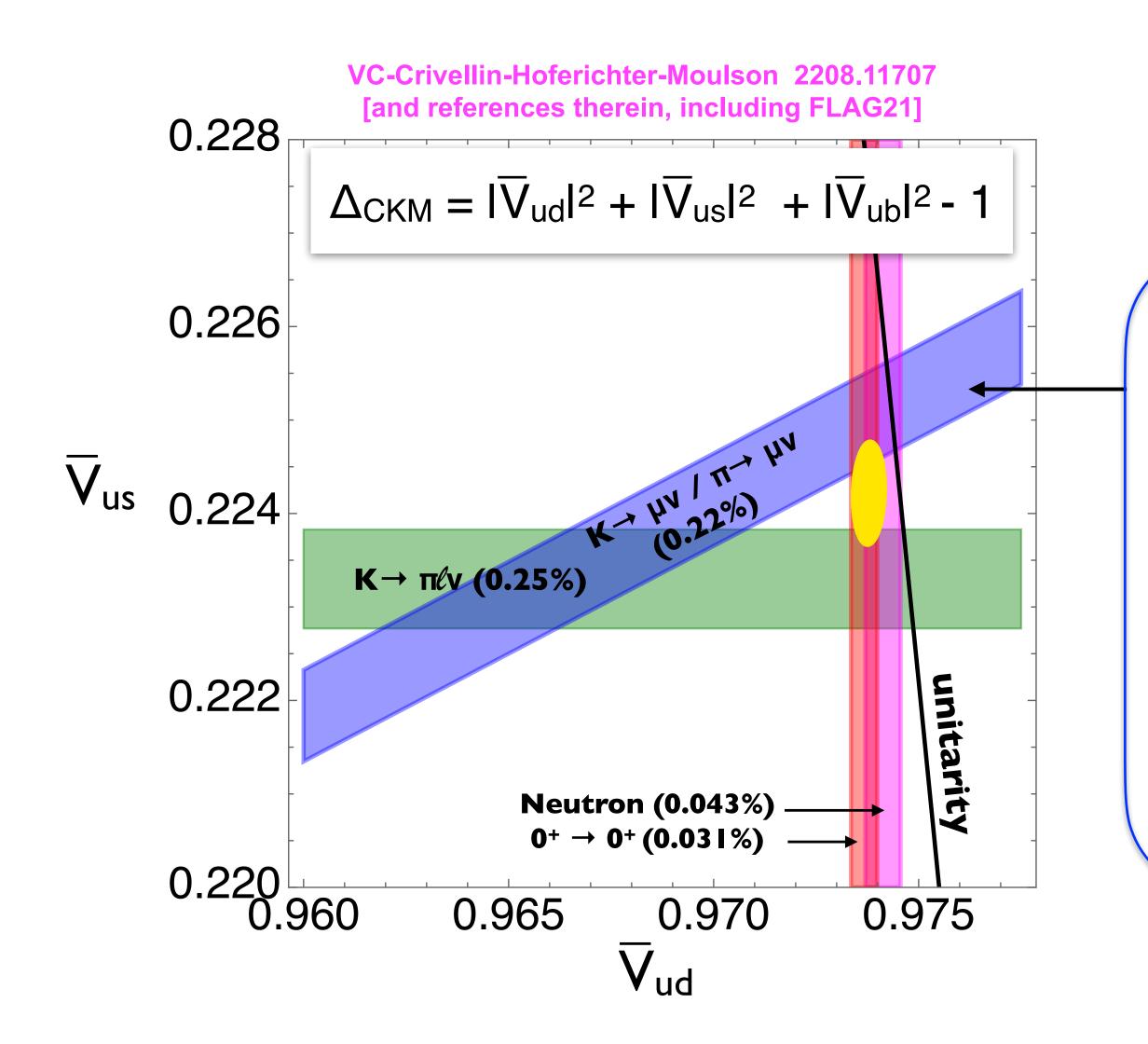
$$-0.3$$
  $-0.4$   $-0.2$   $0.0$   $0.2$   $C_{\Delta}$  (TeV<sup>-2</sup>)

# $\Delta_{\text{CKM}}$ and EW precision fits (3)

#### **Bagnaschi et al 2204.05260**

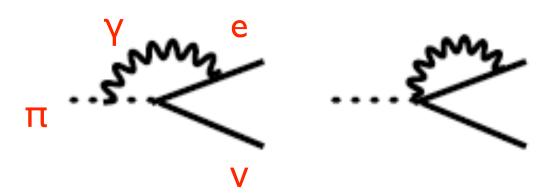






Ratio of decay constants s from Lattice QCD

QED + strong isospin-breaking: Lattice QCD and ChPT

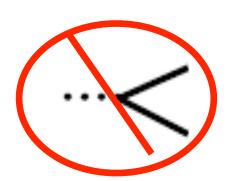


ChPT: VC-Neufeld, I 102.0563

LQCD:

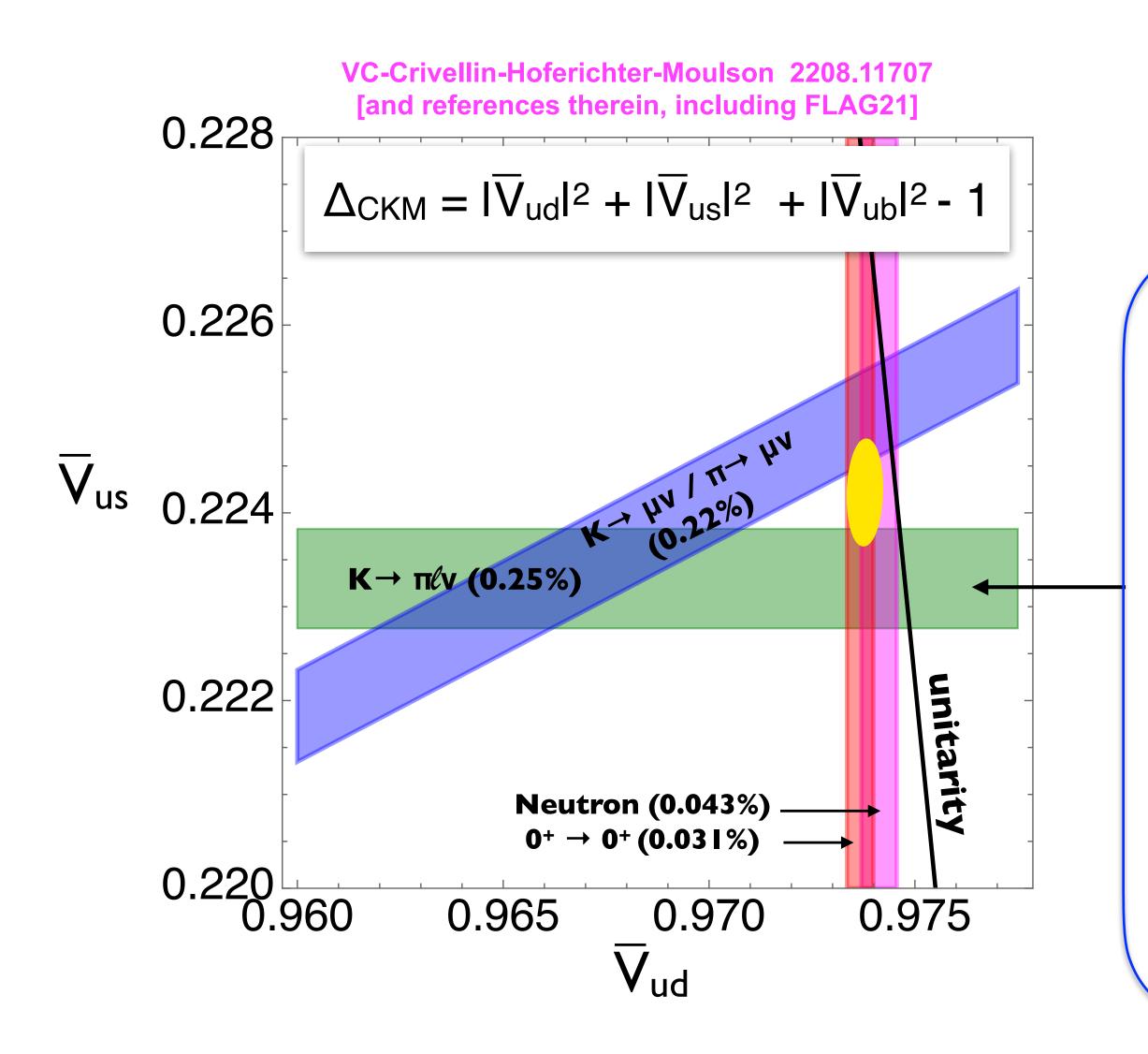
FLAG: 2111.09849 Di Carlo et al., 1904.08731

Boyle et al., 2211.12865



No contact (LEC): contribution cancels

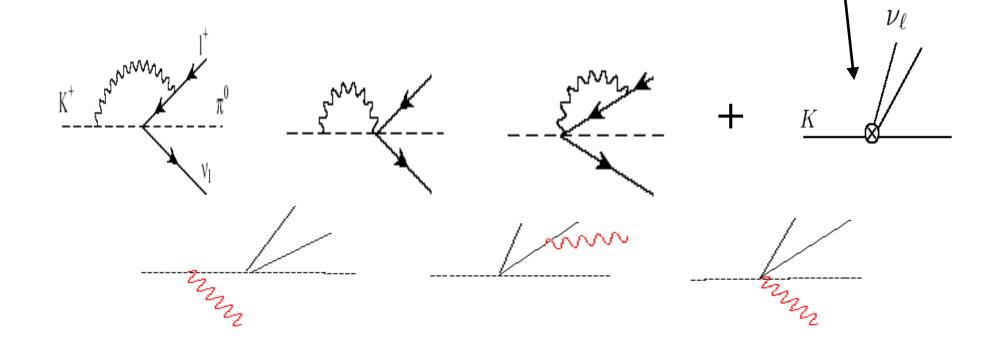
in the ratio!



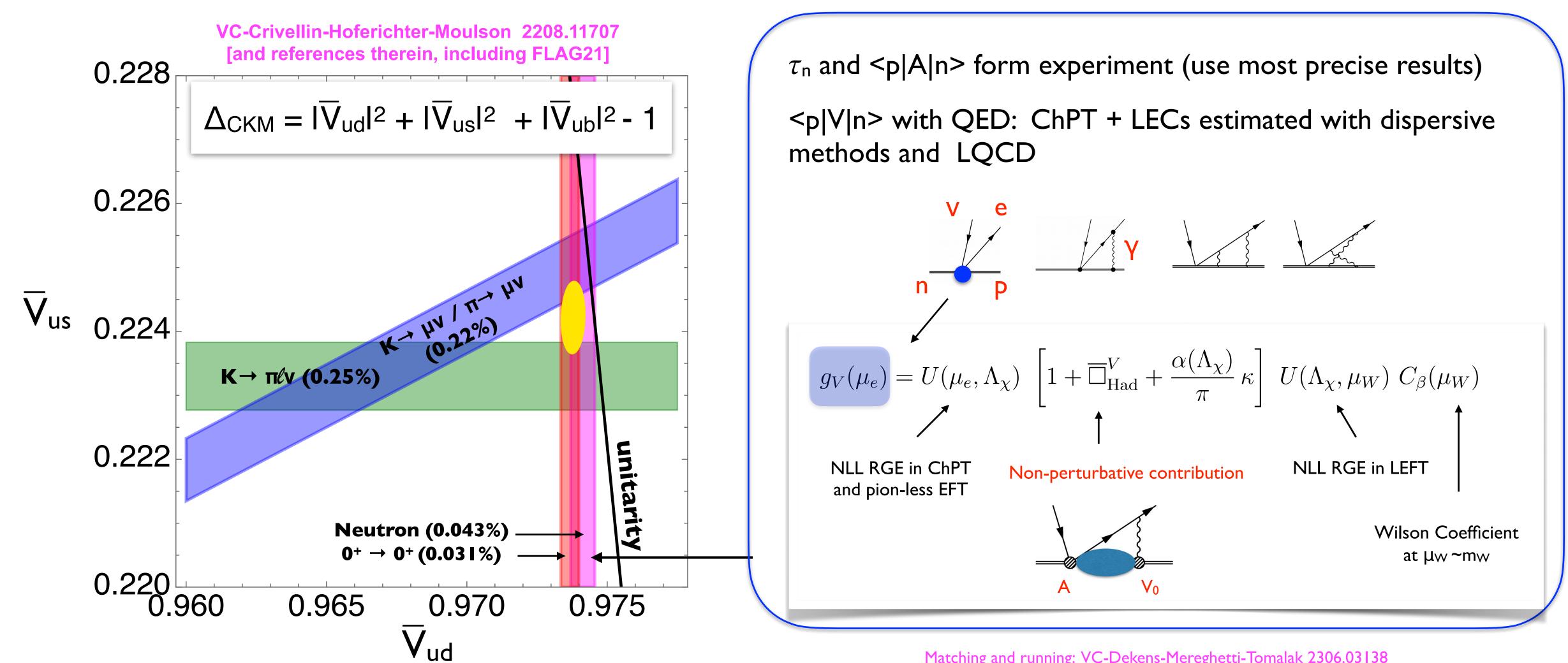
 $<\pi |V|K>$  form factor from Lattice QCD FLAG: 2111.09849

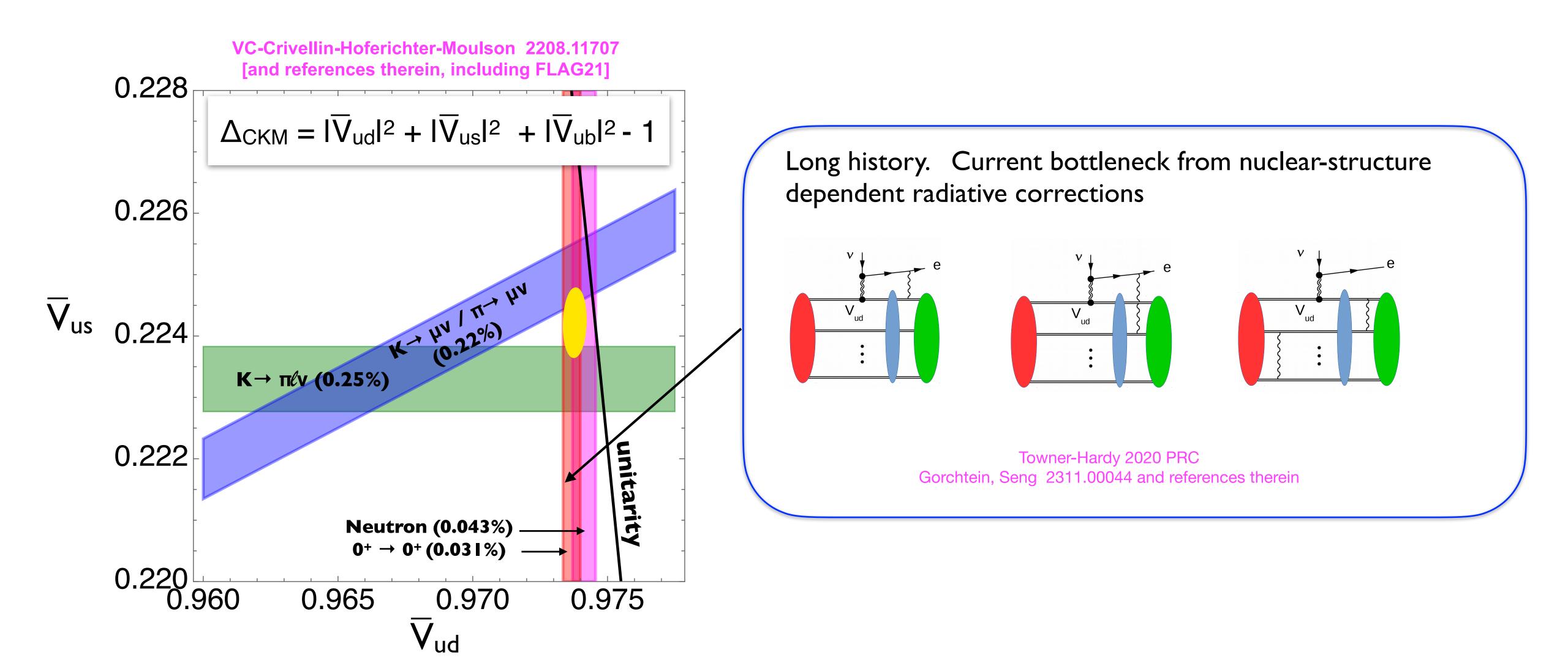
QED + strong isospin-breaking: ChPT + LECs estimated with

dispersive methods and LQCD



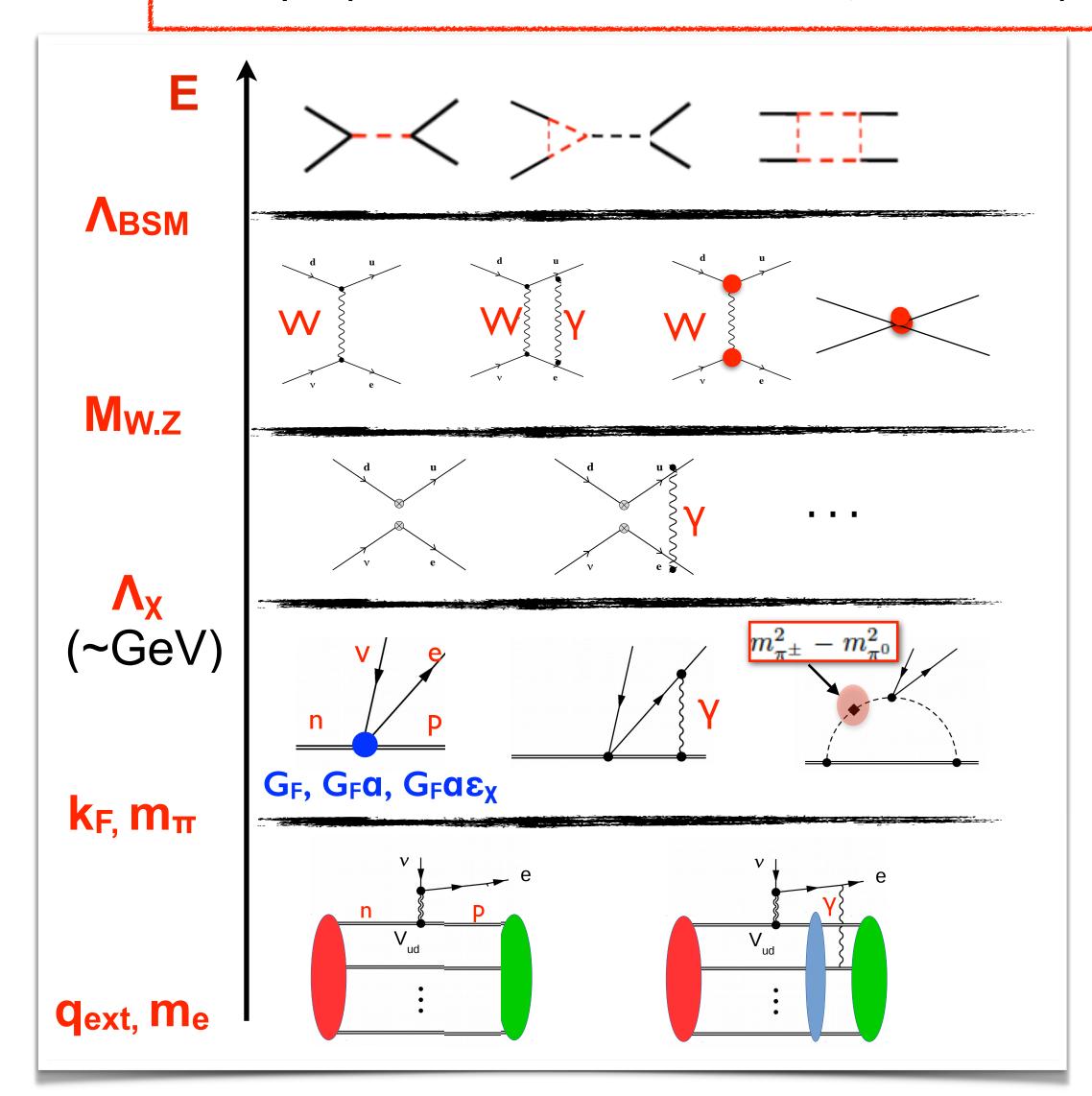
VC, Giannotti, Neufeld 0807.4607 Seng et al, 1910.13209, 2103.00975. 2103.4843. 2107.14708. 2203.05217. Ma et al. 2102.12048





Widely separated scales:  $\Lambda_{BSM}$ ,  $M_W$ ,  $\Lambda_X$ ,  $m_\pi$ ,  $m_e \sim q_{ext}$ 

⇒ Tackle the problem through a tower of EFTs



#### One nucleon

VC, J. de Vries, L. Hayen, E. Mereghetti, A. Walker-Loud 2202.10439, PRL VC, W. Dekens, E. Mereghetti, O. Tomalak, 2306.03138, PRD

#### Multi nucleons

VC, W. Dekens,, J.de Vries, S. Gandolfi, M. Hoferichter, E, Mereghetti, 2405.18469 & 2405.18464

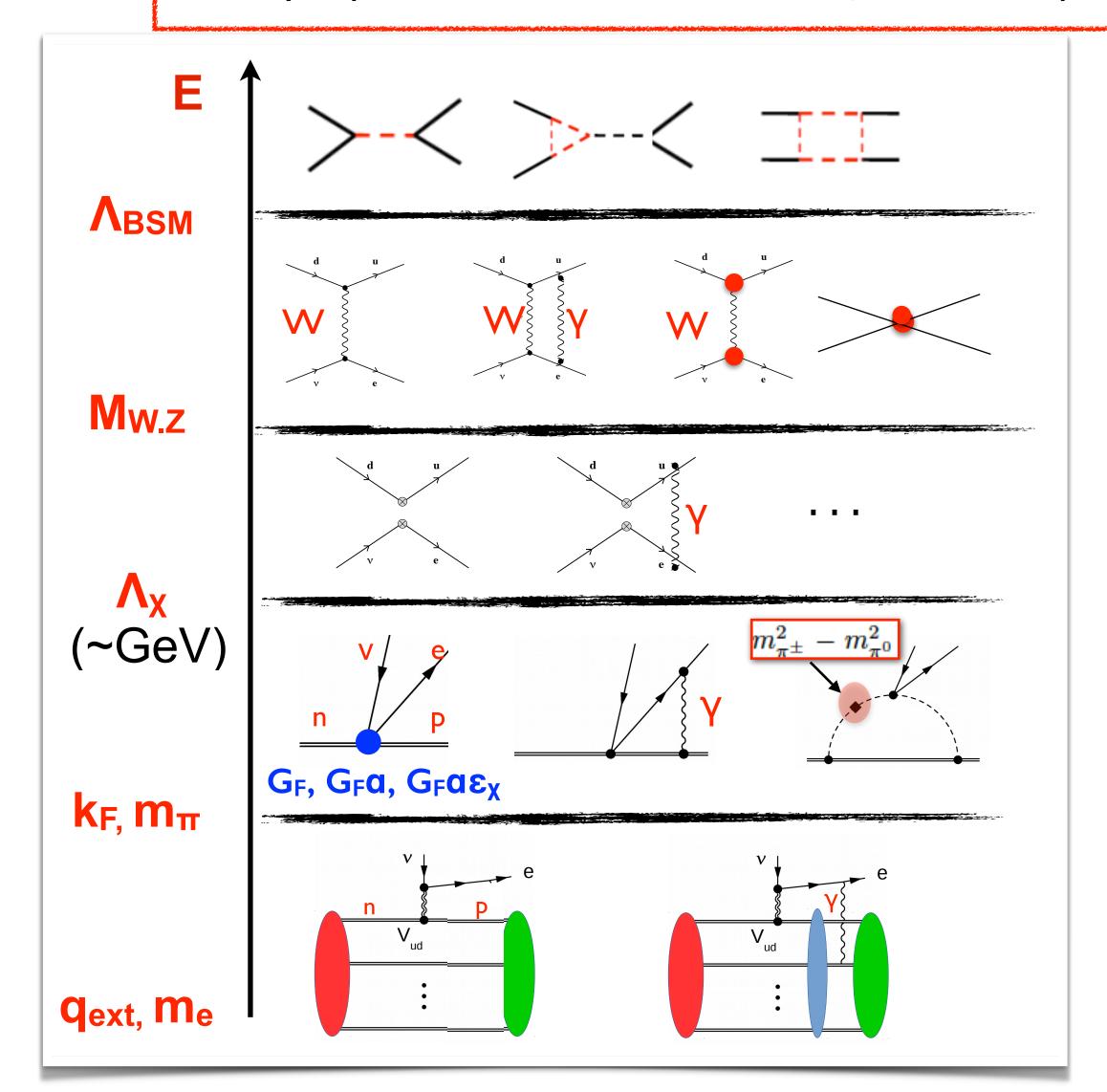
#### Point-like nucleus

K. Borah, R. Hill, R. Plestid, 2309.07343, 2309.15929, 2402.13307

Widely separated scales:  $\Lambda_{BSM}$ ,  $M_W$ ,  $\Lambda_{\chi}$ ,  $m_{\pi}$ ,  $m_e \sim q_{ext}$ Tackle the problem through a tower of EFTs  $\Rightarrow$ **BSM** Perturbative matching **\ABSM Standard Model Effective Field Theory** W  $\varepsilon_{\text{SMEFT}} = (M_{\text{W}}/\Lambda_{\text{BSM}})^2$ M<sub>W.Z</sub> Perturbative matching **LEFT: Fermi Theory + QCD + QED**  $\varepsilon_{W} = (\Lambda_{X}/M_{W})^{2}$ . . . Non-perturbative matching: Lattice QCD,  $\Lambda_{X}$ dispersion relations, data, ... (~GeV)  $\epsilon_{\chi} = \{k_F, m_{\pi,K}\}/\Lambda_{\chi}$ **Chiral Perturbation Theory**  $G_F$ ,  $G_F\alpha$ ,  $G_F\alpha \epsilon_{\chi}$  $k_{F_1} m_{\pi}$ Integrate out pions  $\epsilon_{\!\scriptscriptstyle M} = q_{
m ext}/m_\pi$ **Chiral & pion-less EFT**  $\epsilon_{
m recoil} = q_{
m ext}/\Lambda_{
m g}$ q<sub>ext</sub>, m<sub>e</sub> The EFT expands amplitudes in  $\varepsilon$ 's and re-sums large logarithms  $\sim \alpha^{n+m} (\ln(\varepsilon))^n$ 

Widely separated scales:  $\Lambda_{BSM}$ ,  $M_W$ ,  $\Lambda_X$ ,  $m_{\pi}$ ,  $m_e \sim q_{ext}$ 

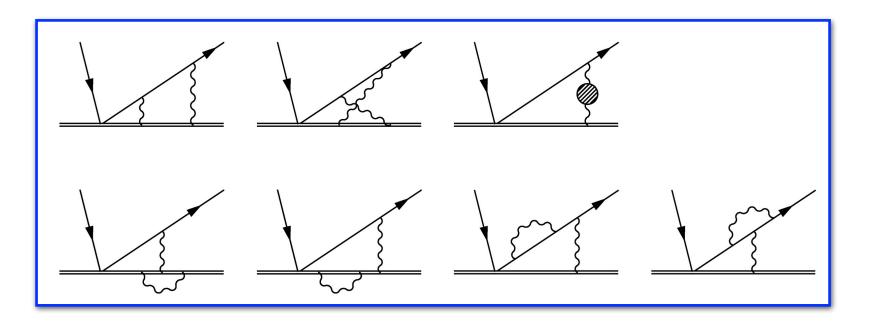
⇒ Tackle the problem through a tower of EFTs



#### Single nucleon

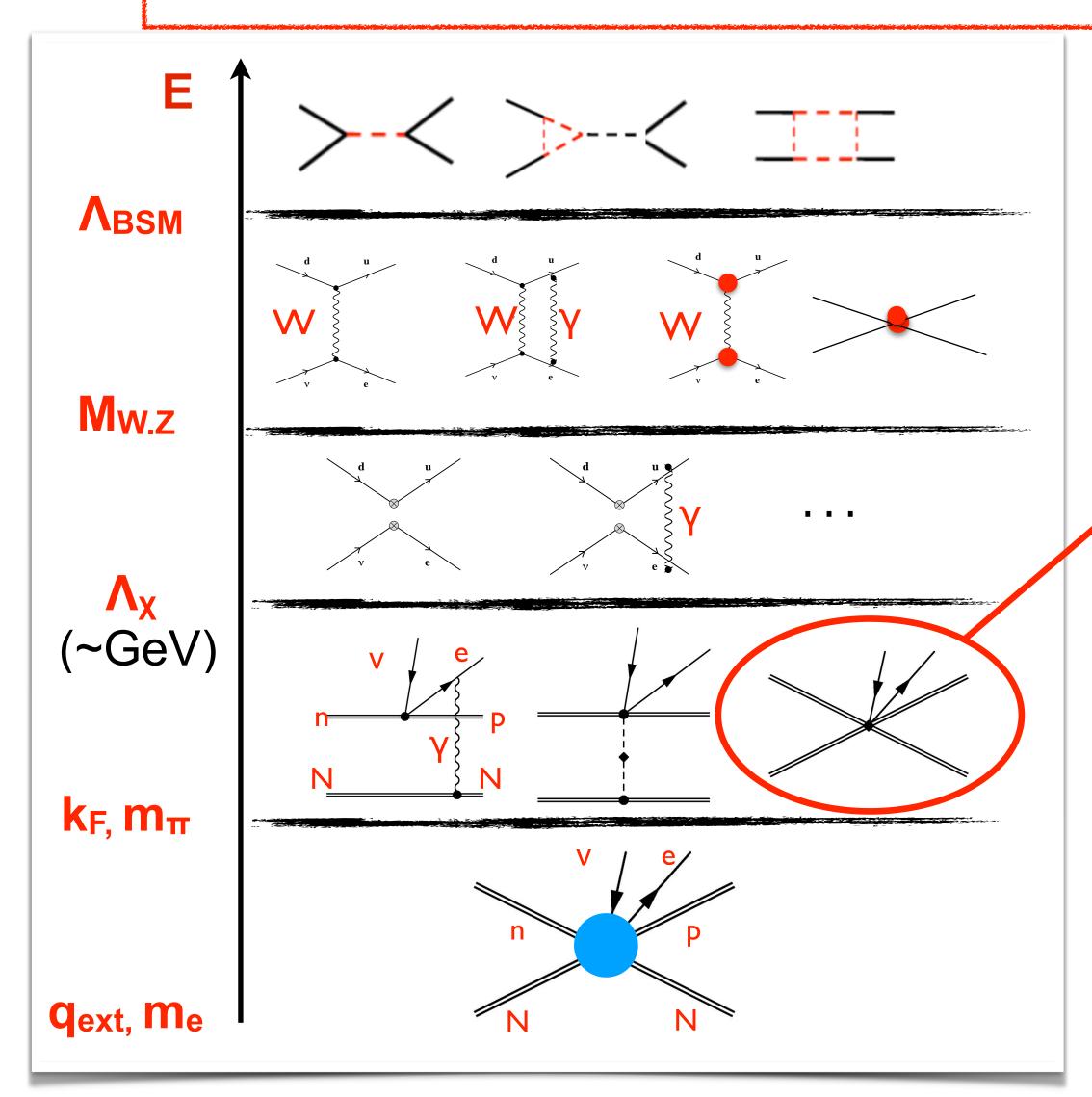
Larger radiative correction to neutron decay rate shifts  $V_{ud}$  by -0.013%

[effect due to difference in treatment of the NLL ~  $\alpha^2 Log(m_N/m_e)$  terms]



Widely separated scales:  $\Lambda_{BSM}$ ,  $M_W$ ,  $\Lambda_{\chi}$ ,  $m_{\pi}$ ,  $m_e \sim q_{ext}$ 

⇒ Tackle the problem through a tower of EFTs



#### Multi nucleon

Hard photons induce NN  $\rightarrow$  NNev contacts  $\Rightarrow$ 

$$\mathcal{L}_W^{2b} = -\sqrt{2}e^2 G_F V_{ud} \ \bar{e}_L \gamma_0 \nu_L \times$$

$$N^{\dagger} \tau^+ N \ \left( e^2 g_{V1}^{NN} \ N^{\dagger} N + e^2 g_{V2}^{NN} \ N^{\dagger} \tau^3 N \right)$$

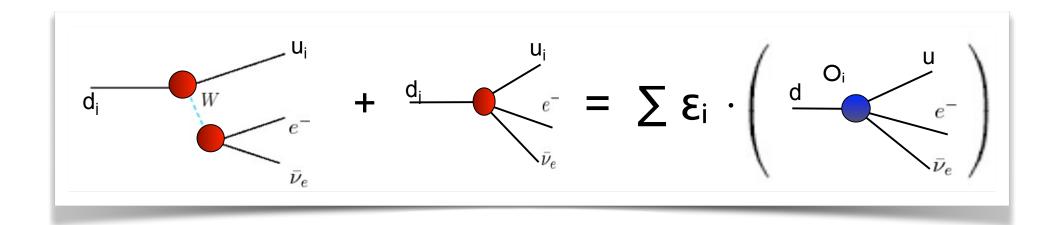
Renormalization 
$$\Rightarrow$$
  $g_{V1,V2}^{NN} \sim \frac{1}{F_{\pi}^2 \Lambda_{\chi}}$ 

 $\delta_{NS}$  in EFT: weak two body potentials of  $O(G_F \alpha \epsilon_X)$  (Recall  $m_\pi/\Lambda_X \sim 0.1$ )

Two currently unknown LECs!

# SMEFT → LEFT matching

- Wilson coefficients determined from the matching condition Asmert = Alert
- Tree-level matching for BSM operators determines ε<sub>L,R,S,P,T</sub>



• Loop-level matching for SM operators (QED / QCD loops needed for precision)

"Full" theory (higher scale EFT)

"Effective theory" (lower scale EFT)

$$\mathcal{L}_{\text{CC}} \rightarrow -\frac{G_F V_{ud}}{\sqrt{2}} C_{\beta}(\mu) \bar{e}_a \gamma_{\alpha} (1 - \gamma_5) \nu_b \cdot \bar{u} \gamma^{\alpha} (1 - \gamma_5) d + \dots$$

$$C_{\beta}(\mu) = 1 + \frac{\alpha}{50} \log \frac{M_Z}{\mu} + \dots$$
 Large log @  $\mu << M_Z$ 

#### Corrections to Vud and Vus

#### General case

$$\begin{split} |\bar{V}_{ud}|_{0^{+}\to 0^{+}}^{2} &= |V_{ud}|^{2} \left(1 + 2\left(\epsilon_{L}^{ee} + \epsilon_{R} - \epsilon_{L}^{(\mu)}\right) + c_{0^{+}}^{S}(Z) \, \epsilon_{S}^{ee}\right) \\ |\bar{V}_{ud}|_{n\to pe\bar{\nu}}^{2} &= |V_{ud}|^{2} \left(1 + 2\left(\epsilon_{L}^{ee} + \epsilon_{R} - \epsilon_{L}^{(\mu)}\right) + c_{n}^{S} \epsilon_{S}^{ee} + c_{n}^{T} \epsilon_{T}^{ee}\right) \\ |\bar{V}_{ud}|_{Ke3}^{2} &= |V_{us}|^{2} \left(1 + 2\left(\epsilon_{L}^{ee(s)} + \epsilon_{R}^{(s)} - \epsilon_{L}^{(\mu)}\right)\right) \\ |\bar{V}_{ud}|_{\pi_{e3}}^{2} &= |V_{ud}|^{2} \left(1 + 2\left(\epsilon_{L}^{ee} + \epsilon_{R} - \epsilon_{L}^{(\mu)}\right)\right) \\ |\bar{V}_{us}|_{K\mu_{2}}^{2} &= |V_{us}|^{2} \left(1 + 2\left(\epsilon_{L}^{\mu\mu(s)} - \epsilon_{R}^{(s)} - \epsilon_{L}^{(\mu)}\right) - 2\frac{B_{0}}{m_{\ell}} \, \epsilon_{P}^{\mu\mu(s)}\right) \\ |\bar{V}_{ud}|_{\pi\mu_{2}}^{2} &= |V_{ud}|^{2} \left(1 + 2\left(\epsilon_{L}^{\mu\mu} - \epsilon_{R} - \epsilon_{L}^{(\mu)}\right) - 2\frac{B_{0}}{m_{\ell}} \, \epsilon_{P}^{\mu\mu}\right) \end{split}$$

ε<sub>S</sub>(s): shifts the slope of the scalar form factor, at levels well below EXP and TH uncertainties

E<sub>T</sub>(s): suppressed by m<sub>lept</sub>/m<sub>K</sub>

# Electroweak precision observables

Obs.	Expt. V	alue	SM Predict:	ion	Obs.	Expt. Val	Expt. Value		tion
$\Gamma_Z  ({ m GeV})$	2.4955(23)	[53, 113]	2.49414(56)	[60]	$m_W({ m GeV})$	80.4335(94)	[39]	80.3545(42)	[60]
$\sigma_{ m had}^0({ m nb})$	41.480(33)	[53, 113]	41.4929(53)	[60]	$\Gamma_W  ({ m GeV})$	2.085(42)	[3]	2.08782(52)	[60]
$R_e^0$	20.804(50)	[53, 113]	20.7464(63)	[60]	$R_{Wc}$	0.49(4)	[3]	0.50	
$R_{\mu}^{0}$	20.784(34)	[53, 113]			$R_{\sigma}$	0.998(41)	[114]	1	
$R_{ au}^{0}$	20.764(45)	[53, 113]			$Br(W \to e\nu)$	0.1071(16)	[3]	0.108386(24)	[60]
$A_{ m FB}^{0,e}$	0.0145(25)	[53, 113]	0.016191(70)	[60]	$\text{Br}(W \to \mu\nu)$	0.1063(15)	[3]	0.108386(24)	[60]
$A_{ m FB}^{0,\mu}$	0.0169(13)	[53, 113]			$Br(W \to \tau \nu)$	0.1138(21)	[3]	0.108386(24)	[60]
$A_{ m FB}^{0, au}$	0.0188(17)	[53, 113]			$\frac{\Gamma(W \to \mu\nu)}{\Gamma(W \to e\nu)}$	0.982(24)	[3]	1	
$R_b^0$	0.21629(66)	[53]	0.215880(19)	[60]	$\frac{\Gamma(W \to \mu\nu)}{\Gamma(W \to e\nu)}$	1.020(19)	[3]		
$R_c^0$	0.1721(30)	[53]	0.172198(20)	[60]	$\frac{\Gamma(W \to \mu\nu)}{\Gamma(W \to e\nu)}$	1.003(10)	[3]		
$A_{ m FB}^{0,b}$	0.0996(16)	[53]	0.10300(23)	[60]	$\frac{\Gamma(W \to \tau \nu)}{\Gamma(W \to e \nu)}$	0.961(61)	[3]		
$A_{ m FB}^{0,c}$	0.0707(35)	[53]	0.07358(18)	[60]	$\frac{\Gamma(W \to \tau \nu)}{\Gamma(W \to \mu \nu)}$	0.992(13)	[3]		
$\mathcal{A}_c$	0.67(3)	[53]	0.66775(14)	[60]	$A_4(0-0.8)$	0.0195(15)	[115]	0.0144(7)	[116]
$\mathcal{A}_b$	0.923(20)	[53]	0.934727(25)	[60]	$A_4(0.8-1.6)$	0.0448(16)	[115]	0.0471(17)	[116]
$\mathcal{A}_e$	0.1516(21)	[53]	0.14692(32)	[60]	$A_4(1.6-2.5)$	0.0923(26)	[115]	0.0928(21)	[116]
${\cal A}_{\mu}$	0.142(15)	[53]			$A_4(2.5-3.6)$	0.1445(46)	[115]	0.1464(21)	[116]
${\cal A}_{ au}$	0.136(15)	[53]			$g_V^{(u)}$	0.201(112)	[117]	0.192	[118]
$\mathcal{A}_e^{ au\mathrm{pol}}$	0.1498(49)	[53]			$g_V^{(d)}$	-0.351(251)	[117]	-0.347	[118]
${\cal A}_{ au}^{ au  m pol}$	0.1439(43)	[53]			$g_A^{(u)}$	0.50(11)	[117]	0.501	[118]
$\mathcal{A}_s$	0.895(91)	[119]	0.935637(26)	[60]	$g_A^{(d)}$	-0.497(165)	[117]	-0.502	[118]
$R_{uc}$	0.166(9)	[3]	0.172220(20)	[60]					