

Small- x Helicity Global Analysis: Now With Polarized pp Data

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Proton Spin Puzzle and Small- x

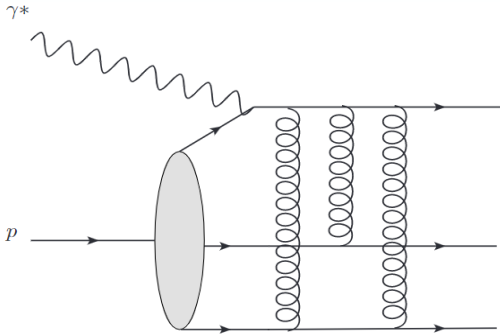
- Proton Spin $\equiv \frac{1}{2}$, Experimental Measurement of spin coming from partons $\neq \frac{1}{2}$

- Jaffe-Manohar sum rule [1]: $S_q + L_q + S_G + L_G = \frac{1}{2}$

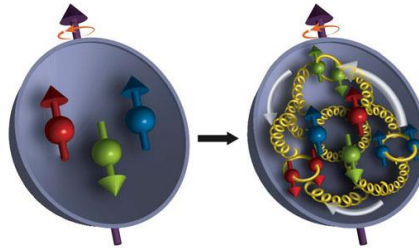
$$S_q(Q^2) = \frac{1}{2} \int_0^1 dx \Delta\Sigma(x, Q^2), \quad S_G(Q^2) = \int_0^1 dx \Delta G(x, Q^2)$$

- Experimental data only exists for a range of values $x \in [x_{min}, 1]$

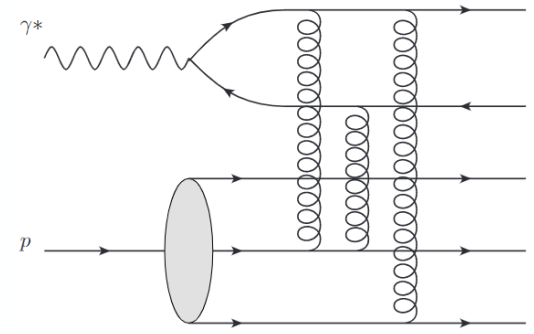
“Knockout” DIS at Large- x



$$x = \frac{Q^2}{s + Q^2} \sim \frac{Q^2}{E_{CM}^2} \sim \frac{1}{m \Delta t_{Ioffe}}$$



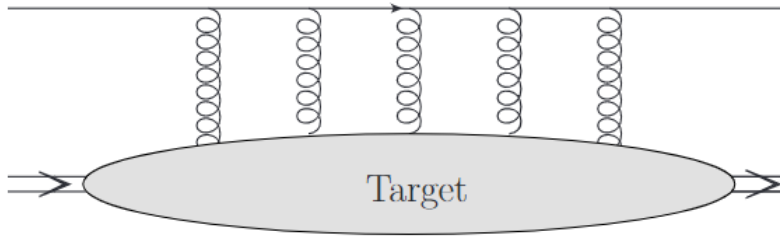
“Dipole” DIS at Small- x



At small- x and with large Ioffe time our degrees of freedom change from quarks and gluons to eikonal Wilson Lines, and the proton appears very dense and frozen.

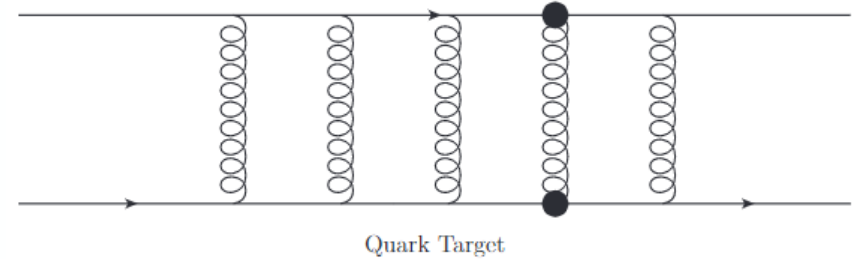
Sub-Eikonal Corrections and Double Logs

Unpolarized Wilson Line

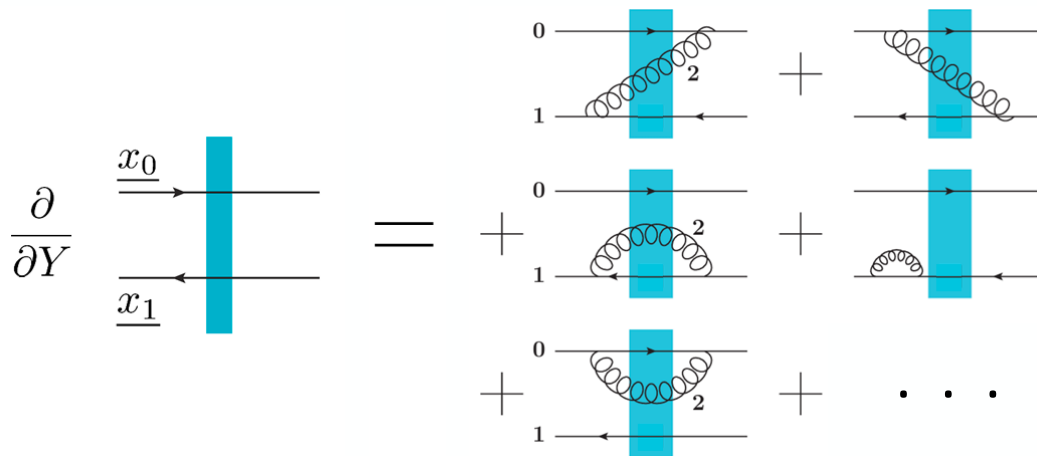


$$V_0 = \mathcal{P} \exp \left[ig \int_{-\infty}^{+\infty} dx^- A^+(x^+ = 0, x^-, \underline{x}_0) \right]$$

Polarized Wilson Line



$$\left(V_{\underline{x}}^{pol} \right)^g \propto \int_{-\infty}^{\infty} dx^- V_{\underline{x}}[+\infty, x^-] F^{12}(x^-, \underline{x}) V_{\underline{x}}[x^-, -\infty]$$



Radiative Corrections



Small- x Evolution

Unpolarized evolution: $\alpha_s \ln \frac{1}{x} \sim 1$

Polarized evolution: $\alpha_s \ln^2 \frac{1}{x} \sim 1$

KPS-CTT Evolution and Helicity Distribution

KPS-CTT = Kovchegov-Pitonyak-Sievert-Cougoulic-Tarasov-Tawabutr

$$Q_{10}(zs) \equiv \frac{1}{2N_c} \text{Re} \left\langle \left\langle \text{Tr} \left[V_0 V_1^{\text{pol}[1] \dagger} \right] + \text{Tr} \left[V_1^{\text{pol}[1]} V_0^\dagger \right] \right\rangle \right\rangle (zs).$$

Polarized dipole amplitudes are various combinations of polarized and unpolarized Wilson lines [2-4].

$$G_{10}^i(zs) \equiv \frac{1}{2N_c} \left\langle \left\langle \text{tr} \left[V_0^\dagger V_1^{i \text{G}[2]} + \left(V_1^{i \text{G}[2]} \right)^\dagger V_0 \right] \right\rangle \right\rangle (zs)$$

...

$$Q_f(x_{10}^2, zs) \sim Q_f^{(0)}(x_{10}^2, zs) + \iint [2\tilde{G} + \tilde{\Gamma} + Q_f - \bar{\Gamma}_f + 2\Gamma_2 + 2G_2] + \iint [Q_f + 2G_2]$$

$$\bar{\Gamma}_f(x_{10}^2, x_{21}^2, z's) \sim Q_f^{(0)}(x_{10}^2, z's) + \iint [2\tilde{G} + 2\tilde{\Gamma} + Q_f - \bar{\Gamma}_f + 2\Gamma_2 + 2G_2] + \iint [Q_f + 2G_2]$$

$$\tilde{G}(x_{10}^2, zs) \sim \tilde{G}^{(0)}(x_{10}^2, zs) + \iint [3\tilde{G} + \tilde{\Gamma} + 2G_2 + \Gamma_2 - \bar{\Gamma}_f] - \iint [Q_f + 2G_2]$$

$$\tilde{\Gamma}(x_{10}^2, x_{21}^2, z's) \sim \tilde{G}^{(0)}(x_{10}^2, z's) + \iint [3\tilde{G} + \tilde{\Gamma} + 2G_2 + \Gamma_2 - \bar{\Gamma}_f] - \iint [Q_f + 2G_2]$$

$$G_2(x_{10}^2, zs) \sim G_2^{(0)}(x_{10}^2, zs) + \iint [\tilde{G} + 2G_2]$$

$$\Gamma_2(x_{10}^2, x_{21}^2, z's) \sim G_2^{(0)}(x_{10}^2, z's) + \iint [\tilde{G} + 2G_2]$$

(Large- N_c & N_f)

$$\Delta G \propto G_2$$

$$\Delta \Sigma \propto -\iint [Q_f + 2G_2]$$

$$\Delta q_f^{NS} \propto \iint [G_f^{NS}]$$

$$A_{\parallel}^{DIS} \propto A_1 \propto g_1^p \propto -\iint [Q_f + 2G_2]$$

$$Q_f^{(0)}, \tilde{G}^{(0)}, G_2^{(0)}, G_f^{NS(0)} \\ (x \approx 0.1)$$



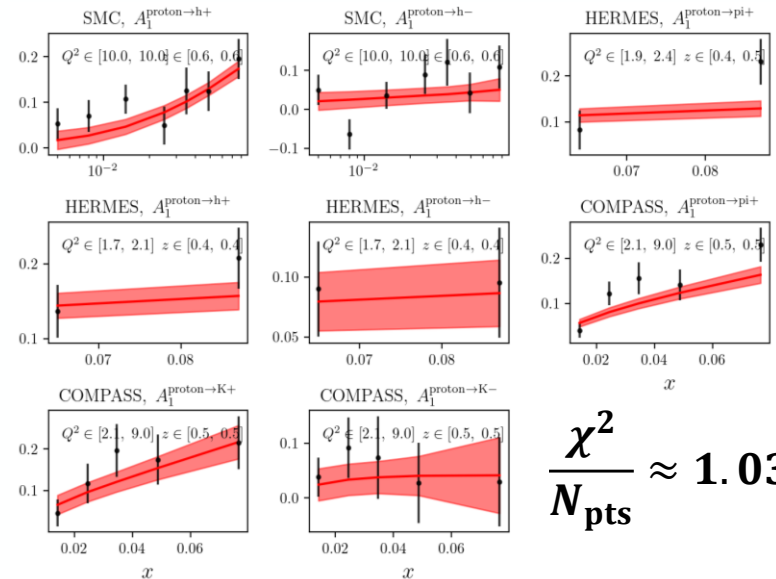
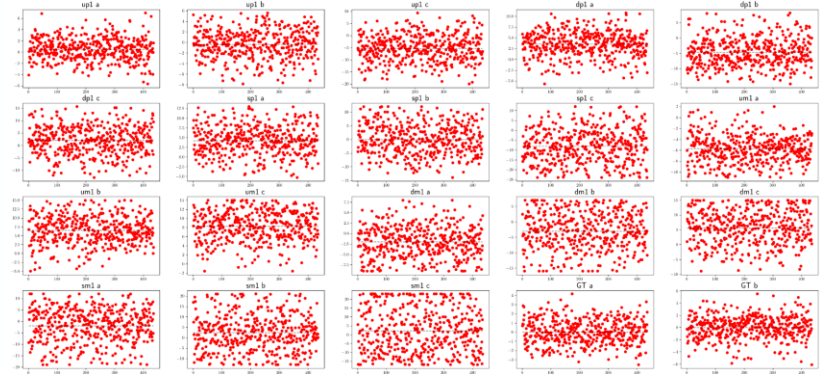
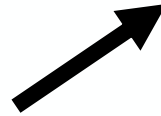
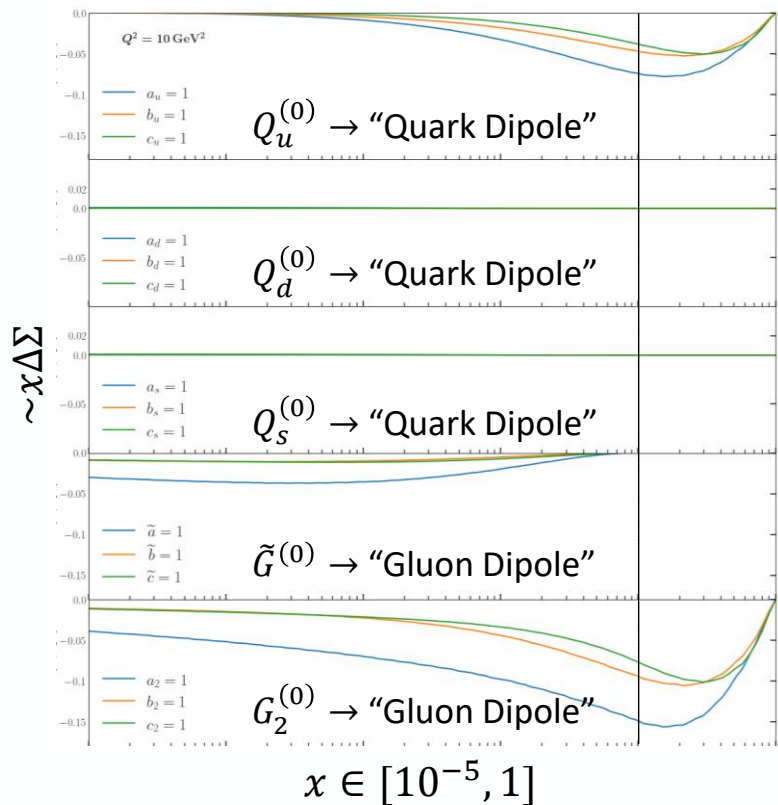
KPS-CTT [5]



$$\Delta G, \Delta \Sigma, \Delta q_f^{NS}, g_1 \\ (x \ll 0.1)$$

Global Analysis: Bayesian-MC Analysis

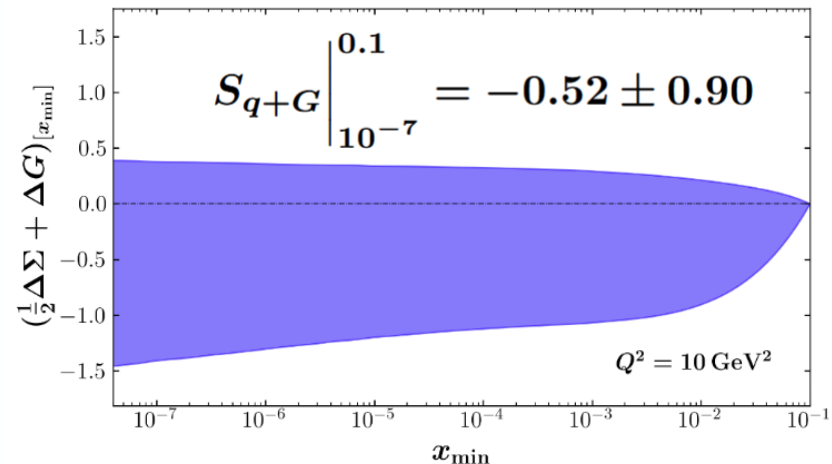
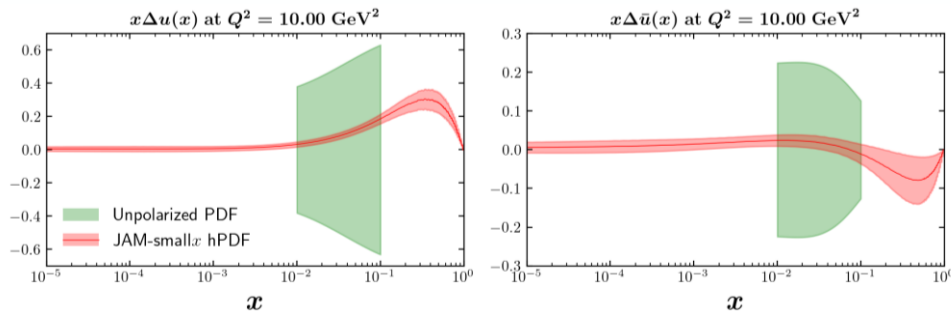
$$G^{(0)} \approx \mathbf{a}\boldsymbol{\eta} + \mathbf{b}s_{10} + \mathbf{c}$$



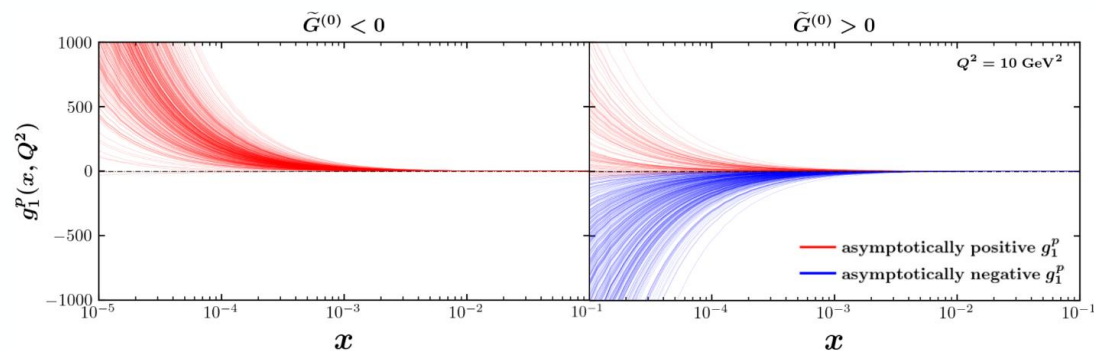
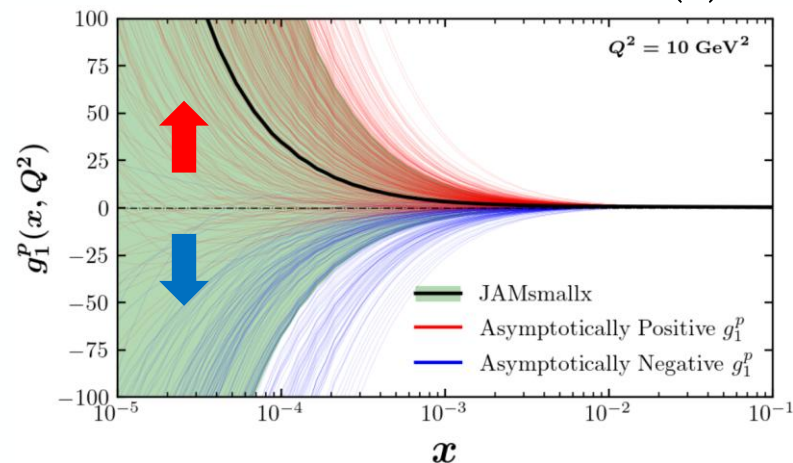
- Compute **Full Evolution** from any parameter.
- Chi-squared optimization for **DIS and SIDIS data**.

Global Analysis: Success and Setback with SIDIS

SIDIS data improves the first analysis [6] and allows us to separate quark flavor hPDFs, Δq_f , from $\Delta \Sigma$.



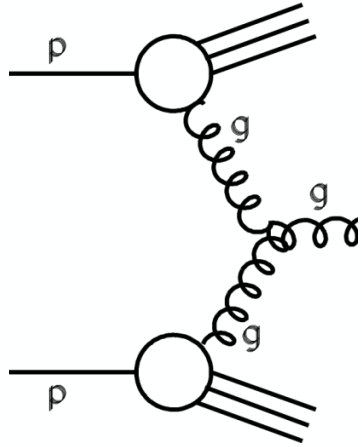
$$\lim_{x \rightarrow 0} g_1^p \sim \lim_{x \rightarrow 0} \Delta \Sigma \sim \lim_{x \rightarrow 0} \Delta G \sim \left(\frac{1}{x} \right)^{\alpha_h}$$



Asymptotic bimodality is caused by the insensitivity of DIS and SIDIS data to **gluon dominated dipole amplitudes** [7].

Global Analysis with pp Data

Polarized proton-proton collisions allow for gluon-gluon interactions and thus can be more sensitive to the gluon dominated polarized dipole amplitudes.



(Picture from CERN)

The polarized pp data available is A_{LL}^{jet} , with jet cross-section [8]:

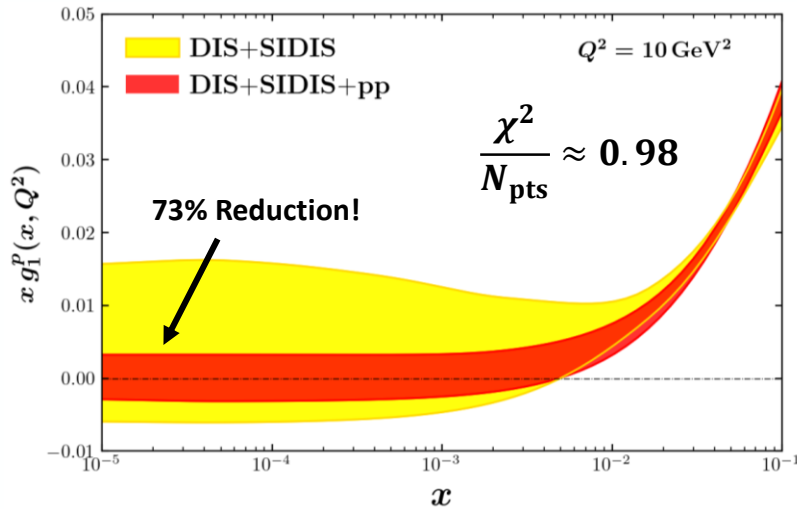
$$\frac{d\Delta\sigma^{pp\rightarrow\text{jet}X}}{d^2p_T^{\text{jet}} d\eta^{\text{jet}}} = \frac{1}{\pi S} \int_{x_g^P, \min}^1 \frac{dx_g^P}{x_g^P} \Delta f_g^P(x_g^P, \mu_F) \int_{x_g^T, \min}^1 \frac{dx_g^T}{x_g^T} \Delta f_g^T(x_g^T, \mu_F) \\ \times \int_{z_g^{\min}}^1 \frac{dz_g}{z_g^2} \frac{d\Delta\hat{\sigma}_{gg}^g(\lambda, \hat{s}, \hat{p}_T, \hat{\eta}, \mu_F, \mu'_F, \mu_R)}{v dv dw} \mathcal{J}_g\left(z_g, \frac{R p_T^{\text{jet}}}{\mu'_F}, \mu_R\right)$$

DLA Accuracy: Only the leading order term in the jet function $\mathcal{J}_g$ preserves the resummation parameter $\alpha_s \ln^2(\frac{1}{x})$: $\mathcal{J}_g \equiv \delta(1 - z_g)$

The **small- x** cross-section in the pure-gluon limit:

$$\frac{d\Delta\sigma^{pp\rightarrow\text{jet}X}}{d^2p_T dy} = \frac{8C_F}{\pi^3} \frac{1}{s p_T^2} \int_0^\infty dx_\perp \frac{1}{\alpha_s(1/x_\perp^2)} x_\perp J_0(p_T x_\perp) \left(x_{T,P} \approx \frac{p_T}{\sqrt{s}} e^{\pm y} < 0.1 \right) \\ \times \left[2G_{2,P} \nabla_\perp^2 \tilde{G}_T + 2(\nabla_\perp^2 \tilde{G}_P) G_{2,T} + \frac{\partial}{\partial x_\perp} \tilde{G}_P \frac{\partial}{\partial x_\perp} \tilde{G}_T + 2 \frac{\partial}{\partial x_\perp} G_{2,P} \frac{\partial}{\partial x_\perp} \tilde{G}_T + 2 \frac{\partial}{\partial x_\perp} \tilde{G}_P \frac{\partial}{\partial x_\perp} G_{2,T} \right]$$

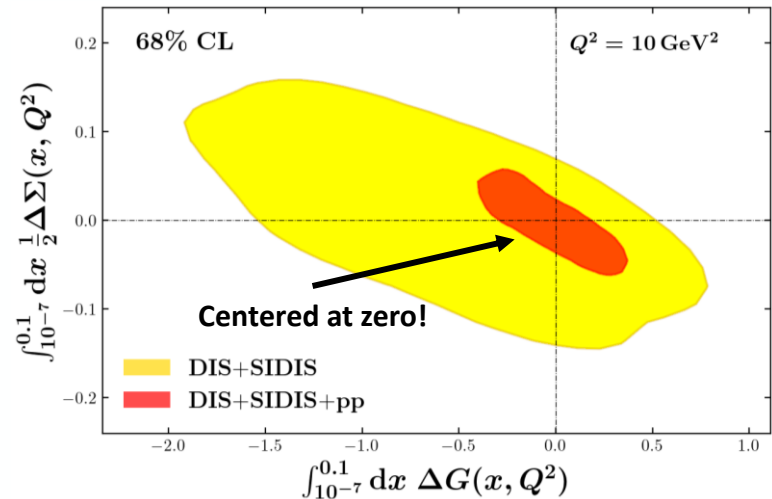
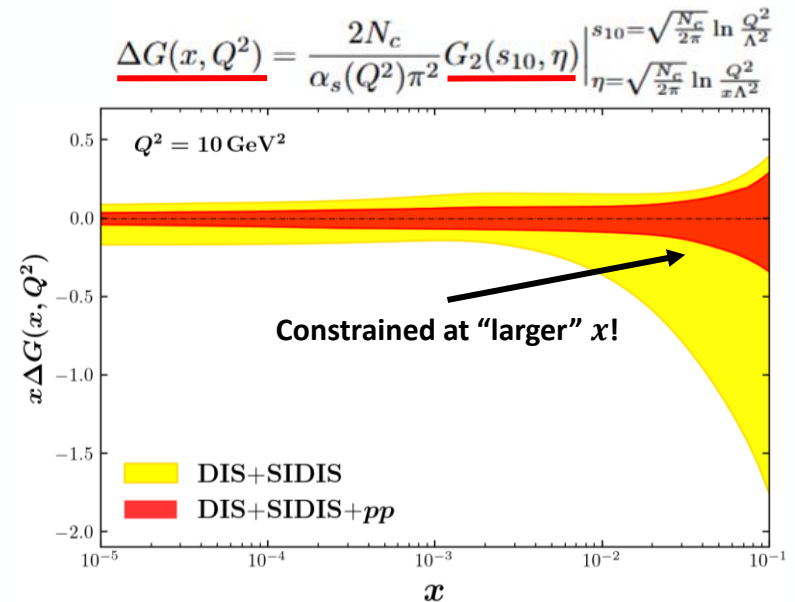
Influence of pp Data



DIS+SIDIS: $S_{q+G} \Big|_{10^{-7}}^{0.1} = -0.52 \pm 0.90$

DIS+SIDIS+pp: $S_{q+G} \Big|_{10^{-7}}^{0.1} = -0.04 \pm 0.23$

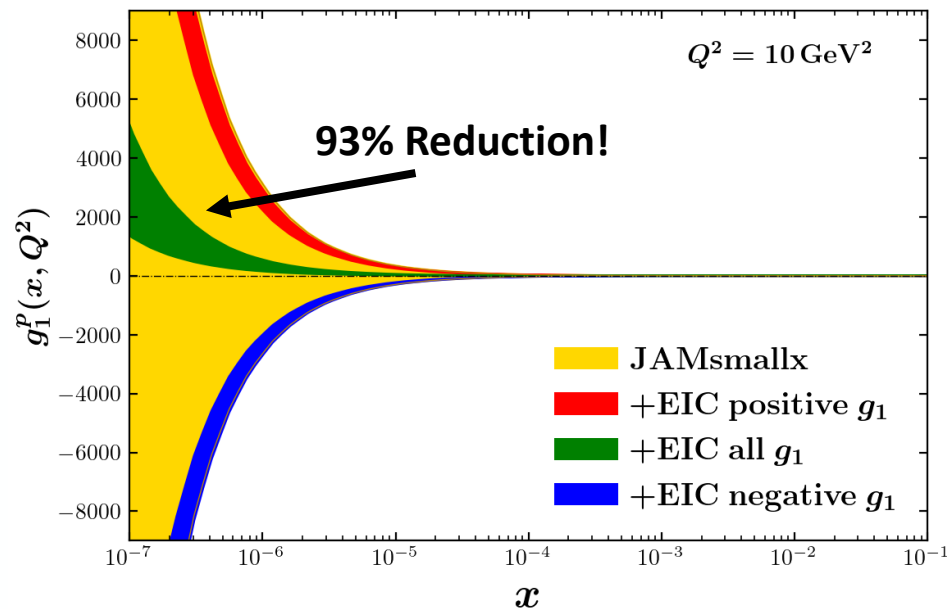
Uncertainty spans zero $\rightarrow$ Bimodality persists



EIC Impact Study

EIC Pseudo data: Create data points with EIC-consistent uncertainties/kinematics [10] using small-x theory input.

- $10^{-4} < x < 10^{-1}$, $1.69 \text{ GeV}^2 < Q^2 < 50 \text{ GeV}^2$
- Proton DIS: $\sqrt{s} = \{29, 45, 63, 141\} \text{ GeV}$, $L = 100 \text{ fb}^{-1}$
- Deuteron/ ^3He DIS: $\sqrt{s} = \{29, 66, 89\} \text{ GeV}$, $L = 10 \text{ fb}^{-1}$
- 2% point-to-point systematic uncertainty



Final Thoughts

- Small- x helicity global analysis is successful and **not degraded** with the inclusion of polarized pp data.
- pp data drastically reduces uncertainty, especially for larger- x gluon hPDFs.
- Asymptotic bimodality persists → Can be broken with smaller- x data ($x \approx 10^{-4}$).
- Net quark and gluon spin now consistent with zero:
 - How will this be affected by re-introducing quarks?
 - Quark and gluon OAM contributions?

Interested? Check arXiv soon!
(also I'm available for a postdoc position!)



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Cuts on Data

- We fit to all available DIS and SIDIS data within the kinematic ranges $5 \times 10^{-3} < x < 0.1$ and $1.69 \text{ GeV}^2 < Q^2 < 10.4 \text{ GeV}^2$
- This leaves a total of 240 data points in the JAM database.

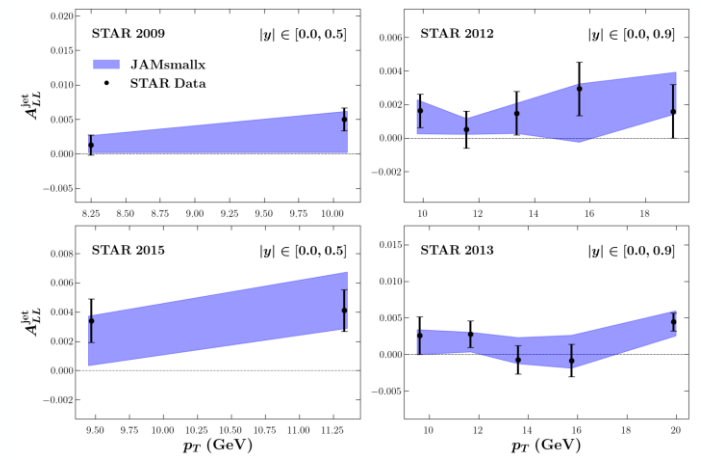


TABLE II. Summary of the polarized SIDIS data on A_1^h included in the fit, along with the χ^2/N_{pts} for each data set.

Dataset (A_1^h)	Target	Tagged Hadron	N_{pts}	χ^2/N_{pts}
COMPASS [132]	d	π^+	5	0.63
	d	π^-	5	0.83
	d	h^+	5	1.01
	d	h^-	5	1.02
	d	K^+	5	1.60
	d	K^-	5	0.71
COMPASS [133]	p	π^+	5	1.94
	p	π^-	5	1.18
	p	K^+	5	0.46
	p	K^-	5	0.23
HERMES [134]	^3He	h^+	2	0.55
	^3He	h^-	2	0.29
HERMES [135]	p	π^+	2	2.75
	p	π^-	2	0.00
	p	h^+	2	1.25
	p	h^-	2	0.19
	d	π^+	2	0.58
	d	π^-	2	1.23
	d	h^+	2	3.03
	d	h^-	2	1.24
	d	K^+	2	0.82
	d	K^-	2	0.25
	d	$K^+ + K^-$	2	0.36
SMC [136]	p	h^+	7	1.22
	p	h^-	7	1.41
	d	h^+	7	0.84
	d	h^-	7	1.52
Total			104	1.04

TABLE I. Summary of polarized DIS data included in the fit, separated into A_1 (left) and $A_{\parallel}$ (right), along with the χ^2/N_{pts} for each data set.

Data set (A_1)	Target	N_{pts}	χ^2/N_{pts}
COMPASS [120]	p	5	0.77
COMPASS [121]	p	17	0.93
COMPASS [122]	d	5	0.34
EMC [123]	p	5	0.23
HERMES [124]	n	2	1.11
SLAC (E142) [125]	^3He	1	1.47
SMC [126, 127]	p	6	1.26
	p	6	0.43
	d	6	0.65
	d	6	2.13
Total		59	0.90

Data set ($A_{\parallel}$)	Target	N_{pts}	χ^2/N_{pts}
HERMES [128]	p	4	1.47
	d	4	1.00
SLAC (E143) [129]	p	9	0.55
	d	9	1.01
SLAC (E154) [130]	^3He	5	0.69
SLAC(E155) [131]	p	16	1.07
	d	16	1.57
Total		63	1.10

TABLE III. Summary of polarized pp data on $A_{\text{LL}}^{\text{jet}}$ included in the fit along with the χ^2/N_{pts} for each data set.

Data set ($A_{\text{LL}}^{\text{jet}}$)	N_{pts}	χ^2/N_{pts}
STAR [137]	2	0.60
STAR [138]	5	0.30
STAR [139]	2	0.55
STAR [140]	5	0.24
Total	14	0.36

Extras

EIC impact: DGLAP extrapolation vs KPS-CTT prediction

- EIC pseudodata can break the bimodality, predicting a specific sign as $x \rightarrow 0$.
- Uncertainties in the extrapolation region are much smaller using small- x helicity than those using DGLAP evolution.

