

Probing dense nuclear matter at small x

Updates from SURGE & nCTEQ

Fred Olness
SMU

*Thanks for substantial input
from my friends & colleagues*



nCTEQ
nuclear parton distribution functions



Gluon Saturation, Diffraction
& Multihadron Production at the EIC:
Stony Brook University
14 July 2026

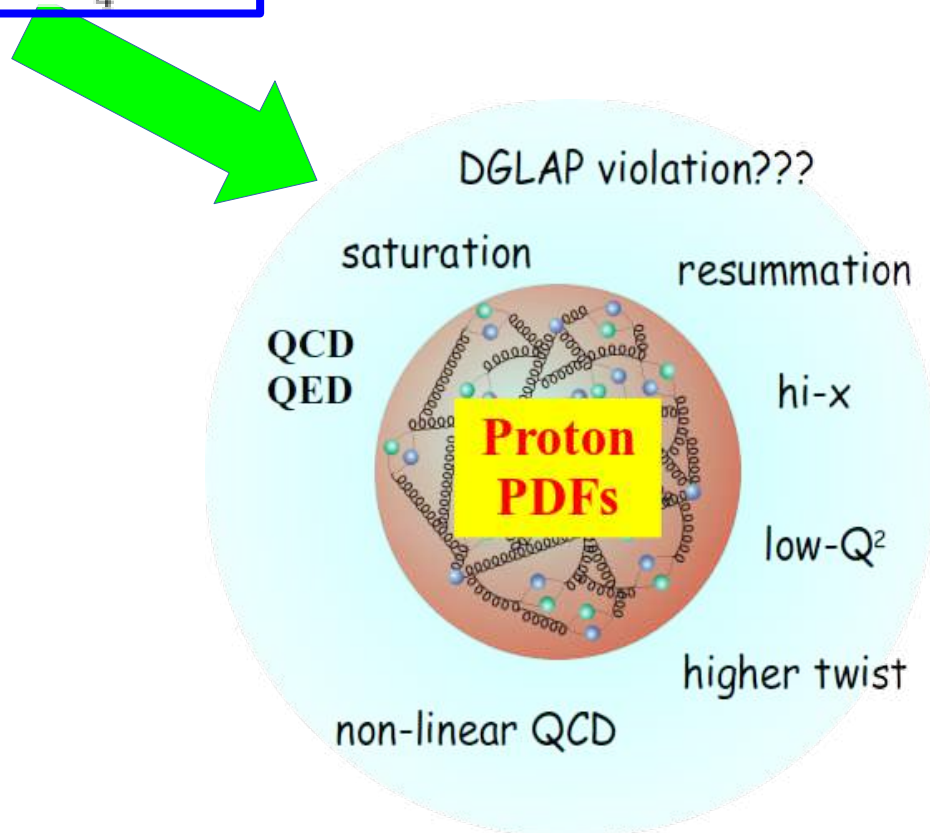
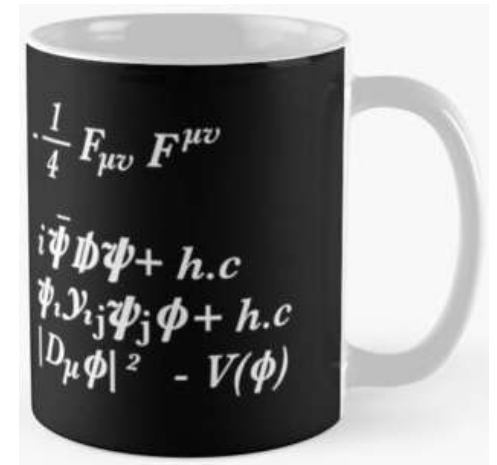
Quantum ChromoDynamics

QCD

Lagrangian

$$\mathcal{L}_{QCD} = \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$

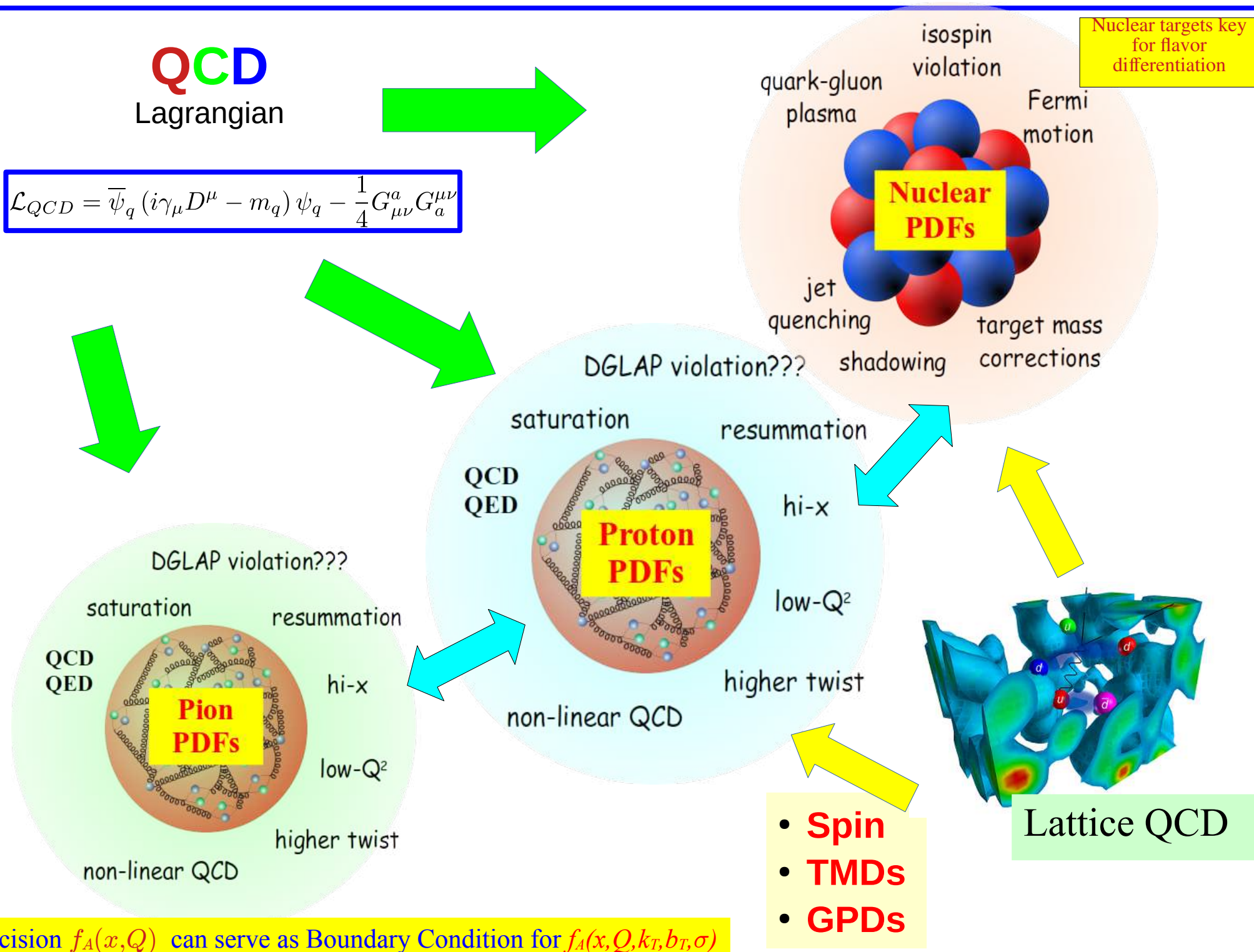
Conjecture: A theory can't be fundamental unless it fits on a coffee mug.



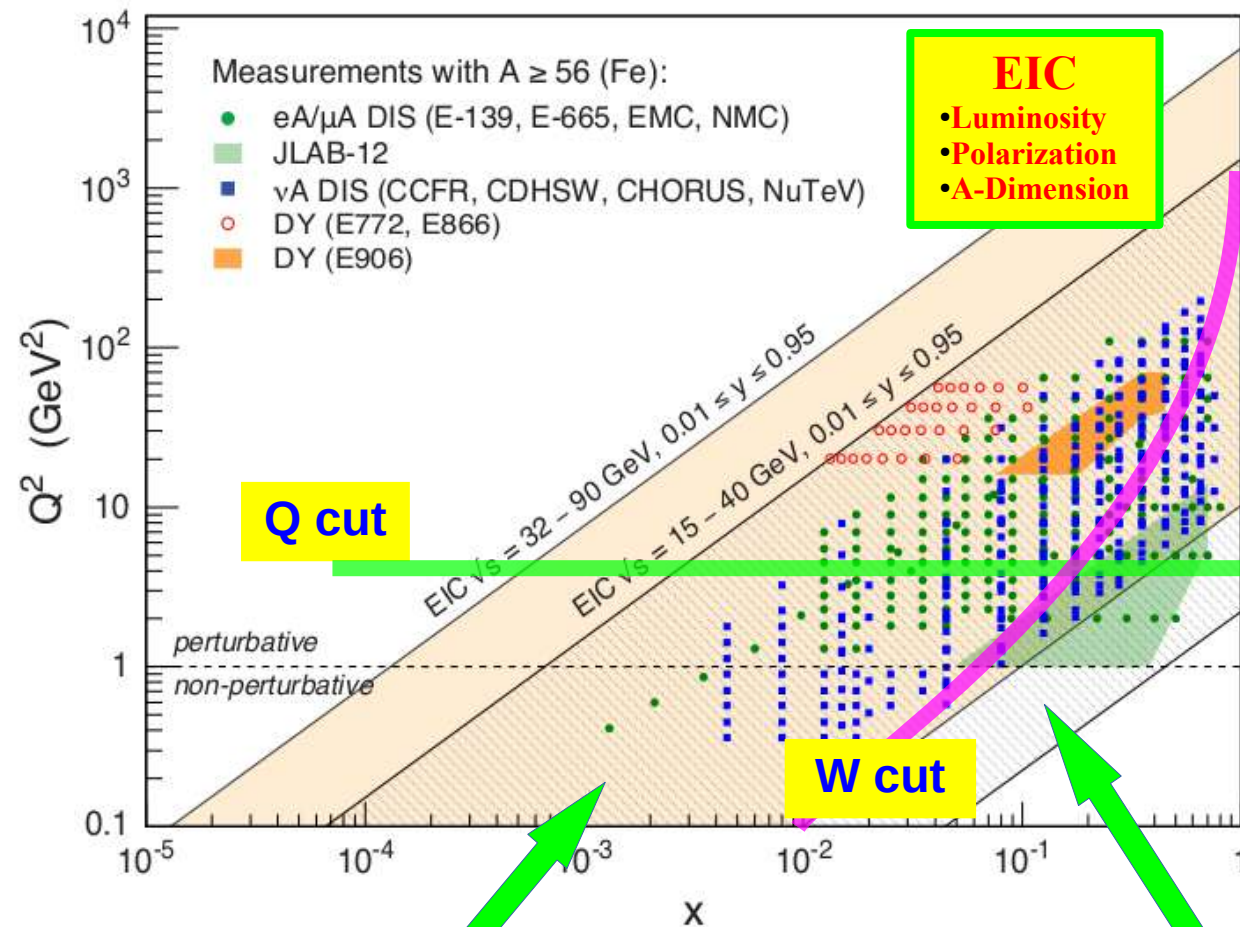
... we can go further

QCD
Lagrangian

$$\mathcal{L}_{QCD} = \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$



precision $f_A(x, Q)$ can serve as Boundary Condition for $f_A(x, Q, k_T, b_T, \sigma)$



High- x :

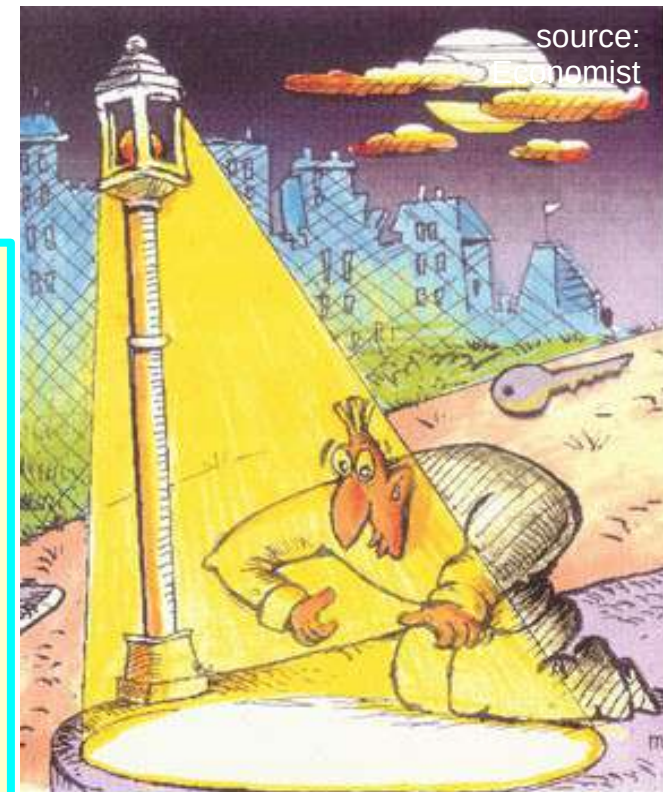
Nuclear PDFs: $x > 1$ allowed;
 impacts $F_2^{\text{Nuc}}/F_2^{\text{Iso}}$ in Fermi region
 Target Mass Corrections
 pick up M^2/Q^2 higher twist
 Deuteron Corrections
 impacts $F_2^{\text{Nuc}}/F_2^{\text{Deuteron}}$ ratio

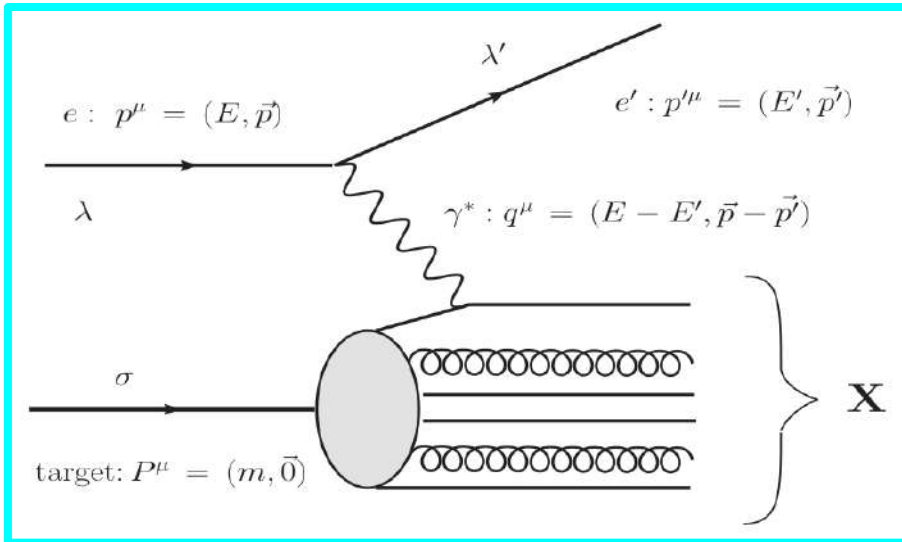
Low- x :

Shadowing
 Recombination
 Resummation
 BFKL
 Saturation

Low- Q^2 :

Non-Perturbative interface
 collective effects
 Target Mass Corrections
 pick up M^2/Q^2 higher twist
 F_L at low Q^2 access to $g(x)$
 Run at multiple energies





Parton Model

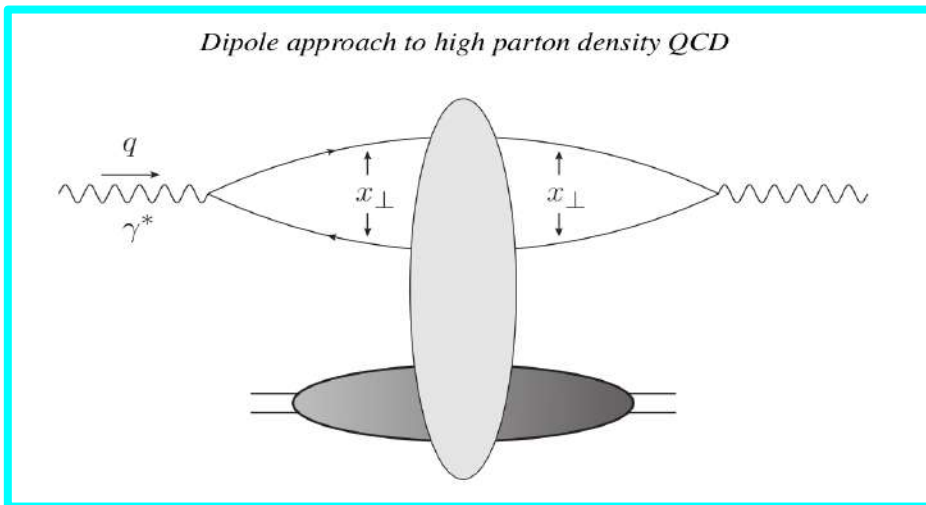
$$\sigma = f_{P \rightarrow a}(x, Q) \otimes \hat{\sigma}_{a\gamma \rightarrow X}(x, \hat{s})$$

Implemented in **xFitter**
uses several numerical “tricks”
for efficient computation

Dipole Model

GOAL: Develop flexible
framework to test
initial/final-state, spin, NLO ...

The dipole model excels at small- x and
describes the transition between perturbative
and non-perturbative QCD regime.
Incorporates “shadowing” or “saturation”
which is key for dense gluon configurations.



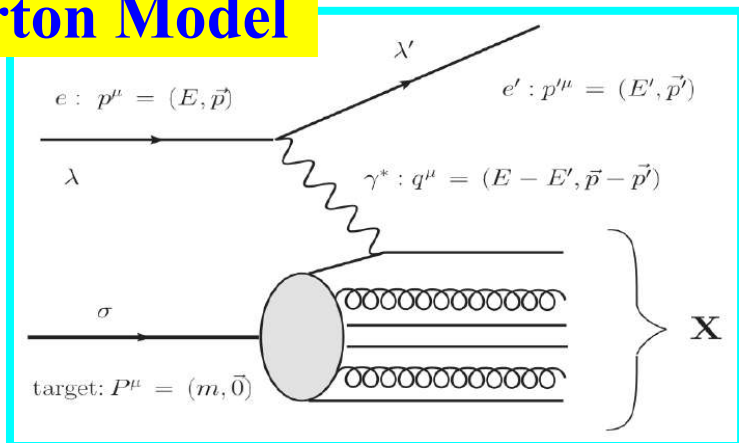
$$\sigma_{tot}^{\gamma^* A}(x, Q^2) \simeq \iint |\Psi^{\gamma^* \rightarrow q\bar{q}}(x_\perp, z)|^2 \otimes \sigma_{tot}^{q\bar{q} A}(x_\perp, Y)$$

Signatures of gluon saturation from structure-function measurements

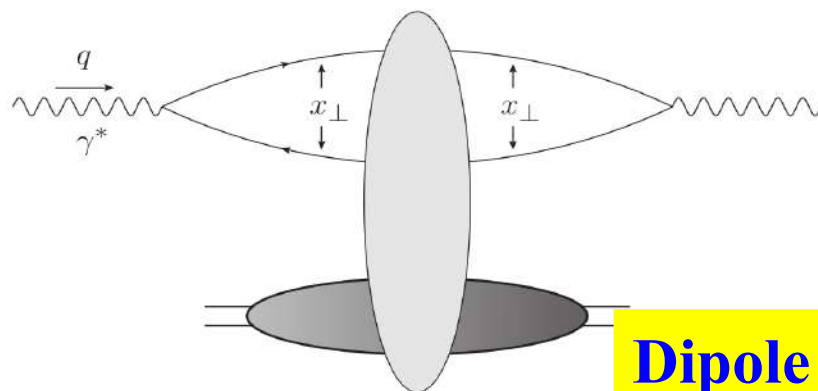
Nestor Armesto,^{1,*} Tuomas Lappi,^{2,3,†} Heikki Mäntysaari,^{2,3,‡} Hannu Paukkunen,^{2,3,§} and Mirja Tevio^{2,3,¶}

Phys.Rev.D 105 (2022) 11, 114017 • e-Print: 2203.05846 [hep-ph]

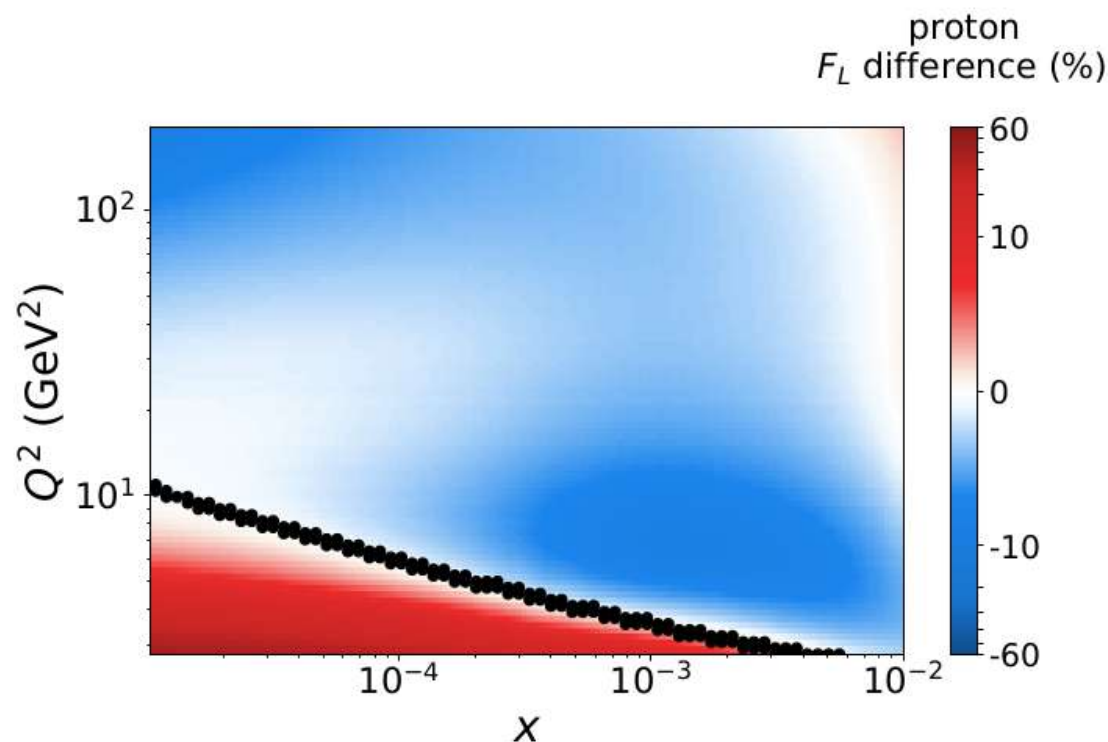
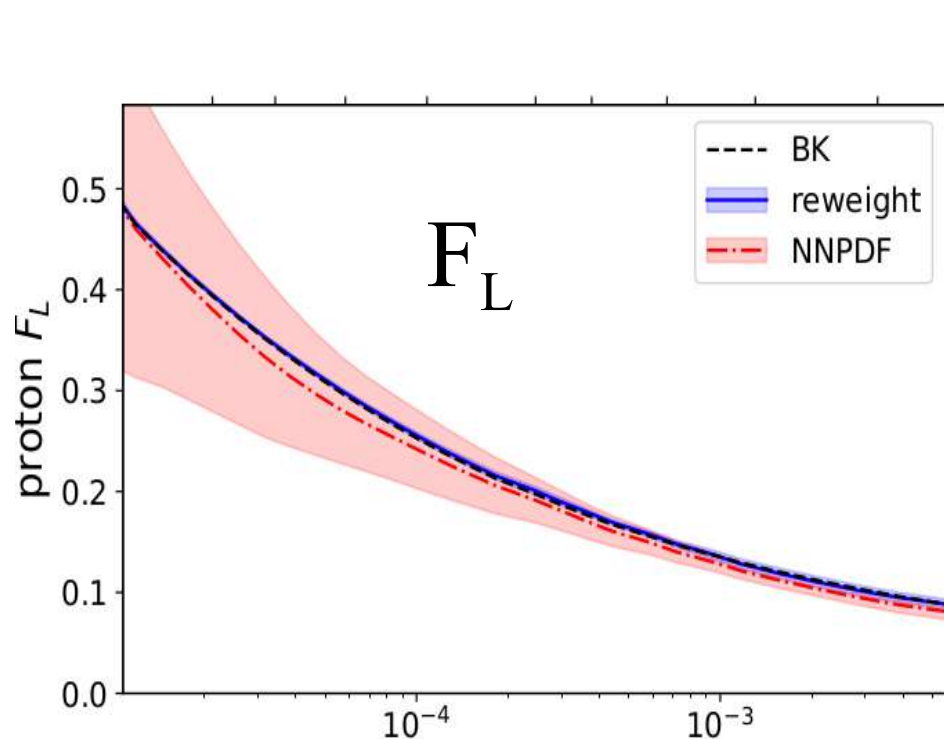
Parton Model



Dipole approach to high parton density QCD



Dipole Model

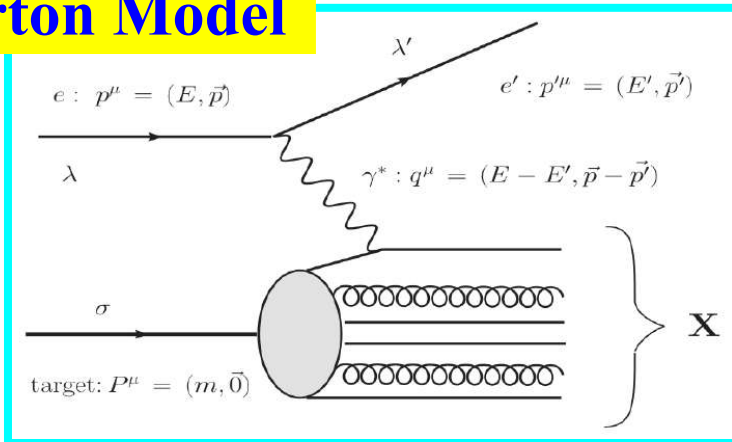


Signatures of gluon saturation from structure-function measurements

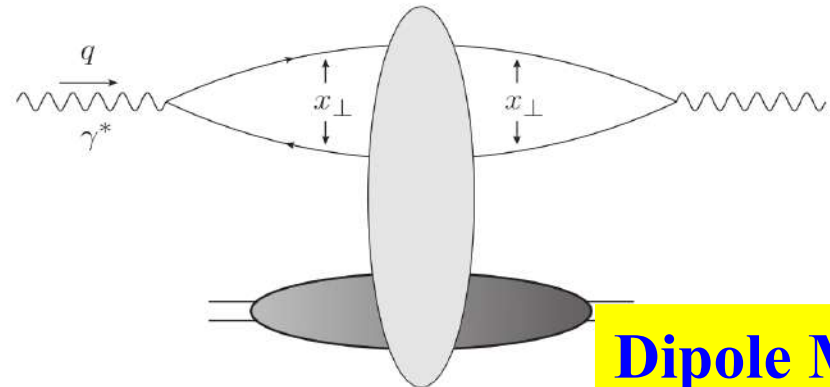
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Parton Model



Dipole approach to high parton density QCD



Dipole Model

nCTEQ
nuclear parton distribution functions



nCTEQ

nuclear parton distribution functions

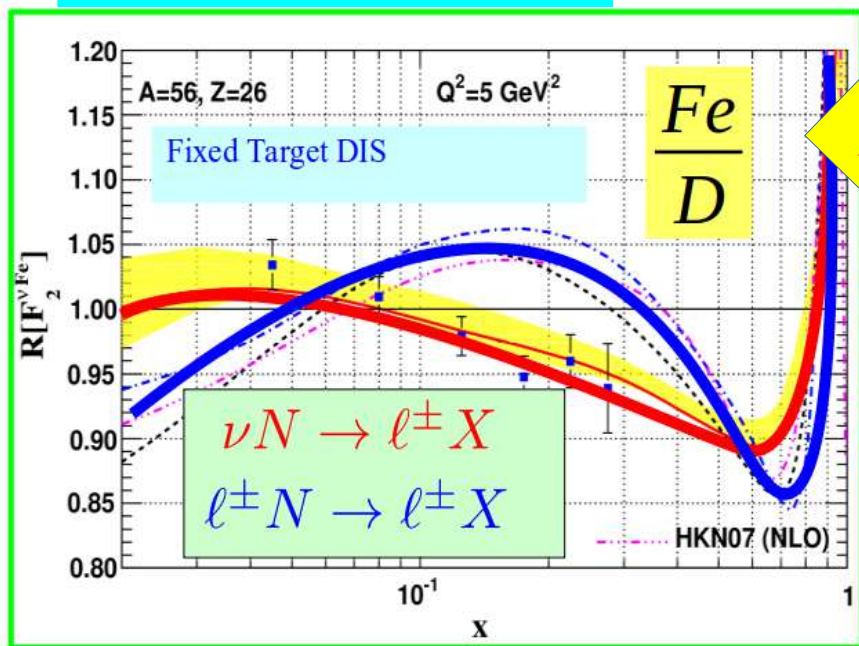
nCTEQ project is an extension of the CTEQ collaborative effort to determine nuclear parton distribution functions (nPDFs).

Grenoble, April 2024



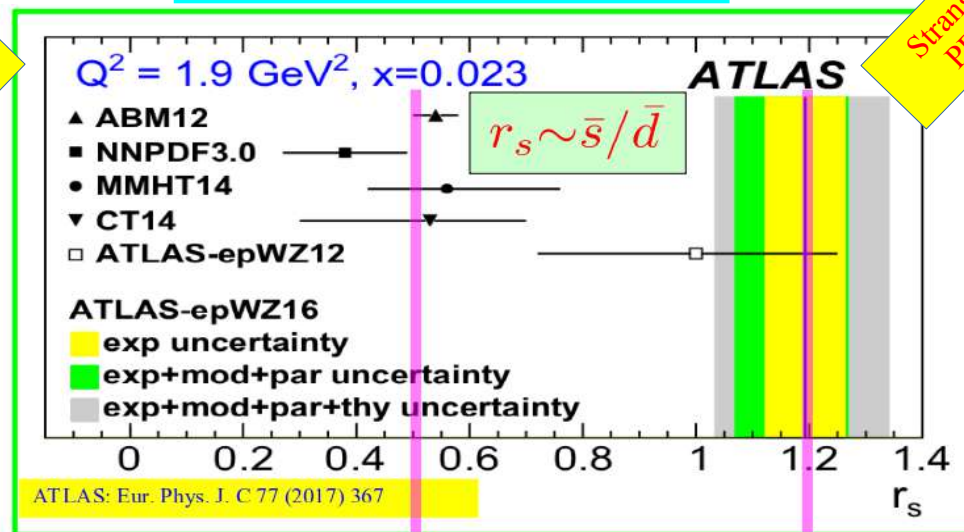
- New nPDF release: **nCTEQ26** combines the previous analyses:
 - ▶ **nCTEQ15** [[PRD 93, 085037 \(2016\)](#)]
 - ★ DIS NC data
 - ★ fixed-target DY data
 - ★ pion data from RHIC
 - ▶ **nCTEQ15WZ** [[EPJC 80, 968 \(2020\)](#)]
 - ★ LHC W/Z data
 - ★ constraints on *gluon* and *strange* nPDFs
 - ▶ **nCTEQ15HIX** [[PRD 103, 114015 \(2021\)](#); [Prog.Part.Nucl.Phys. 136 \(2024\) 104096](#)]
 - ★ JLAB DIS data
 - ★ constraints at high- x
 - ★ theoretical corrections: TMC, HT, deuteron
 - ▶ **nCTEQ15SIH** [[PRD 104 \(2021\) 9, 094005](#)]
 - ★ LHC & RHIC SIH data
 - ★ constraints on *gluon* nPDF
 - ▶ **nCTEQ15neutrino** [[PRD 106 \(2022\) 7, 074004](#)]
 - ★ DIS neutrino data (NuTeV, CHORUS, CDHSW, dimuons)
 - ★ compatibility of NC & CC DIS
 - ★ flavour separation
 - ▶ **nCTEQ15HQ** [[PRL 121, 052004 \(2018\)](#); [PRD 105 \(2022\) 11, 114043](#)]
 - ★ LHC & RHIC HF data
 - ★ constraints on low- x *gluon* nPDF
 - ★ PDF-reweighting + full analysis

nCTEQ15 ν



nCTEQ: arXiv: 2204.13157

nCTEQ15WZ

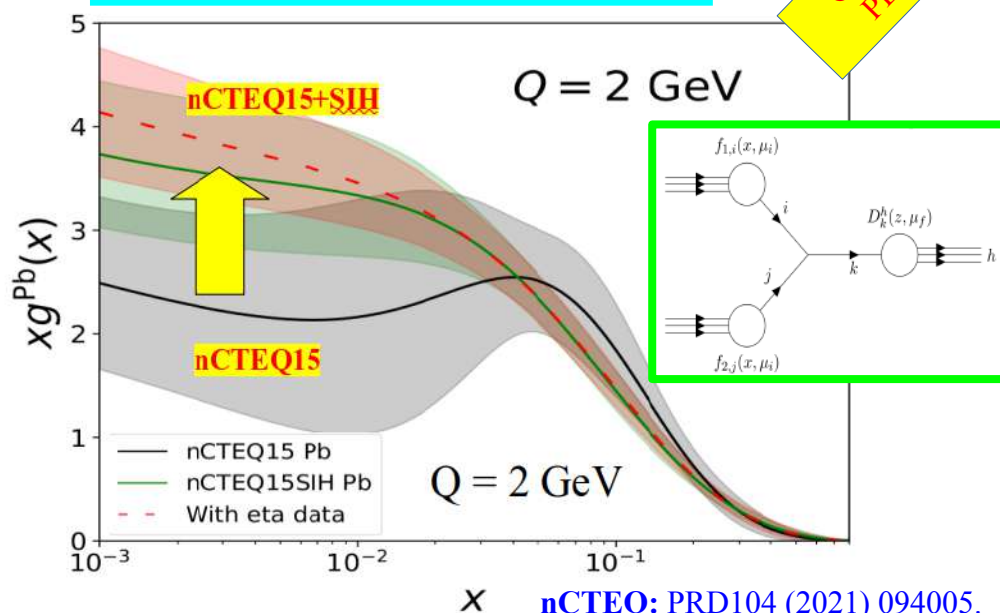


We expect:

At the LHC:

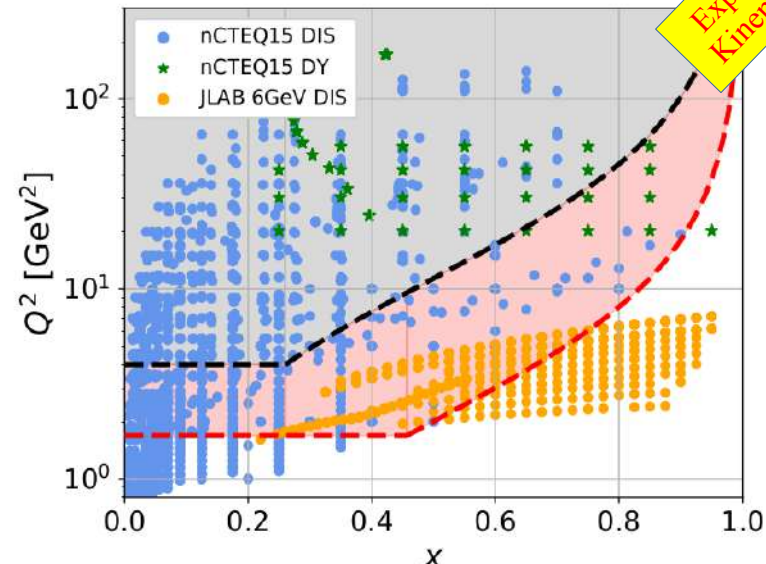
nCTEQ: Phys.Rev.D 104 (2021) 094005

nCTEQ15WZ+SIH



Key for
EIC

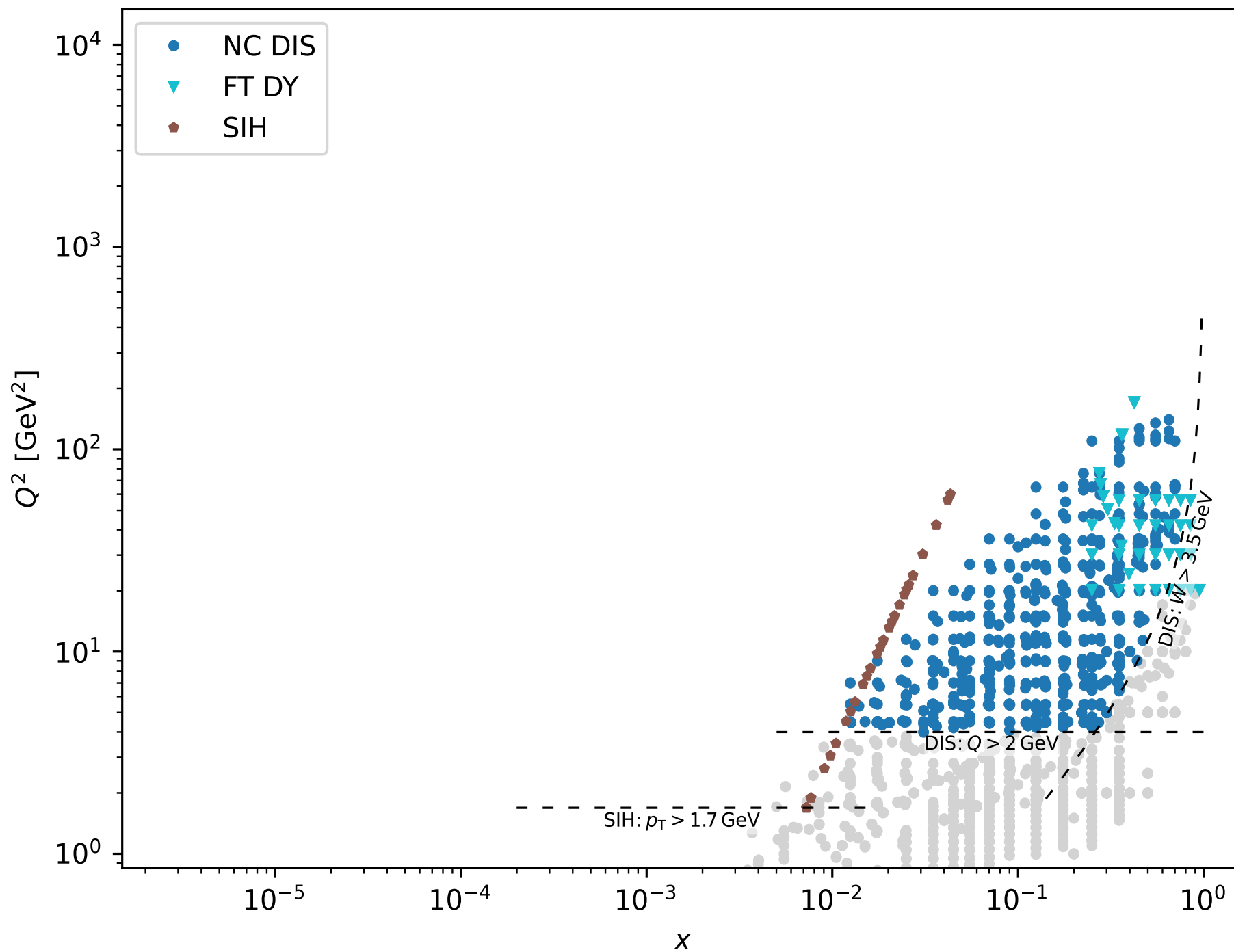
nCTEQ15HIX



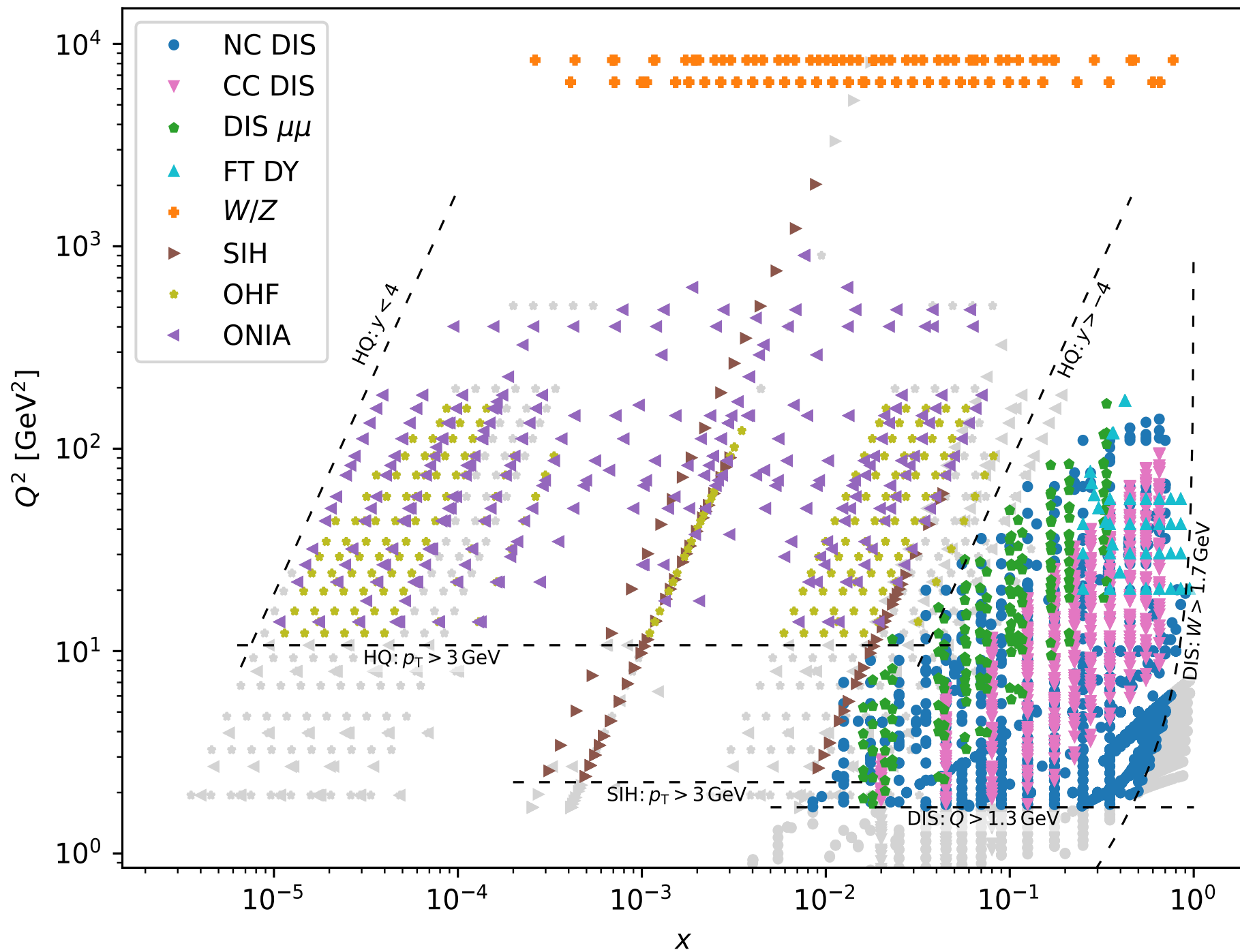
nCTEQ: Phys.Rev.D 103 (2021) 11, 114015

precision $f_A(x, Q)$ can serve as Boundary Condition for $f_A(x, Q, k_T, b_T, \sigma)$

nCTEQ15 ~700 data



nCTEQ26 ~3500 data



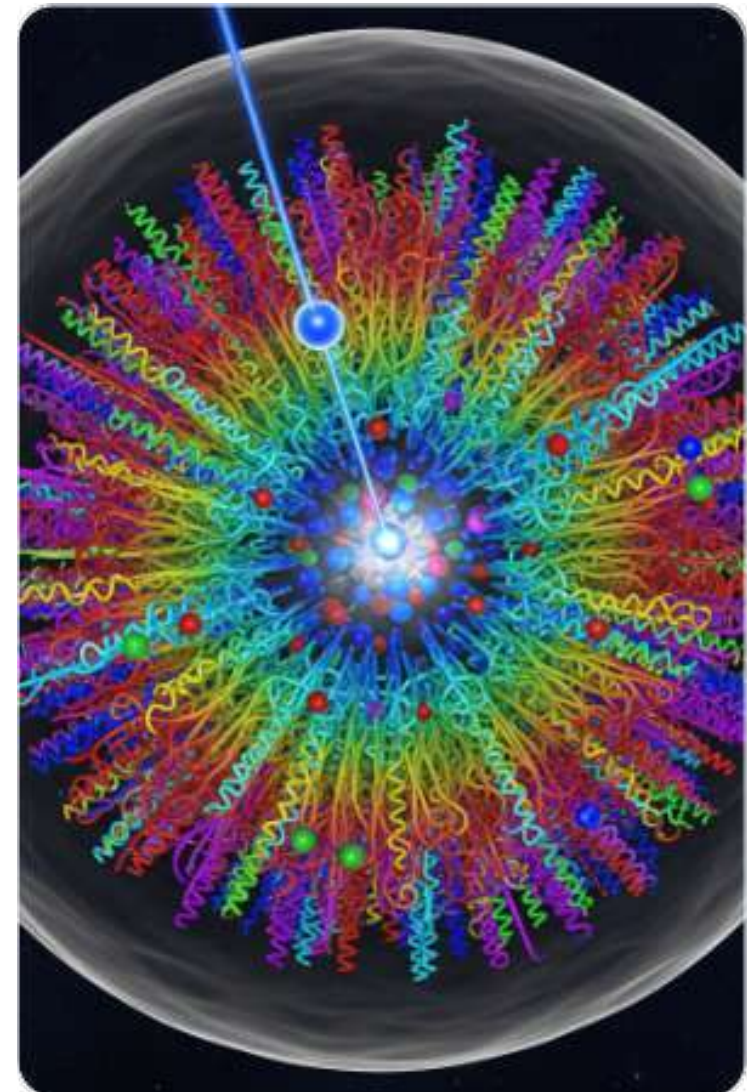
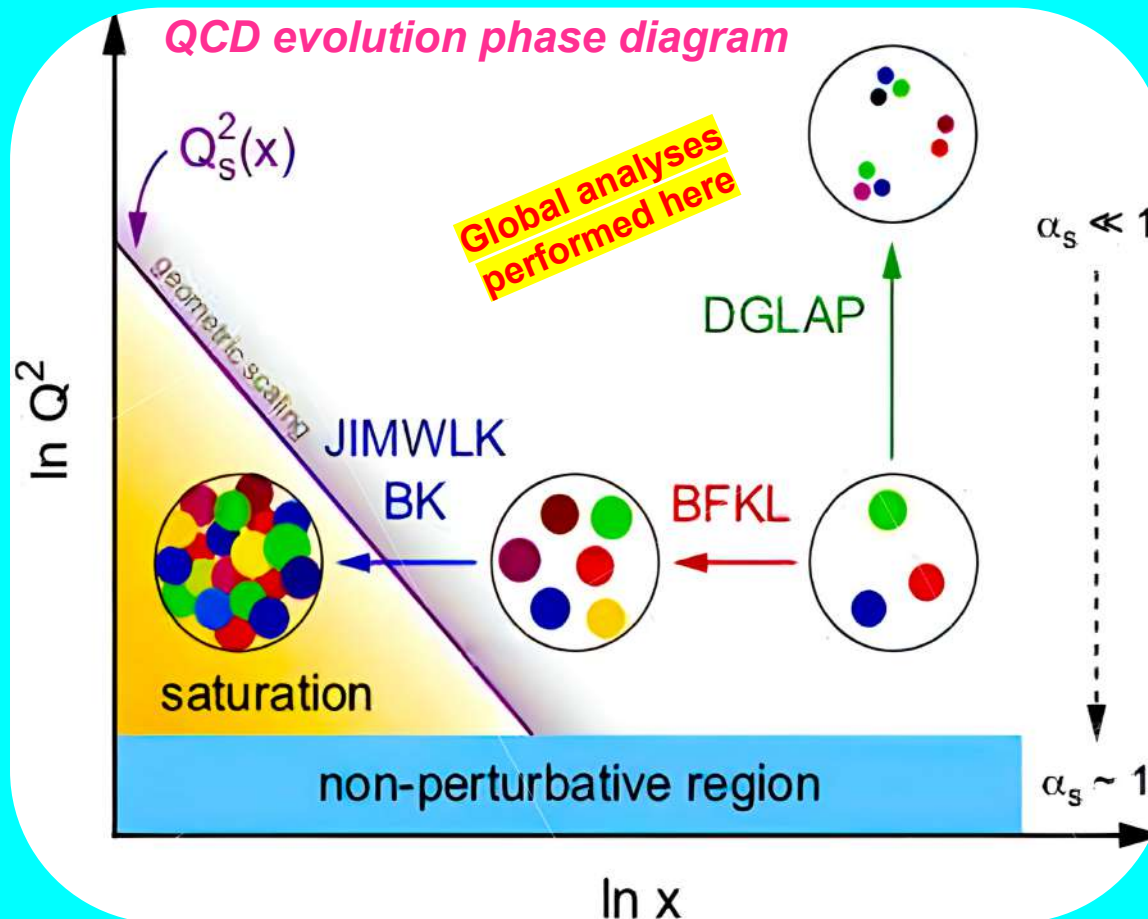
Precision nPDFs provide the essential foundation
for exploring the frontiers of QCD,
including the high-density gluon regime
where novel collective and non-perturbative phenomena
are expected to emerge.

... now let's explore the dense gluon regime

SURGE Topical Collaboration



Mission statement: Discover and explore the gluon saturation regime of quantum chromodynamics by advancing calculations to high precision and developing a comprehensive framework to compute observables and compare to a wide range of experimental data, including predictions for the Electron Ion Collider (EIC).



SURGE Collaboration

The Saturated Glue (SURGE) Collaboration is a Topical Collaboration in Nuclear Theory, funded by the US Department of Energy, Office of Science, Office of Nuclear Physics for the period 2023-2027.

<https://www.bnl.gov/physics/surge/>



The SURGE Collaboration aims at the discovery and exploration of the gluon saturation regime in quantum chromodynamics (QCD)

15



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GOAL: Sketch a work-flow for the global analysis framework.
The calculation must be FAST to be adaptable for a fitting loop

Initial state WG
Improve the initial conditions for evolution for unpolarized and polarized observables.

Spin WG
Analyze role saturation in the polarized observables. Elucidate the role of chiral anomaly in small x helicity evolution.

Global analysis WG
To establish saturation, perform comprehensive global analysis quantifying and minimizing uncertainties, extracting universal building blocks of high energy factorization.

Small x evolution + NLO calculations WG
Non-linear evolution at NLO and beyond, computation and implementation of impact factors

Final states WG Construct a framework for hadronization in a saturated environment, including development of MC generator based on CGC calculations

The SMU Team



Fred
Olness



Brandon
Stevenson
grad student



Rebecca
Preston
grad student



Junaid
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grad student

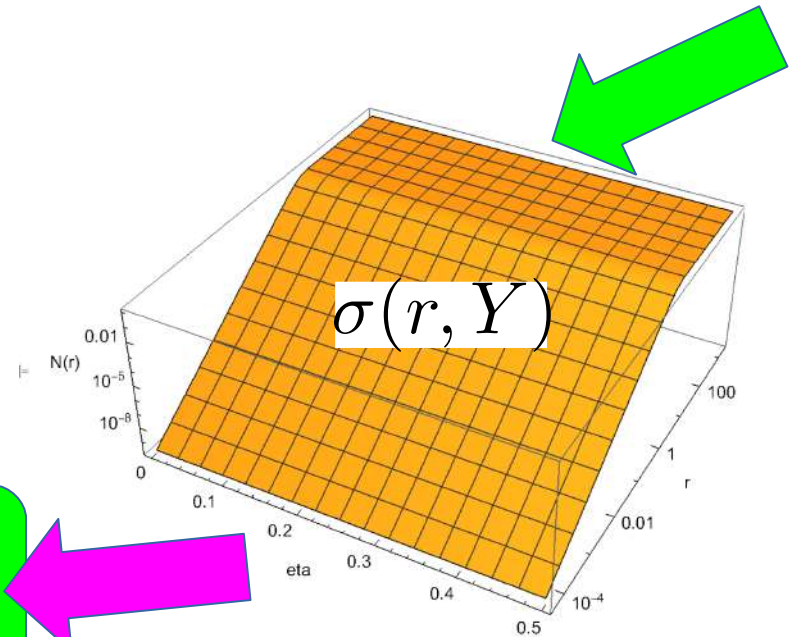
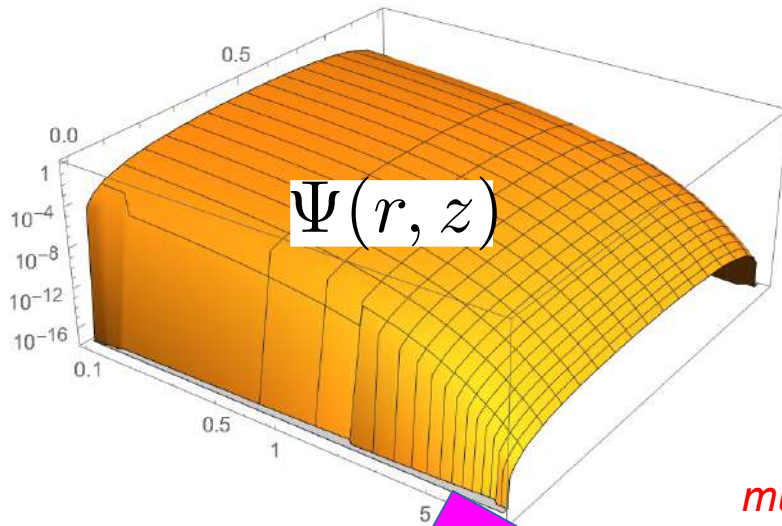


Peter
Risse
Postdoc

$$\sigma_{tot}^{\gamma^* A}(x, Q^2) = \int \frac{d^2 x_{\perp}}{4\pi} \int_0^1 \frac{dz}{z(1-z)} |\Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_{\perp}, z)|^2 \sigma_{tot}^{q\bar{q} A}(\vec{x}_{\perp}, Y).$$

Photon light-front
wave function

Dipole–nucleus
cross section



must be fast!!!

Convolution
2D Grid-based calc

$$\sigma_{tot}^{\gamma^* A}(x, Q^2)$$

... F_2 & F_L

$$\chi^2 = \frac{(D - T)^2}{\sigma^2}$$



$$\sigma_{tot}^{\gamma^* A}(x, Q^2) \simeq \int \int |\Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_\perp, z)|^2 \otimes \sigma_{tot}^{q\bar{q} A}(\vec{x}_\perp, Y)$$

Photon light-front wave function

$\Psi(\gamma^* \rightarrow q\bar{q})$

LO: Analytic functions

NLO: i) K-Factors

ii) Grid Methods

Fred has
experience

Peter has
experience

Short-cuts

Example:

LO

$$|\Psi_L^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_\perp, z)|^2 = 2N_c \sum_f \frac{\alpha_{EM} Z_f^2}{\pi} 4Q^2 z^3 (1-z)^3 [K_0(x_\perp a_f)]^2.$$

We can relate to usual
structure functions

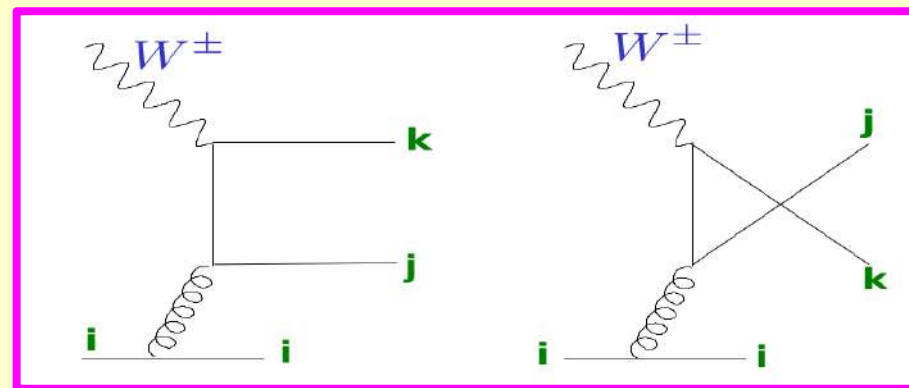
$$F_2(x, Q^2) = \frac{Q^2}{4\pi\alpha_{em}} \left(\sigma_T^{\gamma^* A} + \sigma_L^{\gamma^* A} \right),$$

$$F_L(x, Q^2) = \frac{Q^2}{4\pi\alpha_{em}} \sigma_L^{\gamma^* A}.$$

e.g., Extensible to Spin

Fast evaluation of heavy-quark contributions to DIS in APFEL++

P. RISSE^{a,†}, V. BERTONE^b, T. JEŽO^a, M. KLASSEN^a, K. KOVAŘÍK^a,
F.I. OLNES^c, I. SCHIENBEIN^d



APFEL++ – A PDF evolution library in c++

APFEL++

Bertone, arXiv:1708.00911

Available schemes in APFEL++

scheme	$\mathcal{O}(\alpha_s)$	NC: F_2	NC: F_3	NC: F_L	CC: F_2	CC: F_3	CC: F_L
ZM	N2LO	✓	✓	✓	✓	✓	✓
FONLL-C	N2LO	✓	✗	✓	✗	✗	✗
ACOT	NLO	✓	✓	✓	✗	✗	✗
sACOT- χ	NLO	✓	✓	✓	✓	✓	✓
approx. sACOT- χ	N2LO	✓	✓	✓	✓	✓	✓

Valerio Bertone



Peter Risse



$$\sigma_{tot}^{\gamma^* A}(x, Q^2) \simeq \int \int |\Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_\perp, z)|^2 \otimes \sigma_{tot}^{q\bar{q} A}(\vec{x}_\perp, Y)$$

Photon light-front wave function Dipole target scattering amplitude

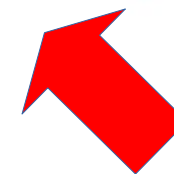
Balitsky-Kovchegov Equation

$$\frac{\partial N(\eta, r)}{\partial \eta} = \int d^2 \mathbf{r}_1 K(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) \left[N(\eta, r_1) + N(\eta, r_2) - N(\eta, r) - N(\eta, r_1)N(\eta, r_2) \right]$$

$$N(\eta, r) \equiv \sigma_{tot}^{q\bar{q} A}$$

$$\eta = Y = \ln(x_0, x)$$

the quadratic term includes the nonlinear saturation effects that tame the growth of gluon densities at small x



Feature 	BFKL	BK	JIMWLK
Type	Linear	Non-linear (Dipole)	Non-linear (Functional)
Physics	Gluon emission	Emission + Recombination	Full CGC Color Fields
Limit	Dilute ($x \sim 10^{-2}$)	Large N_c Saturation	General Saturation
Complexity	Simple	Moderate	Very High

There are primarily four dipole amplitude models:

<u>MV$^\gamma$ Model</u> $x = \frac{(r^2 Q_{s0}^2)^\gamma}{4} \ln \left(\frac{1}{r \Lambda_{\text{QCD}}} + e \right)$ $N^{\text{MV}^\gamma}(r) = \begin{cases} 1 - \exp(-x), & x > 10^{-6} \\ x, & \text{otherwise} \end{cases}$	<u>rcMV$^\gamma$ Model</u> $x = \frac{r^2 Q_{s0}^2}{4} \cdot \alpha_s(r) \cdot \frac{N_c}{\pi} \left(1 + \ln \left(\frac{\alpha_s^{\text{freeze}}}{\alpha_s(r)} \right) \right)$ $N^{\text{rcMV}}(r) = \begin{cases} [1 - \exp(-x^\gamma)]^{1/\gamma}, & x > 10^{-4} \\ x, & \text{otherwise} \end{cases}$
<u>GBW Model</u> $N^{\text{GBW}}(r) = 1 - \exp \left(-\frac{r^2 Q_{s0}^2}{4} \right)$	<u>GBW$^\gamma$ Model</u> $x = \left(\frac{r^2 Q_{s0}^2}{4} \right)^\gamma$ $N_0^{\text{GBW}^\gamma}(r) = \begin{cases} [1 - \exp(-x)]^{1/\gamma}, & \frac{r^2 Q_{s0}^2}{4} > 10^{-4} \\ \frac{r^2 Q_{s0}^2}{4}, & \text{otherwise} \end{cases}$

Running coupling constant :

Golec-Biernat–Wusthöff (GBW)
McLerran-Venugopalan (MV) ,

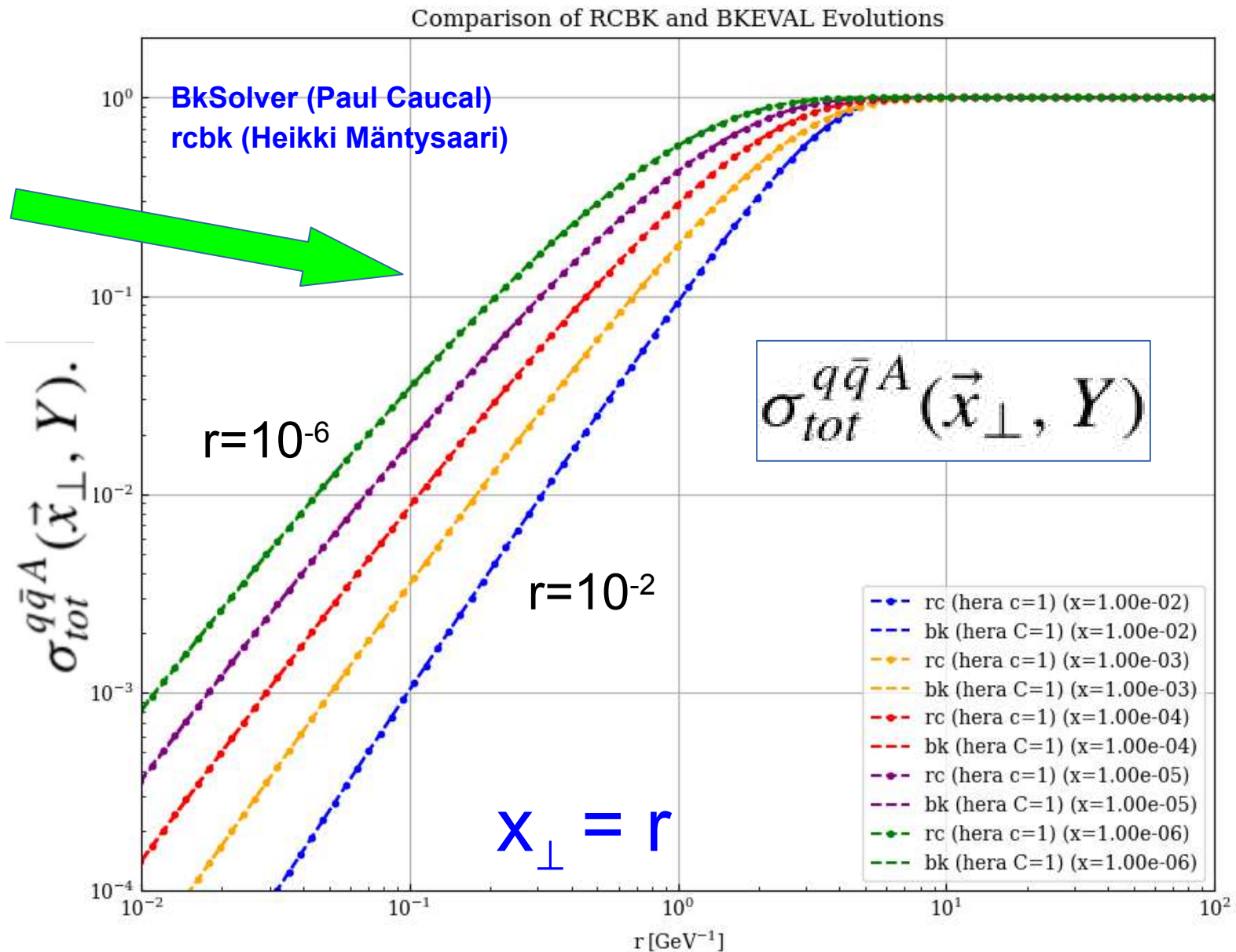
$$\alpha_s = \frac{12\pi}{(33.0 - 2.0N_f) \log \left[\left(\mu_0^{\frac{1}{c}} + \left(\frac{4C^2}{\Lambda_{\text{QCD}}^2 r^2} \right)^{\frac{1}{c}} \right)^c \right]}$$

Parameter	bkEval	rcBK	Description
Initial Condition	MV^γ	MV^γ	Dipole amplitude initial model
Evolution Type	Balitsky	Balitsky	BK equation solver type
Model Parameters			
Q_{s0}^2	$Q_{s0} = 0.4062019 \text{ GeV}$	$Q_{s0}^2 = 0.165 \text{ GeV}^2$	Initial saturation scale
γ	1.135	1.135	Anomalous dimension in MV^γ model
α_s	Evolving with r	Evolving with r	Strong coupling constant
α_s^{freeze}	0.762	0.762	Freeze value to limit $\alpha_s(r)$ in the IR region
Λ_{QCD}	0.241 GeV	0.241 GeV	QCD scale parameter
C or C^2	$C = 2.51992$	$C^2 = 6.35$	Coefficient in running coupling formula
e_c	1	1	Smoothing constant in running coupling equation
Grid Parameters			
Grid Points	$N_u = 421, N_\theta = 21$	150 (step factor 1.10305)	Grid discretization for dipole sizes
Dipole Size Range	$u = \log(r) \in [-10, 4.605]$	$r \in [4.5 \times 10^{-5}, 100]$	Range of dipole size (log-scale for bkEval, linear for rcBK)
Rapidity Range	$\eta_f = 15.0, N_\eta = 150$	$y \in [0, 15], \text{step } 0.1$	Rapidity evolution range

TABLE I. Comparison of parameters used in `bkEval` and `rcBK` codes with MV^γ initial condition.

Two sets of
lines per
color

Excellent
agreement



Cross Check: We see we have good agreement across all x values for two different data generators, the RCBK code and BKeval code with all internal settings matching.

Machine Learning Models

- **Need fast evolution** *(the WHY)*
- Could optimize a program, but ...
 - BFKL, BK, JIMWLK
 - LO, NLO, ...
- **Try Machine Learning** *(the HOW)*
 - Fast, flexible
 - Improved over interpolation

Sample data files:

LHC: ATLAS, CMS, LHCb

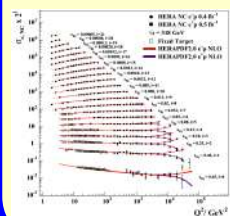
Tevatron: CDF, D0

HERA: H1, ZEUS, Combined

Fixed Target: ...

User Supplied: ...

Experimental Data



Data: HERA, Tevatron, LHC,
fixed target experiments

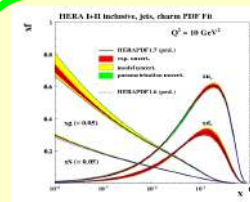
Processes:

Inclusive DIS, Jets, Drell-Yan,
Diffraction, Top production
W and Z production

Theory Calculations

HQ Schemes: MSTW, NNPDF, ABM, ACOT
Jets, W, Z: FastNLO, ApplGrid
Top: Hathor
Evolution: QCDNUM, APFEL, k_T
Other: NNPDF reweighting
TMDs, Dipole Model, ...

xFitter



Parton Distribution
Functions:
PDF, Updf, TMD

$\alpha_s(M_Z)$, m_c, m_b, m_t ...

Theoretical
Cross Sections

Comparisons
to other PDFs
(LHAPDF)



extensions include
nuclear PDFs

Features & Recent Updates:

NNLO DGLAP

Photon PDF & **QED**

Pole & MS-bar masses

Profiling and Re-Weighting

BFKL interface

Heavy Quark Variable Threshold
Improvements in χ^2 and correlations

TMD PDFs (uPDFs)

... and many other

xFitter 2.2.0
Future Freeze

xFitter Collaboration



xFitter Collaboration Meeting
February 2020, DESY



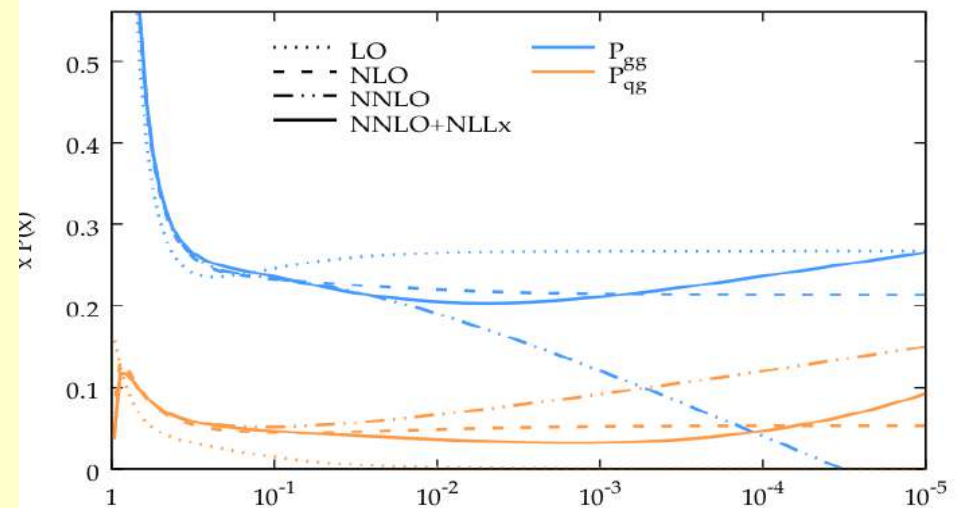
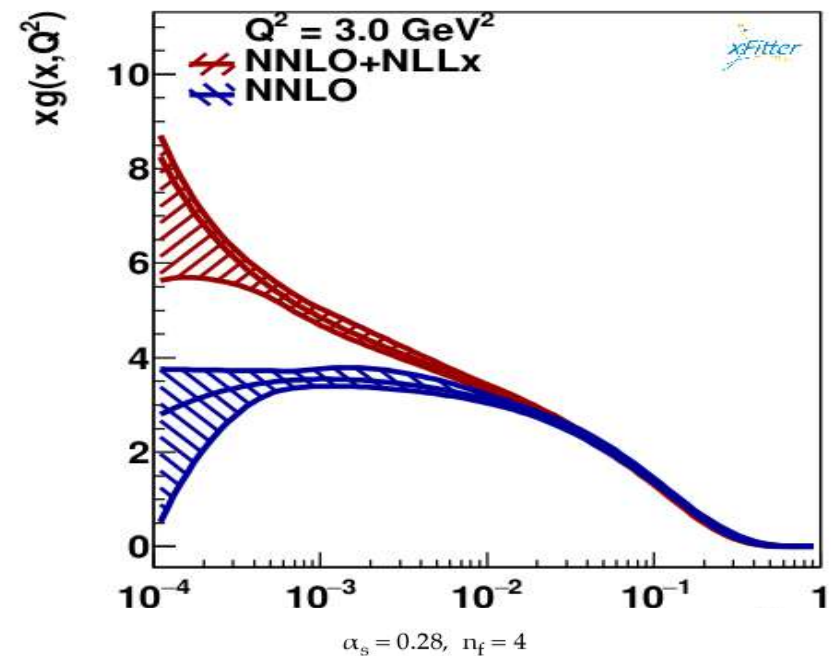
xsect_dipole_proton.c

```
#include <math.h>
#include "xsect_dipole_proton.h"

////////////////////////////////////
// Parametrisation of the dipole-proton cross-section //
// as obtained from high-energy QCD with saturation //
////////////////////////////////////
// This file contains two version of the cross-section //
// The first one is the original from //
// [1] E. Iancu, K. Itakura and S. Munier, //
// Phys.Lett.B590:199-208,2004 [hep-ph/0310338] //
// which includes only light quarks. //
// The second is from //
// [2] G. Soyez, in preparation //
// which also accounts for heavy quarks. //
// They both implement eq. (8) of Ref. 1 or eq. (3) of //
// Ref. 2. Only the parameters of the fit vary. //
// //
// - Arguments: //
//   r : dipole size //
//   Y : rapidity (Y=log(1/x)) //
// - Returned value: //
//   the dipole-proton cross-section (in GeV^{-2}) //
// //
// Additional remarks: //
// - The quark masses are //
//   m_{u,d,s}=140 MeV, m_c=1.4 GeV and m_b=4.5 GeV //
// - When the heavy quarks are considered (2nd model), //
//   the x value for their contribution has to be //
//   shifted to x(1+4 m^2/Q^2) //
////////////////////////////////////
```

Impact of low- x resummation on QCD analysis of HERA data

xFitter Developers' team: Hamed Abdolmaleki¹, Valerio Bertone^{2,3}, Daniel Britzger⁴, Stefano Camarda⁵, Amanda Cooper-Sarkar⁶, Francesco Giuliani⁶, Alexander Glazov⁷, Aleksander Kusina⁸, Agnieszka Luszczak^{7,9}, Fred Olness¹⁰, Andrey Sapronov¹¹, Pavel Shvydkin¹¹, Katarzyna Wichmann⁷, Oleksandr Zenaiev⁷ and Marco Bonvini¹²



Machine Learning Models

- **Need fast evolution** *(the WHY)*
- Could optimize a program, but ...
 - BFKL, BK, JIMWLK
 - LO, NLO, ...
- **Try Machine Learning** *(the HOW)*
 - Fast, flexible
 - Improved over interpolation

1) MLP (Multi-Layer Perceptron) Model



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Khan

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Neural Network Setup

- Input features: **x, r, C, Qs0, γ**
- Input model: **McLerran-Venugopalan**
- Target: **N(x,r)** dipole cross section
- Architecture: 3 hidden layers (64, 64, 32 neurons) with ReLU activation
- Output layer: Linear

Training Details

- Optimizer: **AdamW**
 - AdamW adaptively adjusts the learning rate for each parameter based on estimates of the first and second moments of the gradients. This allows for faster convergence and can handle sparse gradients effectively.

- Learning rate: **Exponentially decaying**

- Loss function: **Custom** (scaled MSE: Mean Absolute Error.)

Dataset split: **80/10/10** (train/validation/test)

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N \left(y_i^{\text{pred}} - y_i^{\text{true}} \right)^2$$

$$L = \frac{1}{N} \sum_{i=1}^N \frac{\text{MSE}}{(0.01 y_i^{\text{true}} + \varepsilon)^2}$$

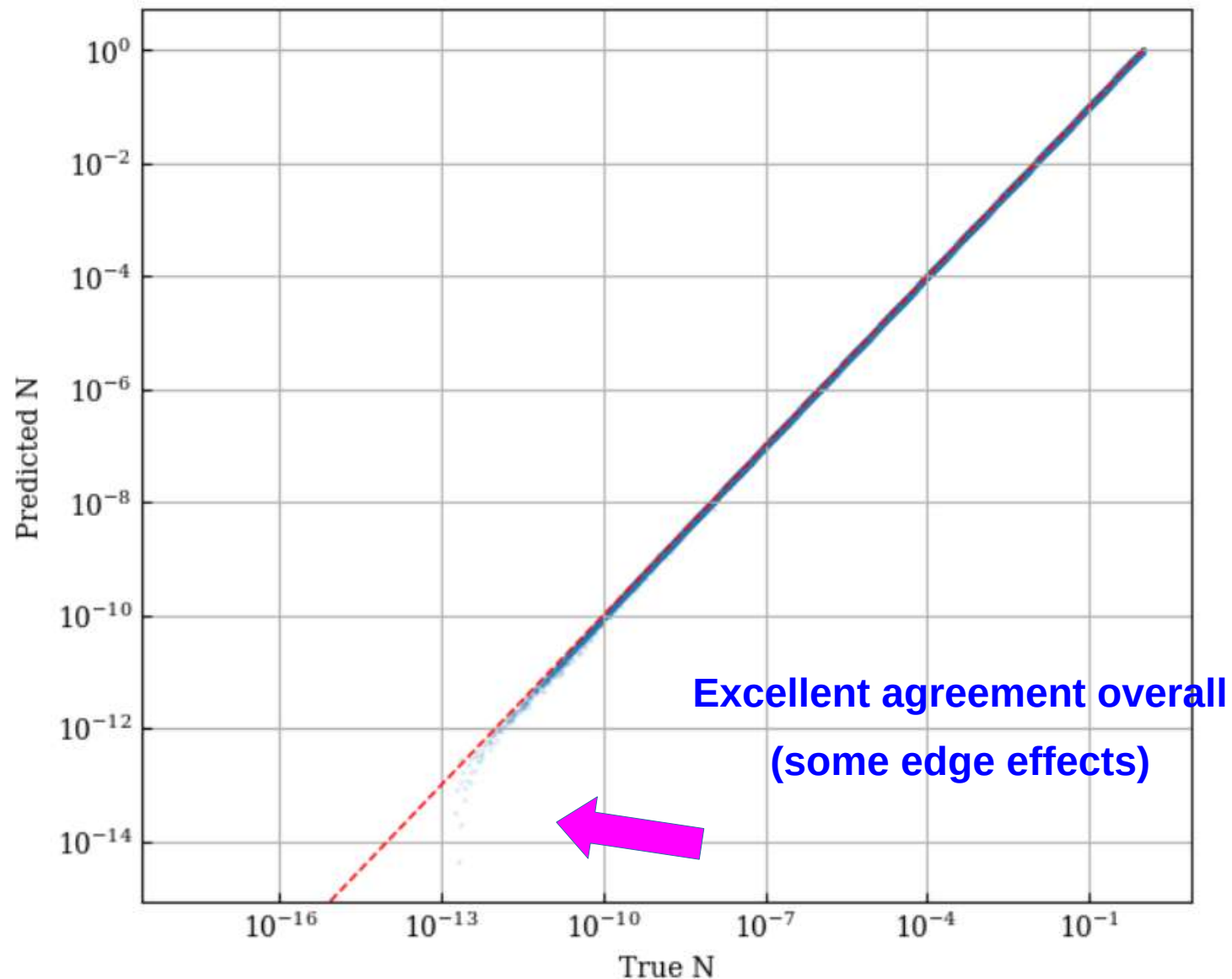
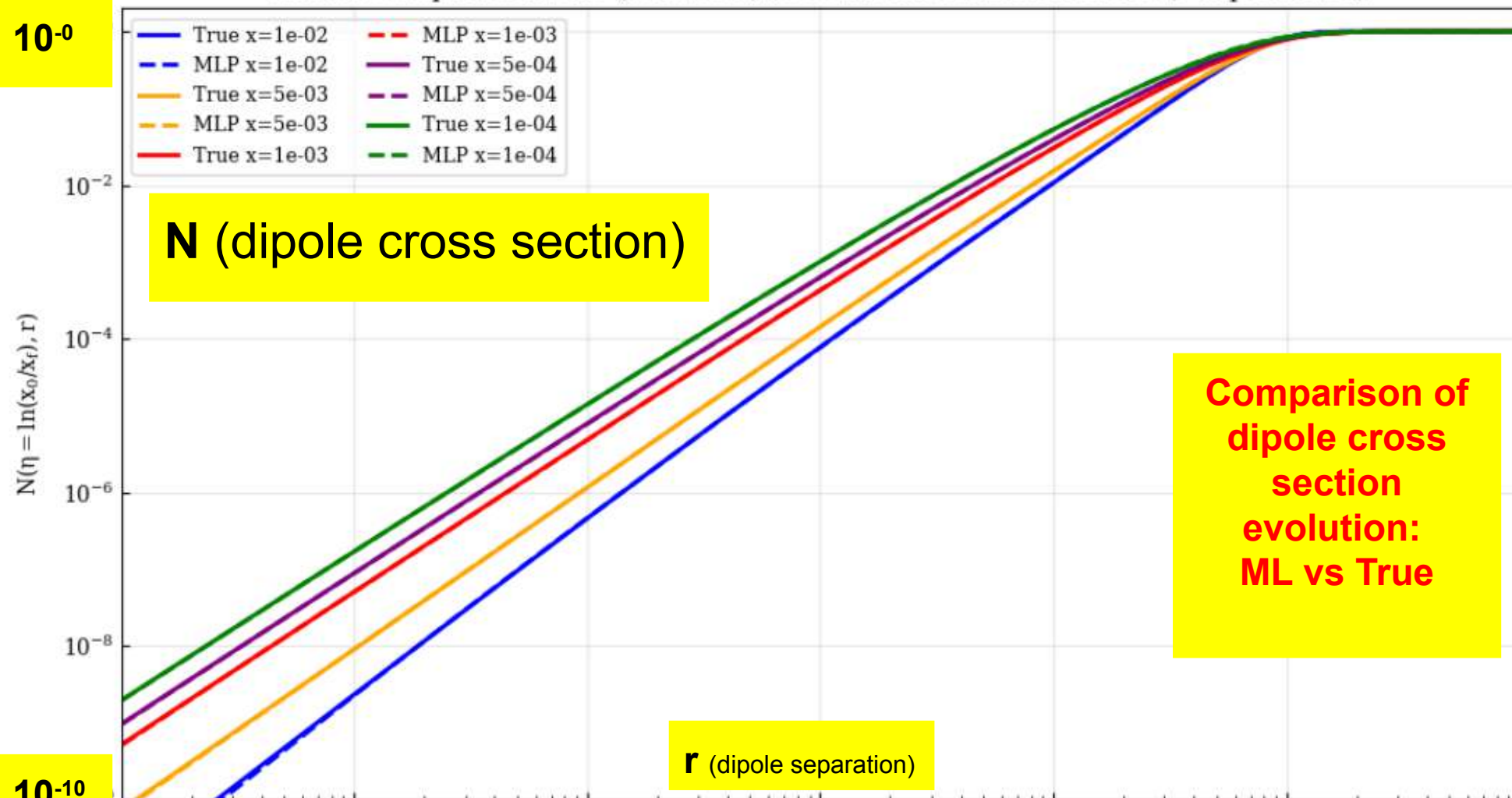
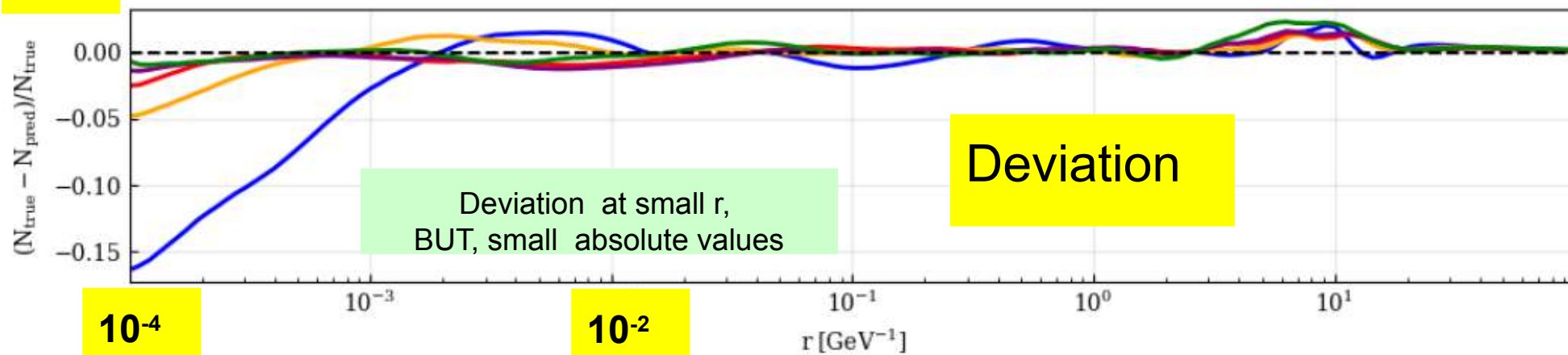


FIG. 1. True vs. predicted N values from the MLP on the test set. The dashed red line indicates perfect agreement.

bkEval Comparison: MLP (MAE loss) vs Truth and Fractional Error (r-dependence)

 10^{-0}  10^{-10}  10^{-4} 10^{-2} 10^{-1} 10^0 10^1

2) DeepONet

DeepONet attempts to learn non-linear operators accurately. Many applications to physics.

“**DeepONet**: Learning nonlinear operators for identifying differential equations based on the universal approximation theorem of operators” <https://arxiv.org/pdf/1910.03193>



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Two sub-networks a branch and trunk. Branch and Trunk network can be any network, MLP (dense connection) chosen for simplicity. Trunk network also uses a simple fourier features layer to give access to high dimensional information.

DeepONet

With test dataset, Varying **C** and **QS0** and 11,998,500 data points:

Training time: ~1 hour, 100 epochs

Size of keras model save: 11mb

Inference time: less than 1 second for full grid

DeepONet

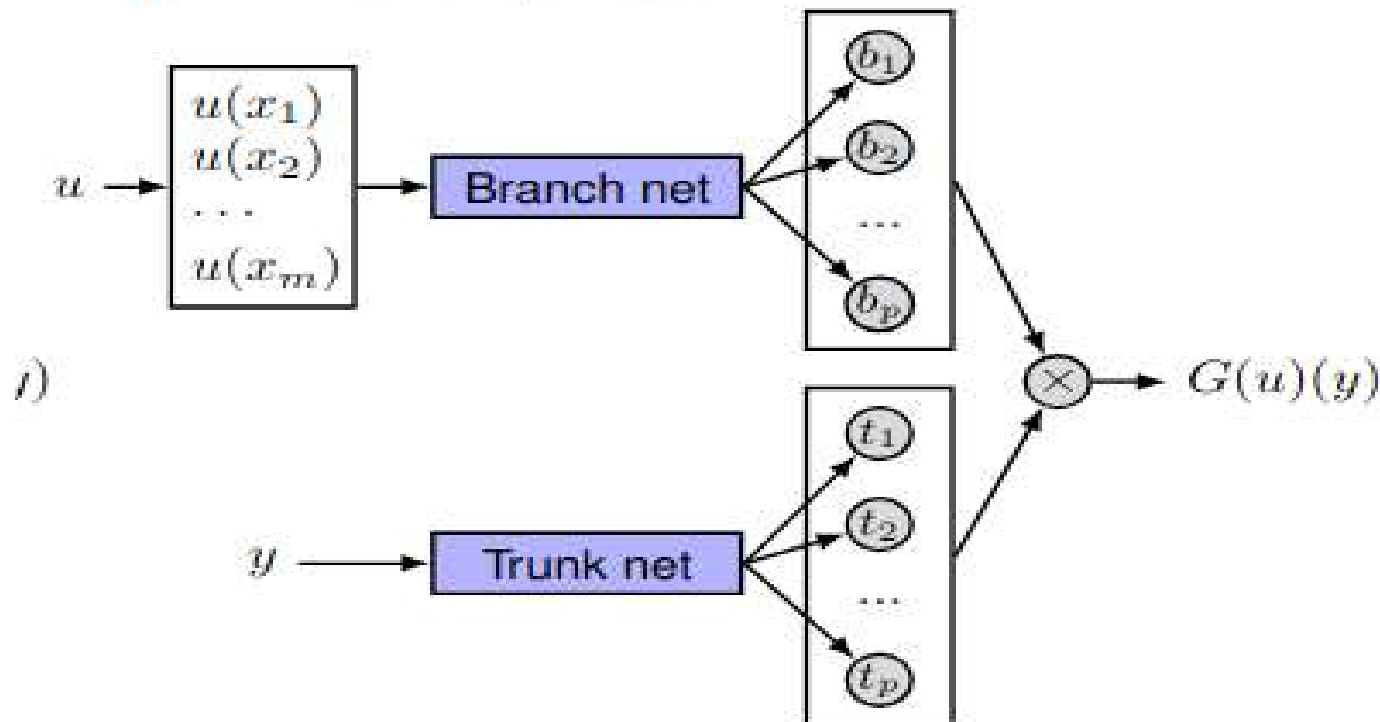
Theorem 1 (Universal Approximation Theorem for Operator). Suppose that σ is a continuous non-polynomial function, X is a Banach Space, $K_1 \subset X$, $K_2 \subset \mathbb{R}^d$ are two compact sets in X and $\mathbb{R}^d$, respectively, V is a compact set in $C(K_1)$, G is a nonlinear continuous operator, which maps V into $C(K_2)$. Then for any $\epsilon > 0$, there are positive integers n, p, m , constants $c_i^k, \xi_{ij}^k, \theta_i^k, \zeta_k \in \mathbb{R}$, $w_k \in \mathbb{R}^d$, $x_j \in K_1$, $i = 1, \dots, n, k = 1, \dots, p, j = 1, \dots, m$, such that

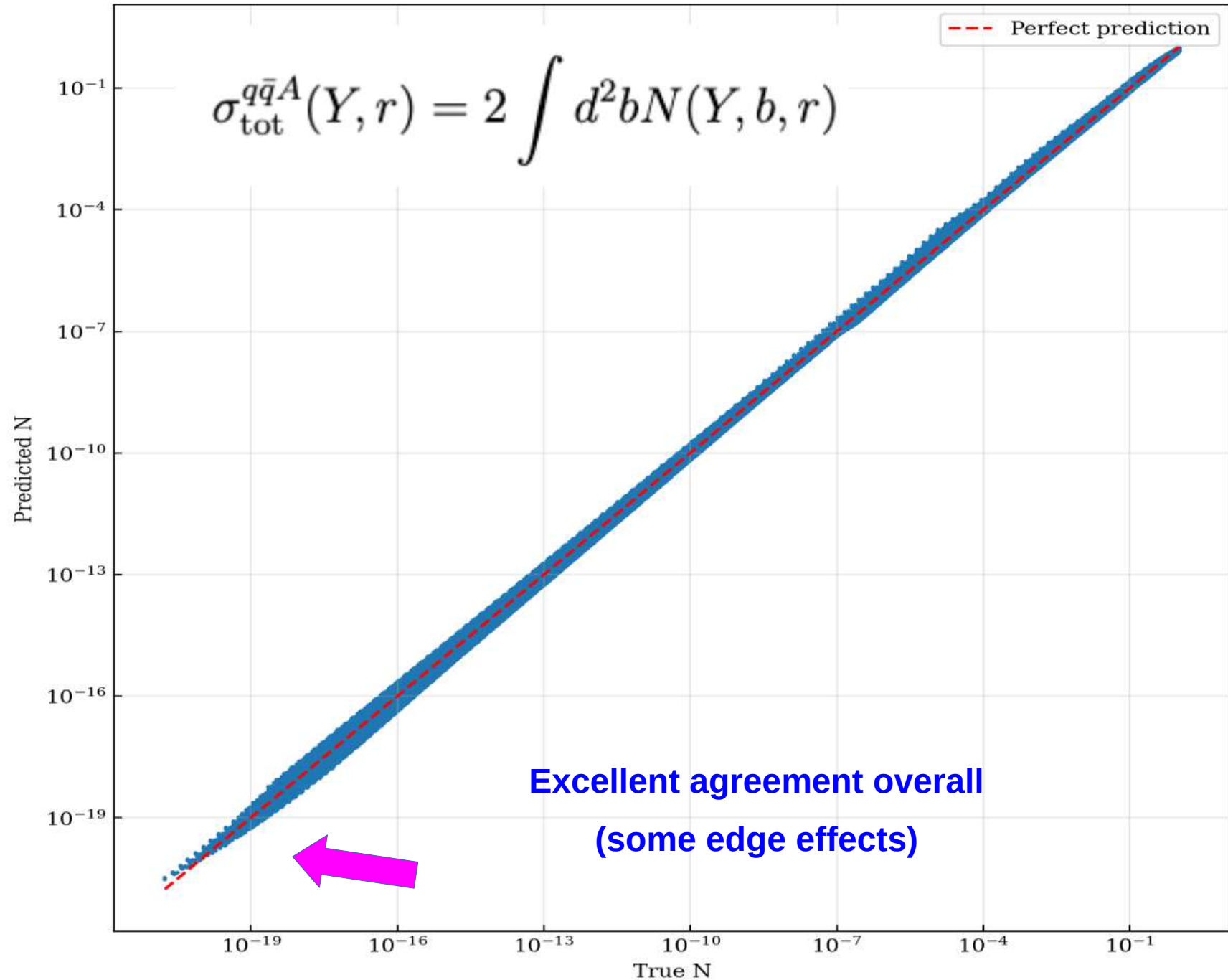
We learn G

$$\left| G(u)(y) - \underbrace{\sum_{k=1}^p \sum_{i=1}^n c_i^k \sigma \left(\sum_{j=1}^m \xi_{ij}^k u(x_j) + \theta_i^k \right)}_{\text{branch}} \underbrace{\sigma(w_k \cdot y + \zeta_k)}_{\text{trunk}} \right| < \epsilon \quad (1)$$

holds for all $u \in V$ and $y \in K_2$.

D Unstacked DeepONet





Best DeepONet: N vs r
 $\gamma=1.074$, $C=2.789$, $Qs0=0.1368$

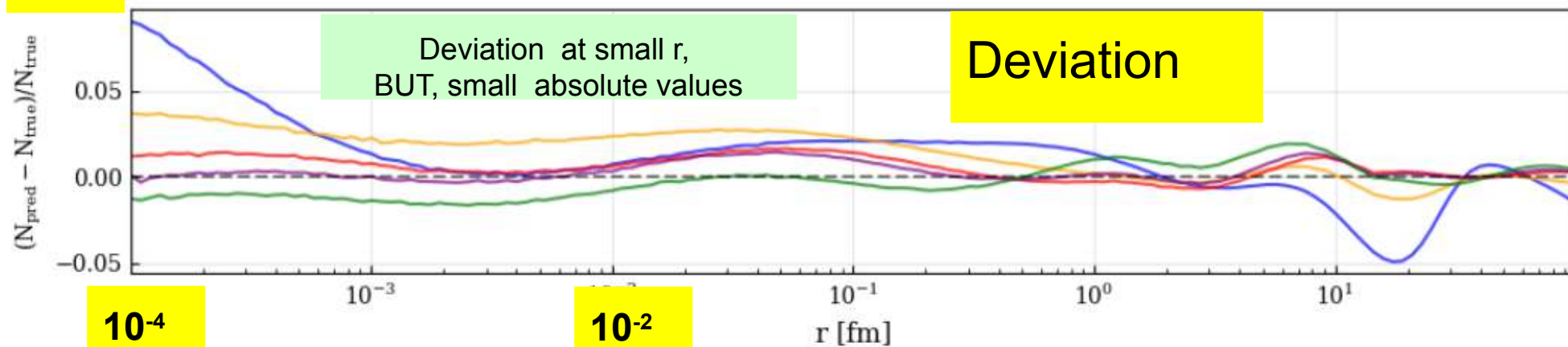
10^{-0}

N (dipole cross section)

**Comparison of
dipole cross
section
evolution:
ML vs True**

r (dipole separation)

10^{-10}



3) Convolutional Neural Network (CNN)



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Khan



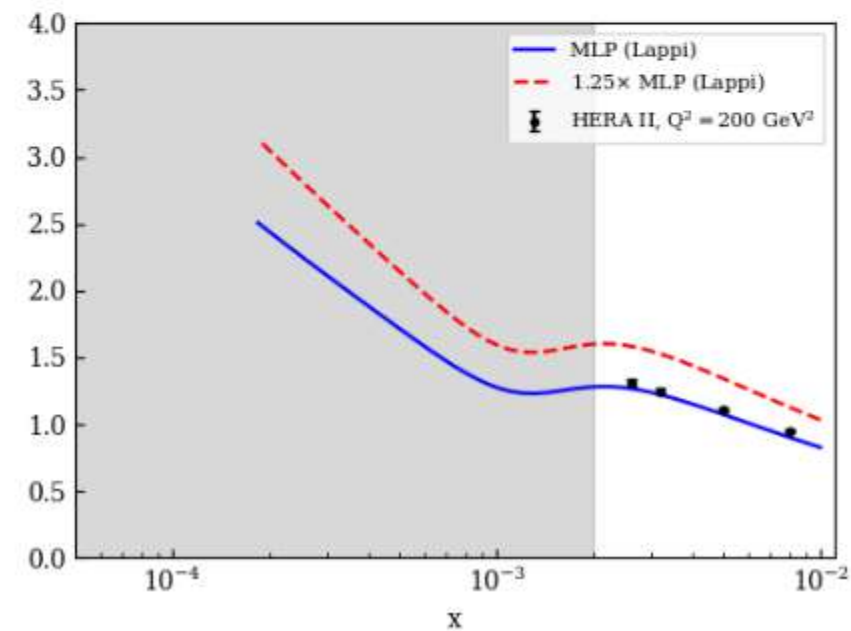
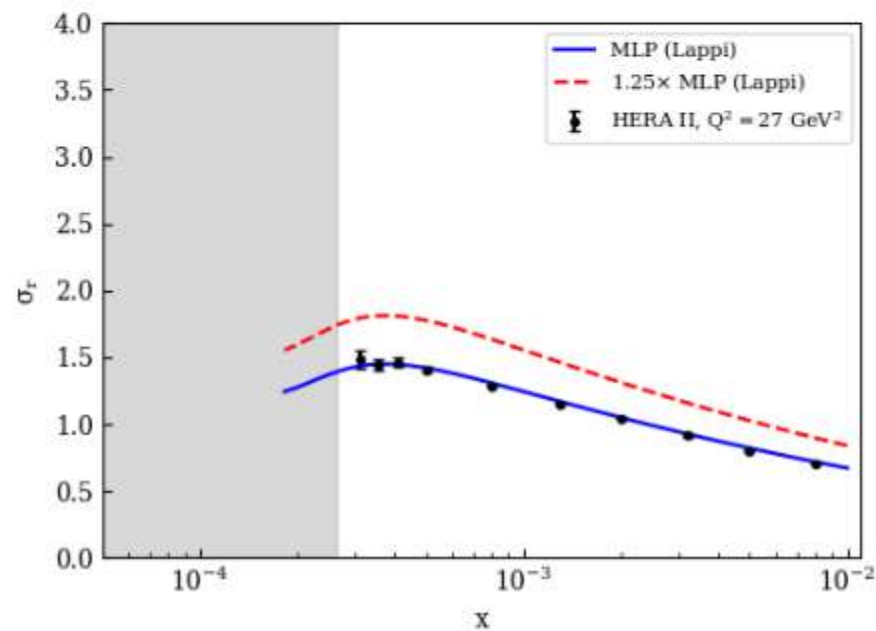
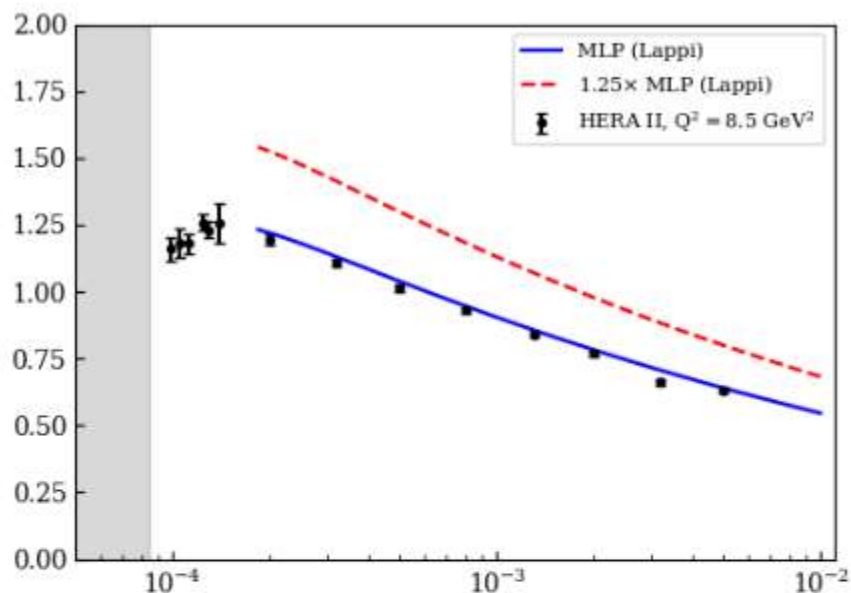
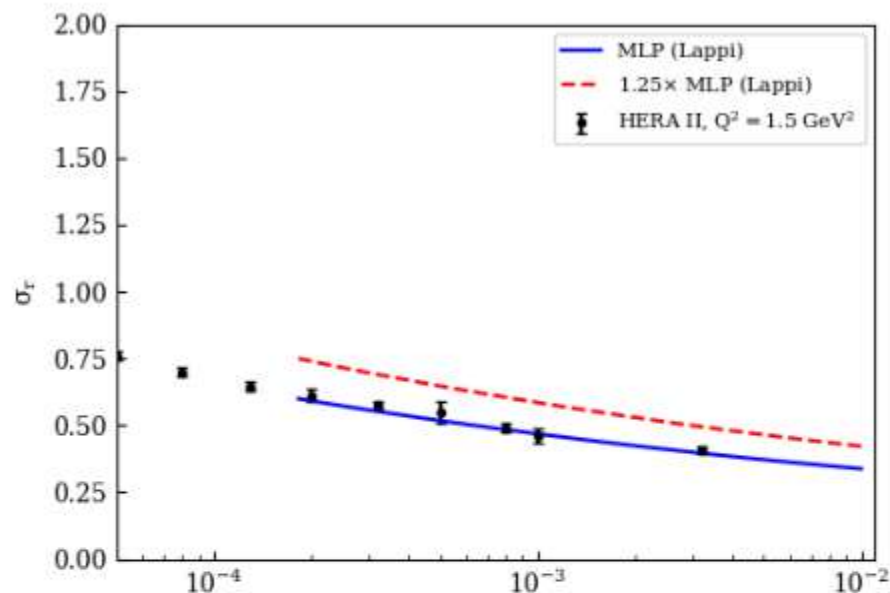
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... in progress ...

Does it work?

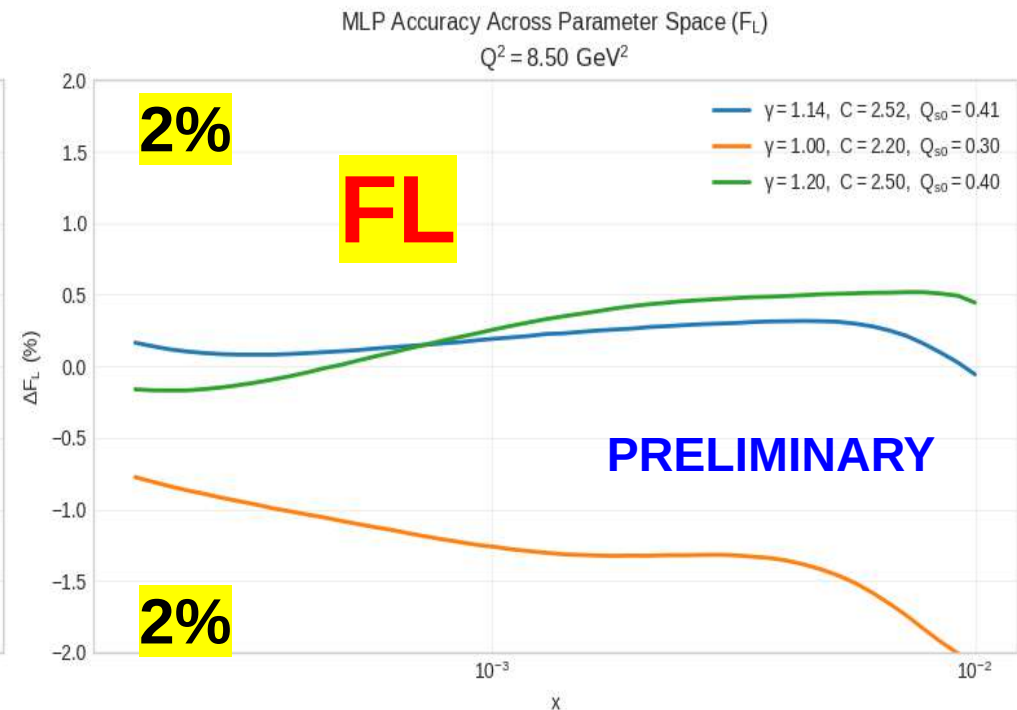
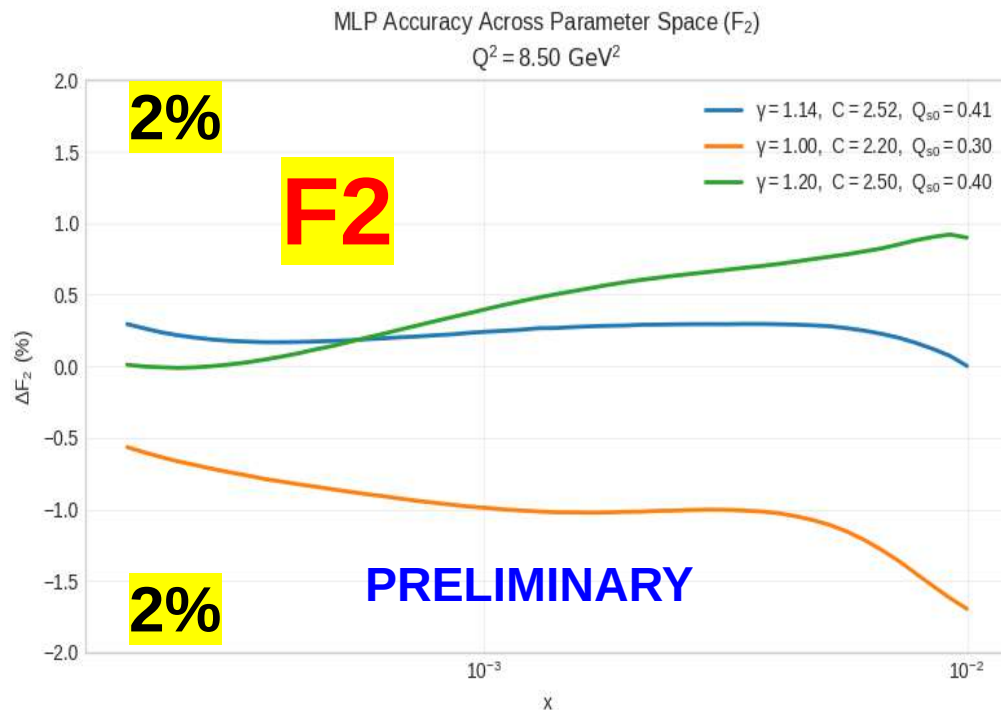
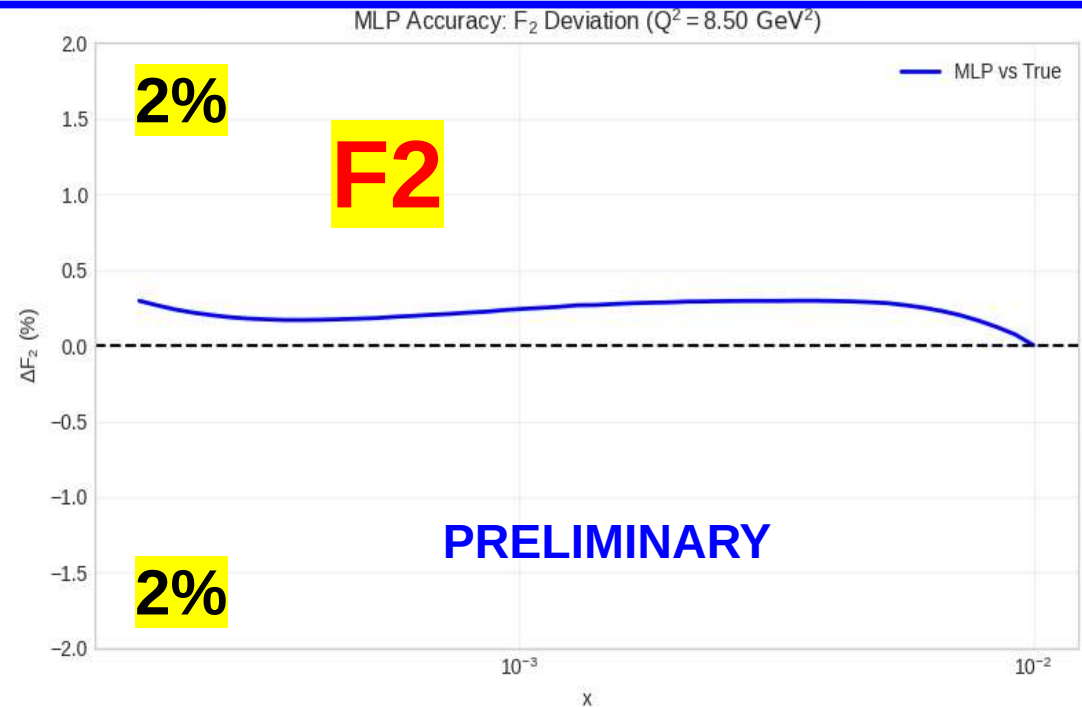
What are the uncertainties?

HERA II vs MLP

Lappi: $\gamma = 1.1350$, $C^2 = 6.35$, $Q_{s0}^2 = 0.165$, $\sigma_0 = 84.5 \text{ GeV}^{-2}$ Original $\sigma_0 = 32.9 \text{ mb}$; light quarks only; also showing $1.25\times$ MLP (Lappi)

Uncertainties: ML vs. True

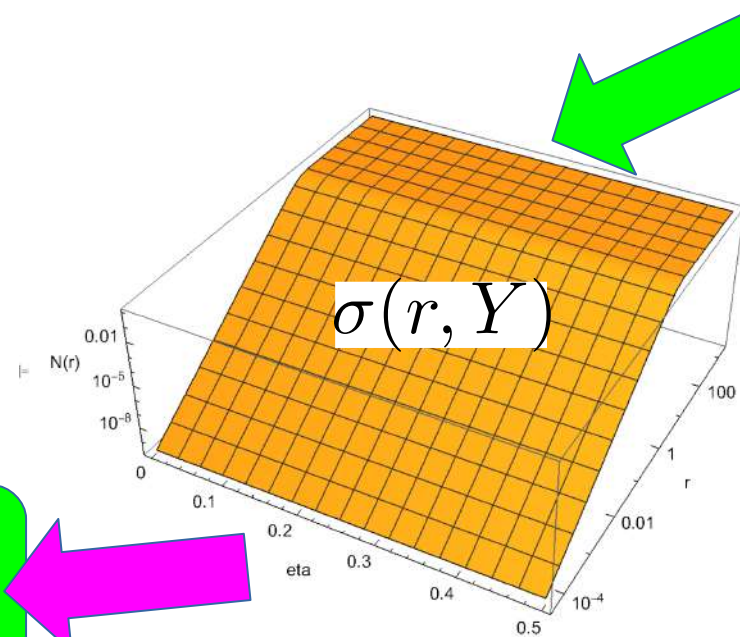
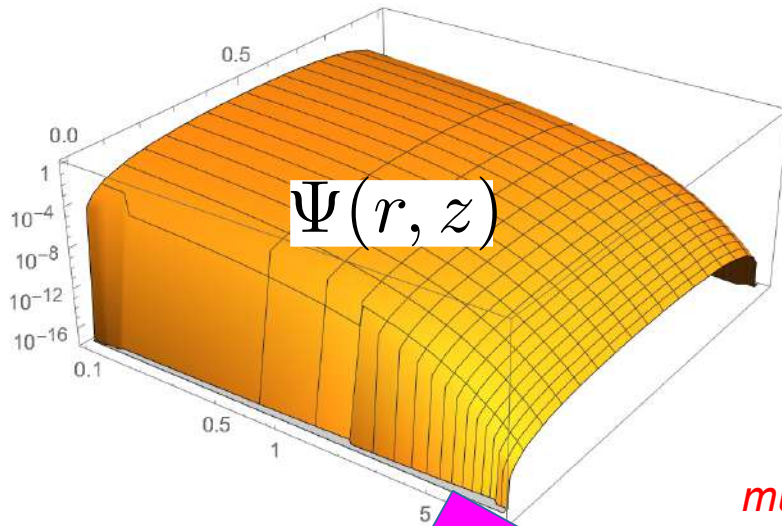
Preliminary uncertainties appear to be satisfactory given typical theoretical and experimental uncertainties



$$\sigma_{tot}^{\gamma^* A}(x, Q^2) = \int \frac{d^2 x_{\perp}}{4\pi} \int_0^1 \frac{dz}{z(1-z)} |\Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_{\perp}, z)|^2 \sigma_{tot}^{q\bar{q} A}(\vec{x}_{\perp}, Y).$$

Photon light-front
wave function

Dipole–nucleus
cross section



must be fast!!!

Convolution
2D Grid-based calc

$$\sigma_{tot}^{\gamma^* A}(x, Q^2)$$

... F_2 & F_L

$$\chi^2 = \frac{(D - T)^2}{\sigma^2}$$



QUARK-GLUON DYNAMICS IN THE NUCLEAR MEDIUM

9 - 13 November 2026

ECT* - Villa Tambosi, Villazzano

This workshop will bring together experimentalists and theorists to discuss recent progress and open questions in understanding how quark and gluon dynamics are modified in the nuclear environment. The workshop aims to foster focused discussion across subfields and to identify key directions for future measurements and theoretical work.

Topics will cover related developments in theory, phenomenology, and experiment in the areas of gluonic components in nuclei, hadronization, partonic structure, nuclear medium effects, short-range correlations, 3D nucleon/nuclear structure, vector mesons, hypernuclei, and connections to the future electron ion collider.

ORGANIZERS

Holly **Szumila-Vance**, Florida International University
Cynthia **Keppel**, 3q Scientific Consulting
Fredrick **Olness**, Southern Methodist University
Matteo **Rinaldi**, INFN Perugia
Misak **Sargsian**, Florida International University

ECT* Director: Prof. Ubirajara van Kolck

The ECT* is part of the Fondazione Bruno Kessler. The Centre is funded by the Autonomous Province of Trento, funding agencies of EU Member and Associated states, and by INFN-TIFPA and has the support of the Department of Physics of the University of Trento.

For the organization please contact: Barbara Gazzoli - ECT* Secretariat - Villa Tambosi - Strada delle Tabarelle 286 | 38123 Villazzano (Trento) - Italy
Tel.: (+39-0461) 314763, E-mail: gazzoli@ectstar.eu or visit <http://www.ectstar.eu>



QUARK-GLUON DYNAMICS IN THE NUCLEAR MEDIUM

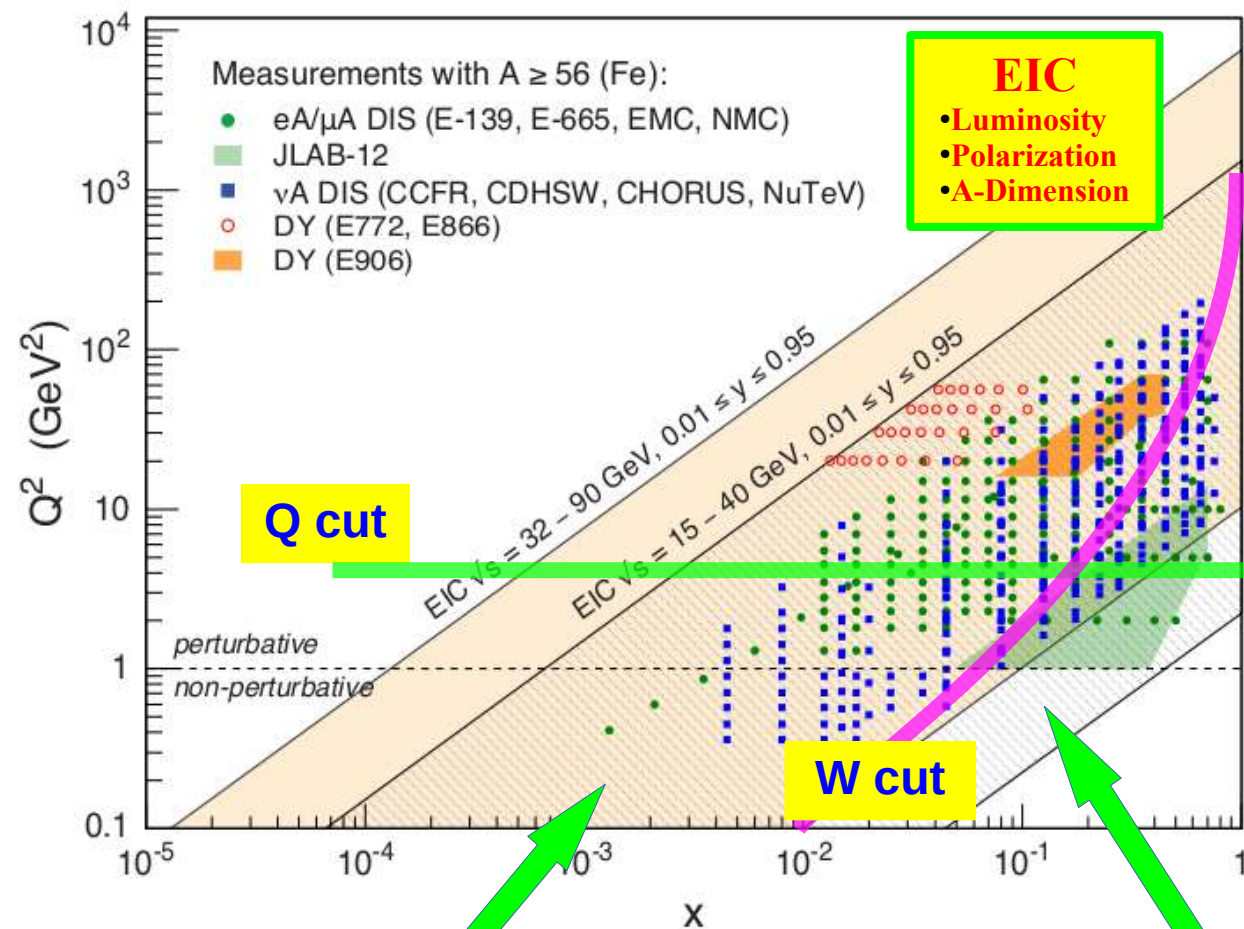


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<https://indico.ectstar.eu/event/276/>

Conclusion



High- x :

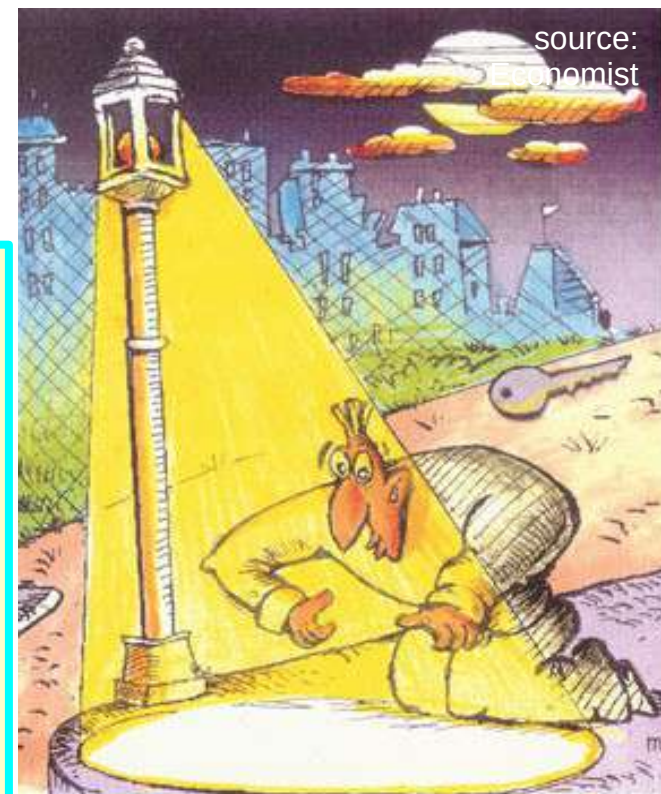
Nuclear PDFs: $x > 1$ allowed;
 impacts $F_2^{\text{Nuc}}/F_2^{\text{Iso}}$ in Fermi region
 Target Mass Corrections
 pick up M^2/Q^2 higher twist
 Deuteron Corrections
 impacts $F_2^{\text{Nuc}}/F_2^{\text{Deuteron}}$ ratio

Low- x :

Shadowing
 Recombination
 Resummation
 BFKL
 Saturation

Low- Q^2 :

Non-Perturbative interface
 collective effects
 Target Mass Corrections
 pick up M^2/Q^2 higher twist
 F_L at low Q^2 access to $g(x)$
 Run at multiple energies



Status Summary:

Dipole Calculation:

- Working Python Framework to compute σ^{tot} and F2, FL
- Reasonable agreement with e.g., HERA data (*need to fit*)
- Grid methods enable fast calculation

BK Evolution:

- Full evolution codes: [BKsolver, rcbk] validated
 - Try ML for inner fitting loop

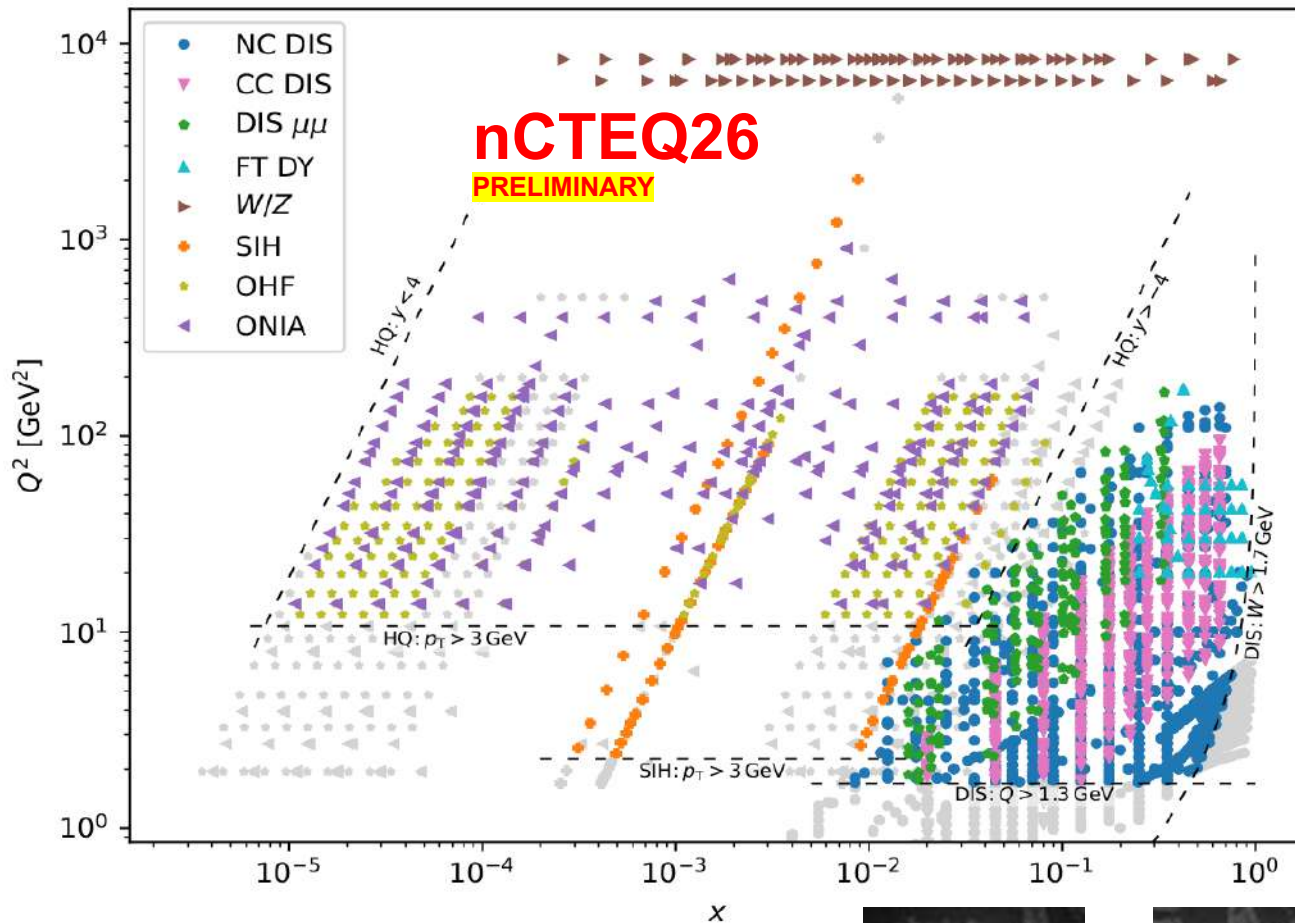
ML approach to BK Evolution

- Reasonable approximation across kinematics [preliminary]
- Fast enough for flexible fits

Other evolution models:

- Could extend to other models: BFKL, JIMWLK, ... DGLAP??
- Could 'warm-up' running BK with LO & NLO

nCTEQ26 Updates:



- Wealth of new data & processes
- Updated theory & methodology
- Updated proton baseline
- Updated x-parametrization
- New A-parametrization
- Good data description overall
- Particular focus on:
 - A-dependence
 - strange & gluon uncertainties

nCTEQ

nuclear parton distribution functions



Tomas
Jezo



Katrin
Greve



Jan
Wissmann



Aleksander
Kusina