

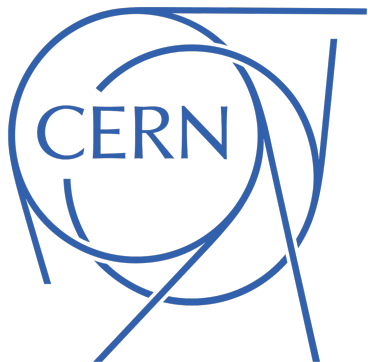
# ***xFitter Tutorial***

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Francesco Giuli

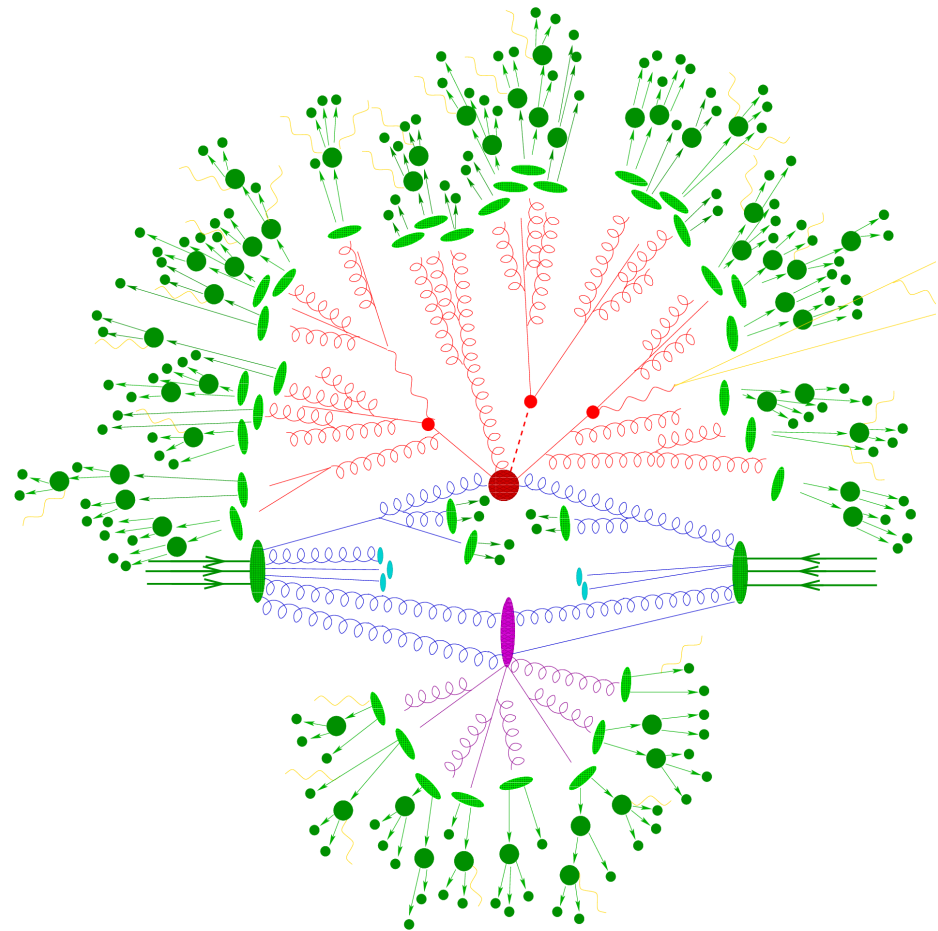
ATLAS SM workshop (Prague, Czech Republic)

14/09/2023



# Motivation

- No new physics found at the LHC so far ☹
- Need for precise measurement of SM processes
- This means accurate higher order (HO) calculations...
- ... but also precise knowledge of **Parton Distribution Functions (PDFs)**
- Proton-proton collision at the LHC
- For simplicity, let's consider **Deep Inelastic Scattering (DIS)** process - just one incoming parton
- $pp$  and  $p\bar{p}$  collisions will be considered in the exercises



# Factorisation theorem

$$\sigma_{DIS}(x, Q^2) = \int_x^1 \frac{dz}{z} C_i(z, \alpha_s(Q^2)) f_i\left(\frac{x}{z}, Q^2\right) = C_i \otimes f_i$$

## Partonic cross sections:

- Process dependent
- High-scale (short-distance) objects
- Computable in perturbation theory (LO, NLO, NNLO, N<sup>3</sup>LO)

## PDFs:

- Universal (process independent)
- Low-scale (long-distance) objects
- Non computable in perturbation theory
- Scale dependence perturbative (DGLAP)

➤ Once PDFs have been **determined at a given scale**, the **DGLAP** evolution equations can be used to **evolve them to any other scale**

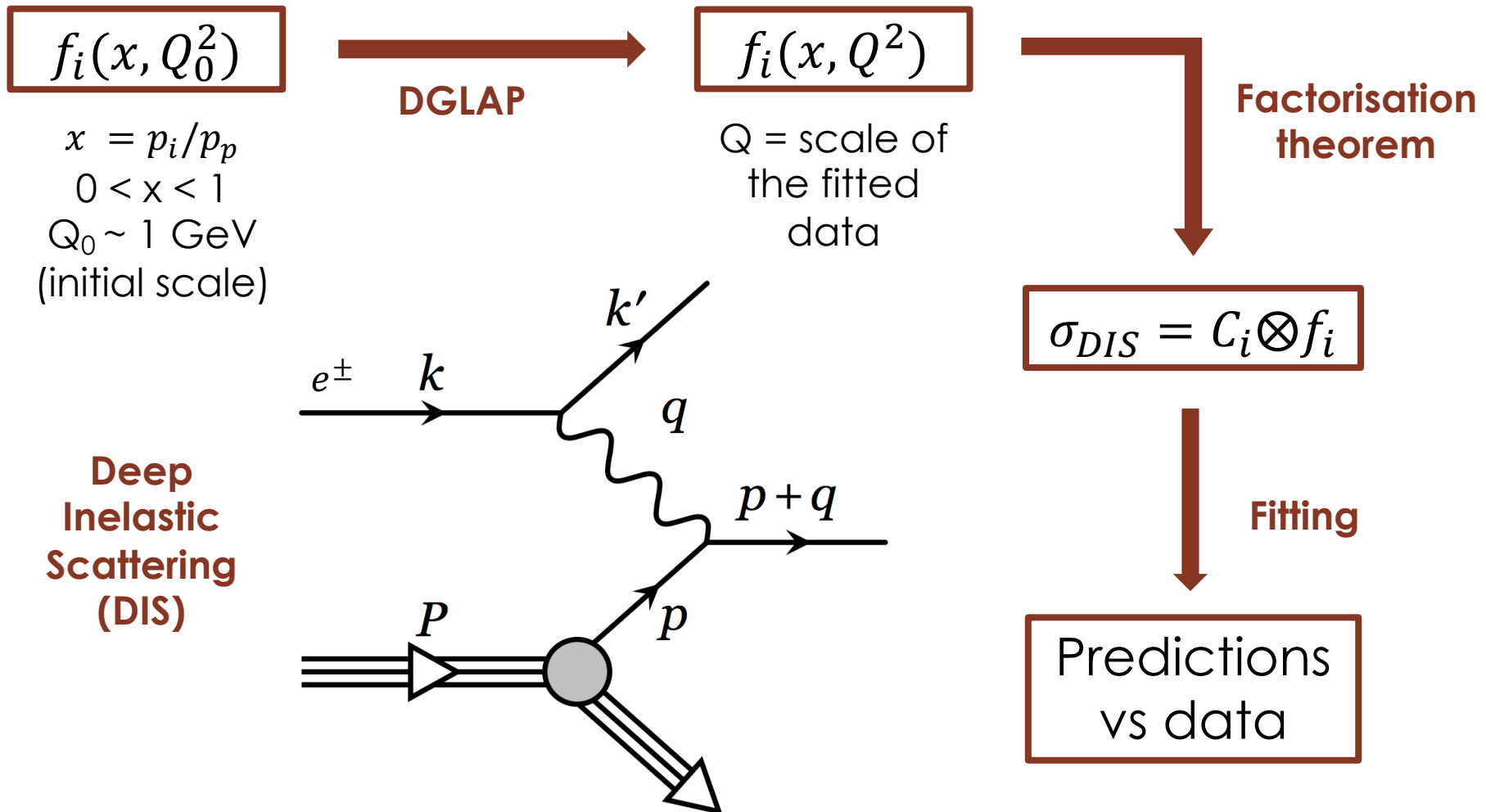
$$\mu^2 \frac{\partial}{\partial \mu^2} f_i(\mu) = P_{ij} \otimes f_j(\mu)$$

$$P_{ij}(y) = \frac{\alpha_s(\mu)}{2\pi} P_{ij}^{(0)}(y) + \left( \frac{\alpha_s(\mu)}{2\pi} \right)^2 P_{ij}^{(1)}(y) + \dots$$

**Splitting functions**

# How do we determine PDFs?

- Presently, the most accurate and reliable way is through **fits to data**





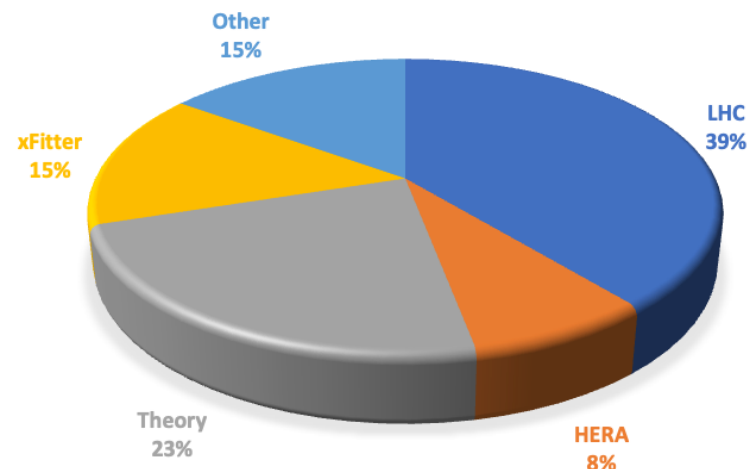
# The xFitter Project

➤ The xFitter project (former HERAFitter) is a **unique open-source QCD fit framework**

➤ GitLab repository (open access)

➤ This code allows users to:

- **extract PDFs** from a large variety of data
- assess the **impact** of **new data on PDFs**
- check the **consistency** of experimental data
- test different **theoretical assumptions**



➤ Several active developers between experimentalists and theorists

➤ More than 100 publications obtained using xFitter since the beginning of the project

➤ List of recent analyses by the xFitter Developers' Team:

**MORE IN PREPARATION!**

Phys.Rev.D 104 (2021) 5, 056019,  
arXiv:2105.11306

[QCD analysis of pion fragmentation functions in the xFitter framework](#)

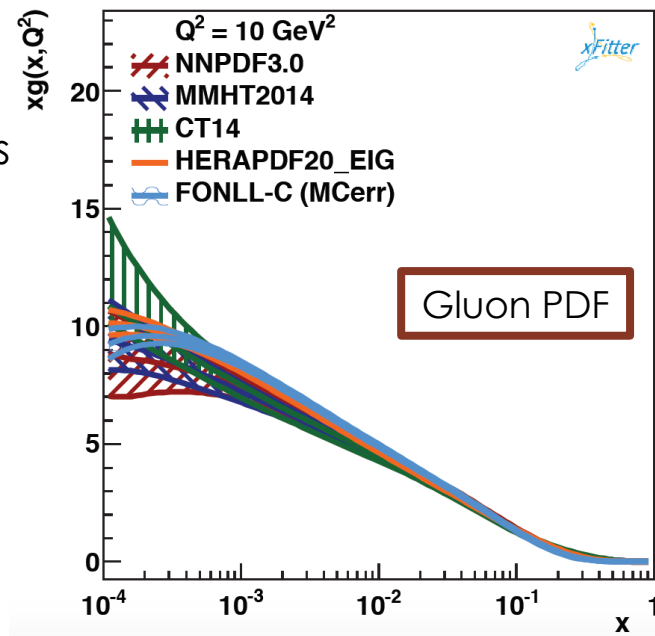
Phys.Rev.D 102 (2020) 1, 014040,  
arXiv:2002.02902

[Parton Distribution Functions of the Charged Pion Within The xFitter Framework](#)

# xFitter in a nutshell

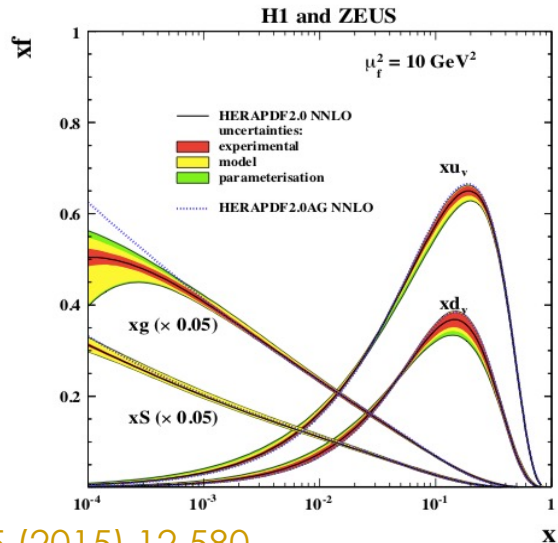


- **Parametrise** PDFs at the initial scale:
  - several functional forms available
  - define PDF parameters to be minimised
- **Evolve** PDFs to the scales of the fitted data points:
  - DGLAP evolution up to NNLO in QCD and NLO QED (QCDNUM, APFEL, MELA)
  - non-DGLAP evolutions (dipole, CCFM)
- **Compute** predictions for the data points:
  - several mass schemes available in DIS (ZM-VFNS, ACOT, FONLL, TR, FFNS)
  - predictions for hadron-collider data through fast interfaces (APPLgrid, FastNLO)
- **Comparison data-predictions** via  $\chi^2$ :
  - multiple definitions available
  - consistent treatment of the systematic uncertainties
- **Minimise** the  $\chi^2$  w.r.t. the fitted parameters
  - using MINUIT or by Bayesian reweighting
- **Useful drawing tools** – nice and colorful plots
- Last xFitter External meeting held in May at CERN



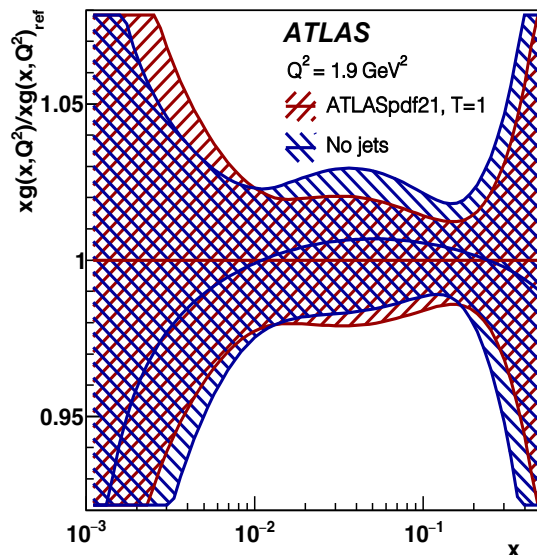
# Results obtained with xFitter

## DIS inclusive processes ( $ep$ )

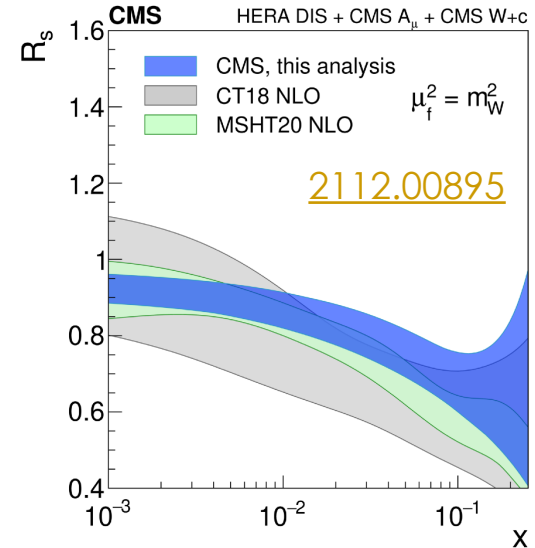


[EPJC 75 \(2015\) 12 580](#)

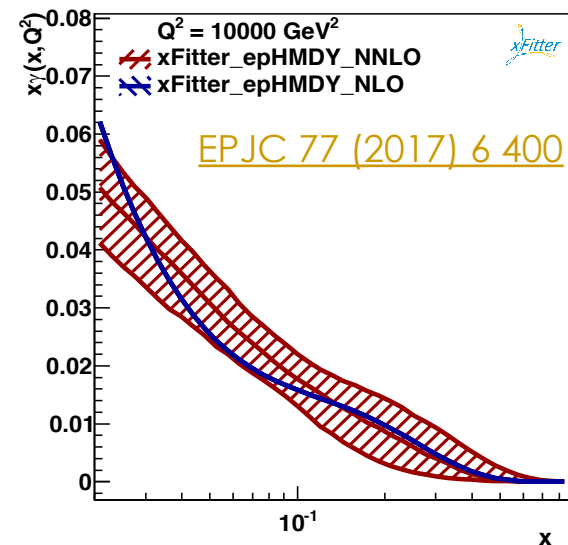
## Jet production ( $ep, pp$ ) [EPJC 82 \(2022\) 5 438](#)



## Drell-Yan processes ( $pp, p\bar{p}$ )



## DY data sensitivity to photon PDF



# xFitter release 2.2.0



## xFitter

### Sample data files:

**LHC:** ATLAS, CMS, LHCb

**Tevatron:** CDF, D0

**HERA:** H1, ZEUS, Combined

**Fixed Target:** ...

**User Supplied:** ...

GitLab

### Wiki

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## xFitter / DownloadPage

### Releases of the xFitter QCD analysis package

- The release notes can be found in this attachment: [xFitter\\_release\\_notes.pdf](#).
- Installation script for xFitter together with QCDNUM, APFEL, APPLGRID, LHAPDF [install-xFitter-2.0.1](#)
  - New installation script from master branch [install-xfitter-master](#)
- Data and theory files can be downloaded from gitlab [gitlab data repository](#)

Date	Version	Files	Remarks
 03/2022	<b>2.2.0 FutureFreeze</b>	<a href="#">xfitter-2.2.0.tgz</a>	Major update of evolution and reaction interfaces
 05/2019	<b>2.0.1 OldFashioned</b>	<a href="#">xfitter-2.0.1.tgz</a>	update/bug fix to 2.0.0 FrozenFrog
 03/2017	<b>2.0.0 FrozenFrog</b>	<a href="#">xfitter-2.0.0.tgz</a>	stable release with decoupled data and theory files



**2.2.0  
Future Freeze**

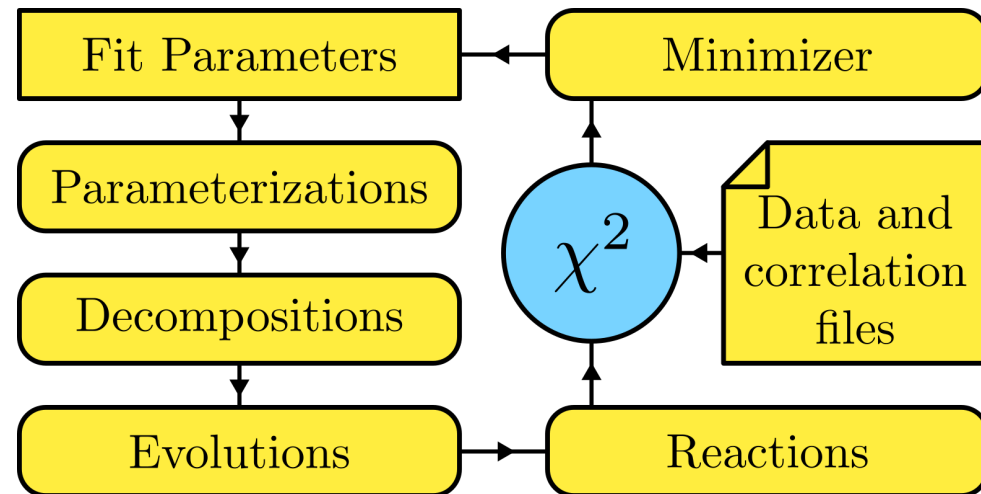
<https://www.xfitter.org/xFitter/xFitter/DownloadPage>

➤ **Release 2.2.0 released!** (major update of evolution and reaction interfaces)

➤ Script to install xFitter and all its dependencies: [install-xFitter](#)

# Talking about the new release...

- **Significant changes** in the internal structure
- **Re-written interfaces** to minimizers, PDF parameterisation, decomposition, evolution and theory reactions
- **Large changes in the user interface**
- Data handling, format and  $\chi^2$  calculation remain largely the same (but there are changes)
- Nicely summarized in this [talk](#) by S. Glazov
- Picture taken from Ivan Novikov's [talk](#)



# xFitter usage in the HEP community

- xFitter is the **tool of choice for PDF/QCD analyses by the LHC Collaborations**
- **ATLAS:**
  - PDF fit from diverse ATLAS data at  $\sqrt{s} = 7, 8$  and 13 TeV - [EPJC 82 \(2022\) 5 438](#)
- **Drell-Yan phenomenology:**
  - PDF impact of  $A_{FB}$  in NC Drell-Yan events - [JHEP 10 \(2019\) 176](#)
  - PDF sensitivity of the longitudinal Z-boson polarisation - [Phys.Lett.B 821 \(2021\) 136613](#)
  - PDF sensitivity to  $A_{FB}$  and  $A_W$  in Drell-Yan for Precision EW Measurements and New Physics Searches - [Nucl.Phys.B 968 \(2021\) 115444](#)
  - Enhancing the LHC sensitivity to broad  $W'/Z'$  resonances of new gauge sectors - [JHEP 02 \(2022\) 179](#), [PLB 841 \(2023\) 137915](#)
- Important contribution in **several ongoing activities of the LHC EW WG:**
  - **Correlations between different PDFs** through pseudo-data fits
  - ATLAS/CMS/LHCb  $\sin^2 \theta_{eff}^l$  **pseudo data** and combination exercise
  - Tevatron/ATLAS (and in future LHCb and CMS)  $m_W$  **combination**
- **$\alpha_s$  extraction** from Z boson transverse momentum distribution - [2203.05394](#), [ATLAS-CONF-2023-015](#)

# List of exercises

- **Exercise 1:** PDF fit
  - learn the basic settings of a QCD analysis, based on HERA data only
- **Exercise 2:**  $\alpha_s$  extraction
  - learn the basic of an  $\alpha_s$  extraction using ATLAS Z  $p_T$  data
- **Exercise 3:** LHAPDF analysis
  - how to estimate impact of a new data without fitting
  - basis on profiling and reweighting techniques

Other useful/interesting exercise you might want to have a look at in backup:

- **Exercise 4:** Including small-x resummation correction in a PDF fit
- **Exercise 5:** Adding your preferred PDF parametrization
- **Exercise 6:** Fit to final combined HERA+II data and ATLAS W,Z data at 7 TeV
  - strange-quark density: fixed vs free  $r_s$
  - unsuppressed strange at low-x
- **Exercise 7:** Charged pion PDF
- **Exercise 8:** Charged pion Fragmentation Functions (FFs)
- **Bonus:** how to generate fixed-order predictions (key ingredient of a PDF fit)

$$r_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$



# Overview

- Each exercise in a separate directory: ~/xFitterTutorial/
  - **exercise1**
  - **exercise2**
  - **exercise3**
  - exercise4
  - exercise5
  - exercise6
  - exercise7
  - exercise8
- You can find the xFitter manual and this tutorial in ~/xFitterTutorial/DOC
  - DOC/xFitter\_Manual.pdf
  - DOC/xFitter\_Tutorial.pdf
- All these exercises (with many more examples) can be found [here](#)
- [Updated Wiki](#) to help users, with also the list of [existing JRAs](#)
- If you cannot find an answer to your question, **create a new JIRA ticket**, with issue type "Question"



# Input files for a xFitter run

➤ Each time we run xFitter, we need to care about three configuration files:

➤ **parameters.yaml:**

- Minimisers – MINUIT or CERES
- Settings and commands for MINUIT
- Define parameters of the PDF parameterization
- Running mode: PDF fit or LHAPDF analysis
- QCD order (NLO or NNLO)
- Heavy flavor scheme (TR, ACOT, FONLL, etc.)

```
Minimizer: MINUIT # CERES
CERES:
  offset: 2
  tolerance: 1e-5
  strategy: 0
  covariance: 1
```

(CERES instructions since the tutorial uses MINUIT)

➤ **steering.txt:**

- List of data sets
- $\chi^2$  settings

➤ **constants.yaml:**

- EW and SM input parameters e.g. couplings, quark masses etc.

# General structure of the exercise

- Each exercise has all the necessary inputs and datafiles for running xFitter
- The results will be saved in the 'output' directory for further manipulation
- Before every exercise, in order to set up environmental variables, do  
**\$> source ~/Software/setup.sh**
- To run xFitter, in the exercise folder type **\$> xfitter**
- To draw graphical visualisation of the results: **\$> xfitter-draw output**
  - Many drawing options! Type **\$> xfitter-draw --help** to see all of them
- Post-fit and pre-fit manipulation of the LHAPDF files: **\$> xfitter-process** (needed for exercise3 in backup)
  - Many modules available! Type **\$> xfitter-process --help** to see all of them
    - profile – to be used with Hessian PDF eigenvectors error sets
    - reweight – to be used with NNPDF-style PDF sets (MC replicas)
    - scale90to68 – scale PDF error bands from 90% CL to 68% CL
    - rotate – obtain a PDF set which members are sorted according to their sensitivity to particular data
    - symmetrize – produces symmetric bands out of hessian PDF set

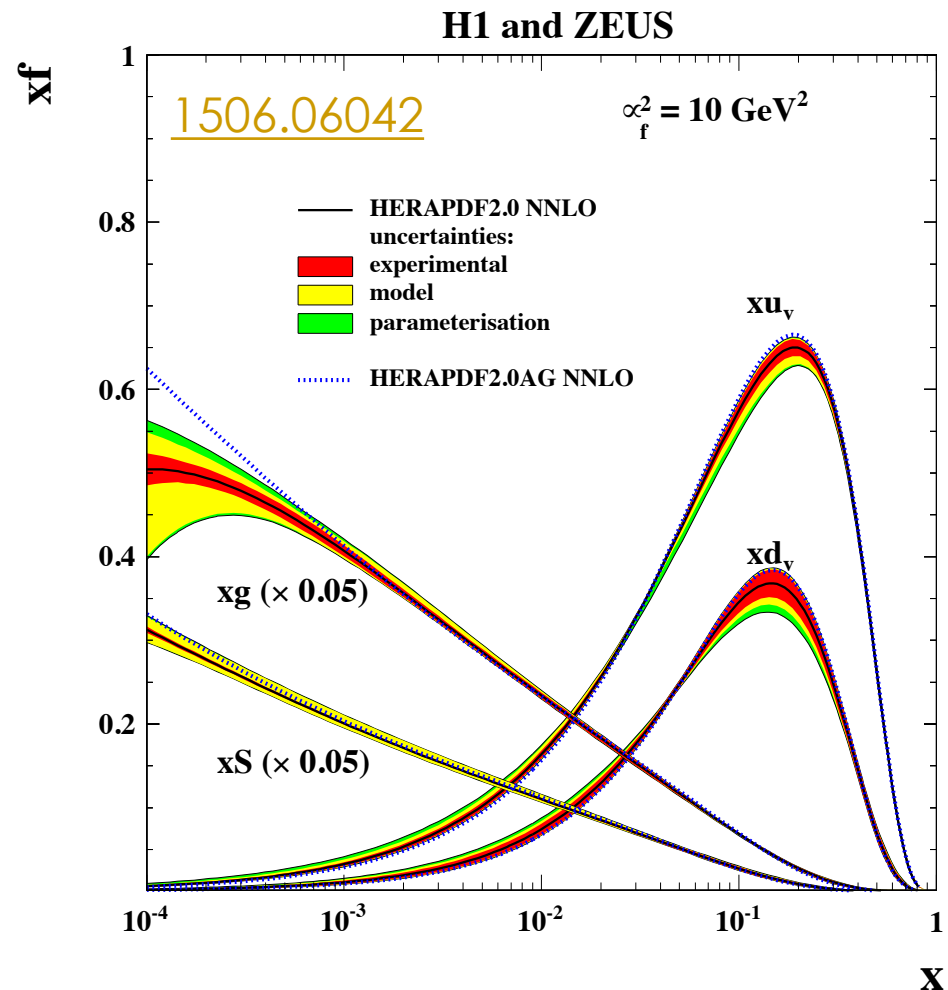
# EXERCISE 1

## PDF fit

# Exercise 1

- **Purpose:** Learn the basic settings of a QCD analysis and reproduce the results of the HERAPDF2.0 fit
- **Data set:** Final combined HERA I+II DIS data
- **QCD order:** NNLO

This data set is very important! **Backbone of all modern PDF fits**



# Exercise 1 - settings

- `$> cd ~/xFitterTutorial/exercise1`
- Final combined HERA1+II DIS data in `steering.txt`

`&InFiles`

`! Number of input files`

`NInputFiles = 7`

`! Input files:`

`InputFileNames =`

```
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_920-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_820-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_575-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_460-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCem-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCep-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCEm-thexp.dat',
```

`&End`

- FYI you can add as many data sets as you want! The fit will take longer ☺  
have a look at this [example](#)

# The structure of a xFitter datafile - DIS

```
&Data
  Name = "HERA1+2 NCep 460"
  IndexDataset = 106
  Reaction = "NC e+-p"

  TermName = 'R'
  TermSource = 'use:hf_scheme_DISNC'
  TermInfo = 'type=signed:flav=incl:echarge=1:epolarity=0' ! in CInfo there was also "YSWIMEXP" = 1.0
  TheorExpr = 'R'

  NData = 210
  NColumn = 176
  ColumnType = 3*"Bin","Sigma", 172*"Error"
  ColumnName = "Q2","x","y","Sigma", "stat", "uncor","sysHZComb1001","sysHZComb1002","sysHZComb1003","sysHZComb1004","sysHZComb1005",
  Percent = 172*true
&End
```

- **'Name'** provides the name of the data set
- **'IndexDataset'** is an internal index of the data set (provide unique numbers to get extra  $\chi^2$  info)
- **'Reaction'** indicates the reaction type of the data set (used to trigger the corresponding theory calculation)
- **'NData'** specifies the number of data points in the file
- **'NColumn'** is the number of columns in the data table
- **'ColumnType'** defines layout of the data table: *Bin, Sigma, Error and Ignored*
- **'ColumnName'** defines names of the columns (e.g. x,  $Q^2$  and y are required for DIS NC xsec)
  - If ColumnType = Sigma, it provides a label for the observable
  - If ColumnType = Error, the following names have special meaning: *stat, uncor and total*
    - Other names specify columns of correlated systematic uncertainties (e.g. each column of the correlated uncertainty must have unique name)
- **'Percent'** tells if an uncertainty is given in absolute (false) or in percent (true)

# The structure of a xFitter datafile - LHC

[Gitlab repository](#)

```
TermName = 'A','K'
TermSource = 'APPLgrid','KFactor'
TermInfo = 'GridName=datafiles/lhc/atlas/wzProduction/1612.03016/grid-40-6-15-3-Z0_zypeak_cc.root',
           'FileName=datafiles/lhc/atlas/wzProduction/1612.03016/kf.zypeak_cc.txt:FileColumn=3'
TheorExpr = 'K*A/1000'
```

- **'TermName'** gives names of terms used in the theory expression
- **'TermSource'** might be:
  - KFactor → term which denotes an array of K-factors corresponding to the data bins
  - APPLgrid, FastNLO, ... → this term tells the parser to initialize the correct theory reaction for the cross section evaluation
  - VirtGrid → it can be used if the fit is performed using multidimensional measurements (here, each row denotes a single bin of the cross section and, the APPLGRID file location and number of bins in it)

#	y1	y2	applgrid	n_grid_bins
0.0	0.3		theoryfiles/atlas/Jets2010-vg/R04/eta1.root	17
0.3	0.8		theoryfiles/atlas/Jets2010-vg/R04/eta2.root	17
0.8	1.2		theoryfiles/atlas/Jets2010-vg/R04/eta3.root	17
1.2	2.1		theoryfiles/atlas/Jets2010-vg/R04/eta4.root	16
2.1	2.8		theoryfiles/atlas/Jets2010-vg/R04/eta5.root	13

- **'TermInfo'** gives paths from where the term numerical values should be taken
- **'TheorExpr'** is the theory expression in simple algebraic form

# The structure of a xFitter datafile - Plot

```
&PlotDesc
  PlotN = 1
  PlotDefColumn = 'y_max'
  PlotDefValue = 0., 5.
  PlotOptions(1) = 'Experiment:ATLAS@ExtraLabel:pp #rightarrow Z; #sqrt{s} = 7 TeV; #int L = 4.7 fb^{-1}@Title: 66 < M_{Z} < 116
&End                                     ,@XTitle: y @YTitle: d#sigma/dy [pb] '
```

- **'PlotN'** tells us the number of distributions to be plotted
- **'PlotDefColumn'** is the variable name you want to plot
- **'PlotDefValue'** specifies the x-axis range of the variable you're plotting
- **'PlotOptions'** are several plotting options to have some graphical improvement and labels on the standard xFitter plots in output



# Exercise 1 - settings

- The PDF parametrisation is set in parameters.yaml

Parameterisations:

```
par_uv:
  class: HERAPDF
  parameters: [Auv, Buv, Cuv, Duv, Euv]
par_dv:
  class: HERAPDF
  parameters: [Adv, Bdv, Cdv]
par_uubar:
  class: HERAPDF
  parameters: [Adbar, Bdbar, Cubar, Dubar]
par_dbar:
  class: HERAPDF
  parameters: [Adbar, Bdbar, Cdbar]
par_s: # s=fs/(1-fs) * Dbar
  class: Factor
  factor: DbarToS #name of parameter
  input: par_dbar
par_g:
  class: NegativeGluon
  parameters: [Ag, Bg, Cg, ZERO, ZERO, Agp, Bgp, Cgp]
```

equivalent  
to...

```
DefaultDecomposition: proton
Decompositions:
  proton:
    class: UvDvUbarDbarS
    xuv: par_uv
    xdv: par_dv
    xubar: par_uubar
    xdbar: par_dbar
    xs: par_s
    xg: par_g
```

```
#par_s:
#class: Expression
#expression: "Adbar*fs/(1-fs)*(x^Bdbar*(1-x)^Cdbar)"
# Another example for Expression parameterisation
#par_g:
#class: Expression
#expression: "Ag*(x^Bg*(1-x)^Cg-Agp*x^Bgp*(1-x)^Cgp)"
```

- HERAPDF-like PDF parametrisation:

$$Ax^B(1-x)^C(1+Dx+Ex^2) - \underbrace{A'x^{B'}(1-x)^{C'}}_{\text{Just for the gluon PDF } (C'_g = 25) \text{ to suppress negative contributions at high-}x}$$

Just for the gluon PDF ( $C'_g = 25$ )  
to suppress negative  
contributions at high- $x$

- Sum rules
- Asymptotic behaviour
- To better model the high- $x$  region

# Exercise 1 - settings

- The starting values of the parameters are set in parameters.yaml

Parameters:

```

Ag   : DEPENDENT
Bg   : [ -0.061953, 0.27 ]
Cg   : [ 5.562367, 0.32 ]
Agp  : [ 0.166092, 0.01 ] # negative gluon ....
Bgp  : [ -0.383100, 0.01 ]
Cgp  : [ 25.0, 0. ] # fix C of negative gluon
Auv  : DEPENDENT
Buv  : [ 0.810476, 0.016 ]
Cuv  : [ 4.823512, 0.06 ]
Euv  : [ 9.921366, 0.8 ]
Adv  : DEPENDENT
Bdv  : [ 1.029995, 0.06 ]
Cdv  : [ 4.846279, 0.3 ]
CUbar: [ 7.059694, 0.8 ]
DUbar: [ 1.548098, 1.0 ]
ADbar: [ 0.26883, 0.01 ]
BDbar: [ -0.1273, 0.004 ]
CDbar: # another example of providing value, step etc.
      value: 9.586246
      step: 1.2345
      #min
      #max
      #pr_mean
      #pr_sigma
ZERO  : [ 0. ] # zero
fs    : [ 0.4, 0.0 ]
fd    : "=1-fs"
AUbar: "(1-fs)*ADbar"

```

- The first number is the starting value, the second number the step size in the minimisation (if set to 0, the parameter is fixed)
- You can also define parameters as a function of other parameters i.e. AUBar

Another possible way to provide values, step, etc.

# Exercise 1 - settings

## ➤ Settings for PDFs as output of the fit in steering.txt

&Output

! -- Q2 values at which the pdfs & errors are done (up to 20)

Q2VAL = 1.9, 3.0, 4.0, 5., 10., 100., 6464, 8317

! Q2VAL = 1.9, 4., 10., 100., 6464, 8317

! How many x points to write (standard = 101)

OUTNX = 101

! x-range of output (standard = 1E-4 1.0)

OUTXRANGE = 1E-4, 0.9999

! Write out LHAPDF5 output

! WriteLHAPDF5 = false

&End

## ➤ Process dependent cuts in steering.txt

!----- CC ep -----

ProcessName(3) = 'CC e+-p'  
Variable(3) = 'Q2'  
CutValueMin(3) = 3.5  
CutValueMax(3) = 1000000.0

Should be identical to 'Name' in the datafile

ProcessName(4) = 'CC e+-p'  
Variable(4) = 'x'  
CutValueMin(4) = 0.000001  
CutValueMax(4) = 1.0

Should be one of the variable name ('ColumnName') in the datafile

There's also a 'binFlag' in the datafiles:

0 → bin not included in the fit

1 → bin included in the fit

# Exercise 1 - settings

- We want to perform a PDF fit...
- ... So we will use the option 'DefaultEvolution: proton-QCDNUM' in `parameters.yaml`

```
DefaultEvolution: proton-QCDNUM
```

```
Evolutions:
```

```
  proton-QCDNUM:
```

```
    ? !include evolutions/QCDNUM.yaml
```

```
    decomposition: proton #this could be omitted, as the default decomposition is set
```

- The QCD perturbative order is set in `parameters.yaml` as well:

```
# QCD parameters
```

```
Order: NNLO
```

```
NFlavour: 5
```

```
isFFNS: 0
```

```
Q0 : 1.378404875209 # Initial scale =sqrt(1.9)
```

```
alphas : 0.118
```

```
? !include constants.yaml
```

$Q_0$  is the starting scale  
where we parametrize PDFs

- Here you can see other parameters as well i.e. number of flavours,  $Q_0$ ,  $\alpha_s$  value etc. – this will overwrite what you have in `constants.yaml` (leaving everything else unchanged)

# Exercise 1 - settings

- The Heavy Flavour scheme is set in `parameters.yaml`

```
# Specify HF scheme used for DIS NC processes:
hf_scheme_DISNC :
  defaultValue : 'RT_DISNC'          # global specification
# defaultValue : 'BaseDISNC'         # global specification
# defaultValue : 'FONLL_DISNC'       # global specification
# defaultValue : 'FFABM_DISNC'
# 'HERA1+2 NCep 920' : 'BaseDISNC' # datafile specific (based on name)
# 1 : BaseDISNC
# 'HERA1+2 NCep 920' : 'Fractal_DISNC' # Fractal model. Add parameters file if you want to try it (see above)

# Specify HF scheme used for DIS CC processes:
hf_scheme_DISCC :
  defaultValue : 'BaseDISCC'         # global specification
# defaultValue : 'FONLL_DISCC'       # global specification
# defaultValue : 'FFABM_DISCC'       # global specification
```

- Several mass schemes available in DIS:

- ZM-VFNS
- ACOT
- FONLL
- TR
- FFNS

# Exercise 1 - settings

- To do a real fit with proper MINUIT minimisation:

MINUIT:

Commands: |

call fcn 1

set str 2

call fcn 3

migrad

hesse

minimisation

call fcn 3

PDF errors – 3 options:

- Pumplin – Eq. 43 of [hep-ph/0611148](https://arxiv.org/abs/hep-ph/0611148) (asymmetric)
- Hesse – symmetric version of Pumplin
- None – no error bands evaluation

Regulated by **doErrors: ###**

- To run just 3 iterations:

MINUIT:

Commands: |

set str 2

call fcn 3

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`

- To run xFitter: `$> xfitter`

- To draw your results: `$> xfitter-draw output`

- To see the full list of plotting options: `$> xfitter-draw --help`

# The output folder

- You can modify the folder name by changing `OutputDirectory: "output"`
- `'Status.out'` tells us if the fit has converged (OK) or not (Failed)
- `'minuit.out.txt'` contains the information about the MINUIT output of the fit
- `'Results.txt'` shows the global and partial  $\chi^2$ , as well as the pulls of each systematic uncertainty present in the fit
- `'parsout_0'` contains the output fit parameters (and their associated errors) in MINUIT format
- `'fittedresults.txt'` shows the comparison between data and fit predictions for each data point
- The `'proton'` contains the output PDFs in LHAPDF format
  - You can modify the name in `parameters.yaml`
- `'pdfs_q2val_0*.txt'` are .txt files with the PDF values at different Bjorken x ('01' represents the starting scale, and then you have one file for each scale defined in the steering card → Q2VAL)

```
WriteLHAPDF6:  
  name: "proton"  
  description: "..."  
  authors: "..."  
  reference: "..."
```



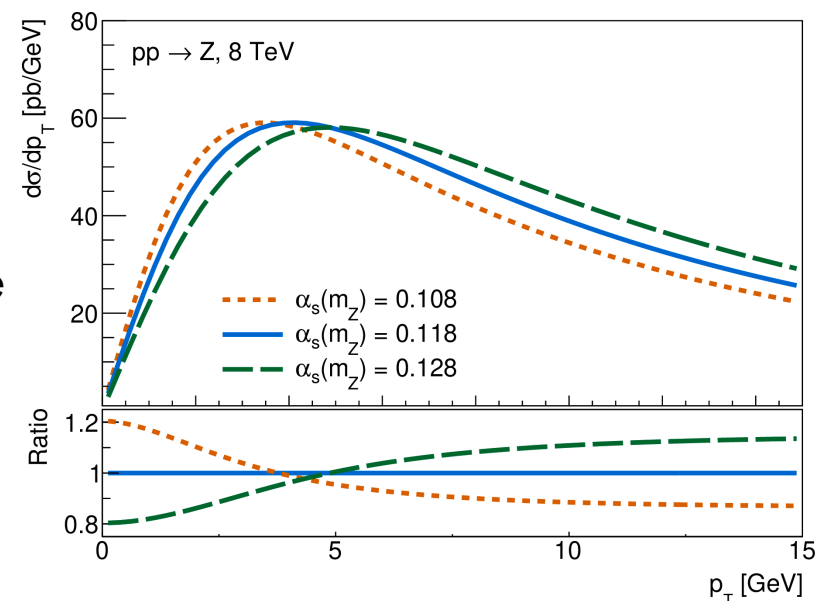
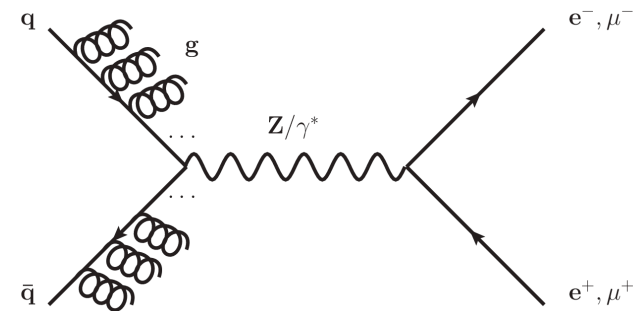
# EXERCISE 2

$\alpha_s$  extraction from  
ATLAS Z  $p_T$  data



# Exercise 2

- **Purpose:** Learn the basics of an  $\alpha_s$  extraction
- **Data set:** Final combined HERA+II DIS data + ATLAS 8 TeV Z  $p_T$  data ([ATLAS-CONF-2023-013](#)) – see backup for more details
- **QCD order:** N<sup>3</sup>LL + N<sup>3</sup>LO (through [DYTurbo](#) predictions)
- Strong coupling constant  $\alpha_s$  is the **least well known in nature**
- **Dominant uncertainties** to precision measurements of **Higgs coupling** at LHC or **EW precision observables** at  $e^+e^-$  colliders
- Non-zero value of Z  $p_T$  arises from initial state radiations from incoming partons due to momentum conservation
- The **peak position of Z  $p_T$**  and above is **sensitive to  $\alpha_s(m_Z)$**



## Exercise 2 - settings

- `$> cd ~/xFitterTutorial/exercise2/`
- We added the ATLAS 8 TeV Z  $p_T$  data on top of the final combined HERA+II DIS data in `steering.txt`  

```
'datafiles/lhc/atlas/zptfull8tev/zpt_y00_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y01_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y02_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y03_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y04_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y05_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y06_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y07_bwi.dat',
```
- Additional datasets which have sensitivity to  $\alpha_s$  (i.e. CDF Z  $p_T$  [data](#)) can be downloaded using the `./tool/xfitter_getdata.sh` script
- Very easy to use! `./tool/xfitter_getdata.sh arXiv_number`
- To see available data sets: `./tool/xfitter-getdata.sh --print`

## Exercise 2 – Z p<sub>T</sub> datafiles

- Open e.g.  
`./datafiles/lhc/atlas/zptfull8tev/zpt_y00_bwi.dat`

```
Reaction =      'NC pp'
TheoryType      = 'expression'
TermName = 'A1','K','C'
TermSource = 'DYPurbo','KFactor','KFactor'
TermInfo = 'FileName=datafiles/lhc/atlas/zptfull8tev/dyturbo/z-8tev-y00-n311.in',
           'FileName=datafiles/lhc/atlas/zptfull8tev/qedisr/qedisr_zpt_y00.txt:FileColumn=3',
           'FileName=datafiles/lhc/atlas/zptfull8tev/mcfm/afactor/n3lo-afactor-y00.txt:FileColumn=3'
TheorExpr= '(2*A1+C)*K*0.996/1000'
```

- Note the kind of reaction → 'NC pp' (Neutral Current production in pp collisions)
- 'TermSource = DYPurbo' thanks to a direct interface to xFitter
- The first file is literally a DYPurbo input file
- Additional k<sub>F</sub> to take into account e.g. ISR QED corrections or missing N<sup>3</sup>LO QCD contributions

# Exercise 2 - settings

- We add the statistical correlation matrices in `steering.txt`

&InCorr

```
! Number of correlation (statistical, systematical or full) files
NCorrFiles = 36
```

! Correlation files:

```
CorrFileNames(1) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y0.corr',
CorrFileNames(2) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y1.corr',
CorrFileNames(3) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y2.corr',
CorrFileNames(4) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y3.corr',
CorrFileNames(5) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y4.corr',
CorrFileNames(6) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y5.corr',
CorrFileNames(7) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y6.corr',
CorrFileNames(8) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y7.corr',
CorrFileNames(9) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y1.corr',
CorrFileNames(10) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y2.corr',
CorrFileNames(11) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y3.corr',
CorrFileNames(12) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y4.corr',
CorrFileNames(13) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y5.corr',
CorrFileNames(14) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y6.corr',
CorrFileNames(15) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y7.corr',
CorrFileNames(16) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y2.corr',
```

```
CorrFileNames(17) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y3.corr',
CorrFileNames(18) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y4.corr',
CorrFileNames(19) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y5.corr',
CorrFileNames(20) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y6.corr',
CorrFileNames(21) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y7.corr',
CorrFileNames(22) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y3.corr',
CorrFileNames(23) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y4.corr',
CorrFileNames(24) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y5.corr',
CorrFileNames(25) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y6.corr',
CorrFileNames(26) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y7.corr',
CorrFileNames(27) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y4.corr',
CorrFileNames(28) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y5.corr',
CorrFileNames(29) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y6.corr',
CorrFileNames(30) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y7.corr',
CorrFileNames(31) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y5_y5.corr',
CorrFileNames(32) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y5_y6.corr',
CorrFileNames(33) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y5_y7.corr',
CorrFileNames(34) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y6_y6.corr',
CorrFileNames(35) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y6_y7.corr',
CorrFileNames(36) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y7_y7.corr',
```

&End

- The general format of correlation matrices ➡

- 'Name1, Name2' are the dataset name(s)
- 'IdColumns' are the variables i.e.  $p_T$ ,  $m_{ll}$ , etc.
- 'NBins' are the number of bins for each variables
- You need to specify the kind of correlation (i.e. you can also have 'Full covariance matrix')
- The input format is very easy to understand!

&StatCorr

```
Name1 = 'ATLAS 1D ttbar vs ptavt 13 TeV'
Name2 = 'ATLAS 1D ttbar vs mtt 13 TeV'
```

```
NIdColumns1 = 2
NIdColumns2 = 2
```

```
IdColumns1 = 'ptlow','pthigh'
IdColumns2 = 'mtt1','mtt2'
```

```
NBins1 = 2
NBins2 = 3
```

```
MatrixFormatIsTable = true
```

```
MatrixType = 'Statistical correlations'
&End
```

0	0	325	400	480
0	0	400	480	580
0	50	0.5	0.2	-0.07
50	100	0.5	0.4	0.07

## Exercise 2 - settings

- Let's also have a look at the DYTurbo part in `parameters.yaml`

DYTurbo:

```
#? !include reactions/DYTurbo.yaml
order: 3      # Perturbative order in QCD: 0 for LL, 1 for NLL+NLO, 2 for NNLL+NNLO, 3 for NNNLL+NNLO
muR: 1.       # Renormalization scale
muF: 1.       # Factorization scale
muRes: 1.     # Resummation scale
g1: 0.66      # Universal Gaussian non-perturbative form factor
g2: 0         # Q-dependent Gaussian non-perturbative form factor
g3: 0         # x-dependent Gaussian non-perturbative form factor
q: 0.1        # quartic term
debug: 0
```

- $g_1$ ,  $g_2$  and  $g_3$  regulates a non-perturbative form factor which affects the region of  $Z$   $p_T < 5$  GeV

$$S_{\text{NP}}(b) = \exp \left[ -g_j(b) - g_K(b) \log \frac{m_{\ell\ell}^2}{Q_0^2} \right]$$

- $q$  regulates the quartic term

- **$g_1$  and  $q$  are free parameters of the fit!**

Constrained by data

DYTurbo/g1: [ 0.488881, 0.0434729 ]

DYTurbo/q: [ -0.187143, 0.0296958 ]

$$g_j(b) = \frac{g b^2}{\sqrt{1 + \lambda b^2}} + \text{sign}(q) \left( 1 - \exp \left[ -|q| b^4 \right] \right)$$

$$g_K(b) = g_0 \left( 1 - \exp \left[ -\frac{C_F \alpha_s(b_0/b_*) b^2}{\pi g_0 b_{\text{lim}}^2} \right] \right)$$

## Exercise 2 - settings

- We have to free the  $\alpha_s(m_Z)$  parameter in `parameters.yaml`

```
alphas: [ 0.117178, 0.000417857 ]
```

- We want to do a real MINUIT minimisation fit, so:

MINUIT:

```
Commands: |
call fcn 1
set str 2
call fcn 3
migrad
hesse
call fcn 3
```

[EPJ Plus \(2019\) 134, 531](#)

As regards the PDF parametrisation, we adopt one with more flexibility at low x - see Exercise 5 in backup!

```
doErrors : Hesse # None
```

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output_PDF_aS`
- Bonus: you can also run separate fits with fixed values of  $\alpha_s$  (see next slide)
  - In this way we can check the correlation between  $\alpha_s$  and the gluon PDF

# Exercise 2 - results

ATL-COM-PHYS-2023-076

➤  $\alpha_s(m_Z) = 0.118616 \pm 0.000757$

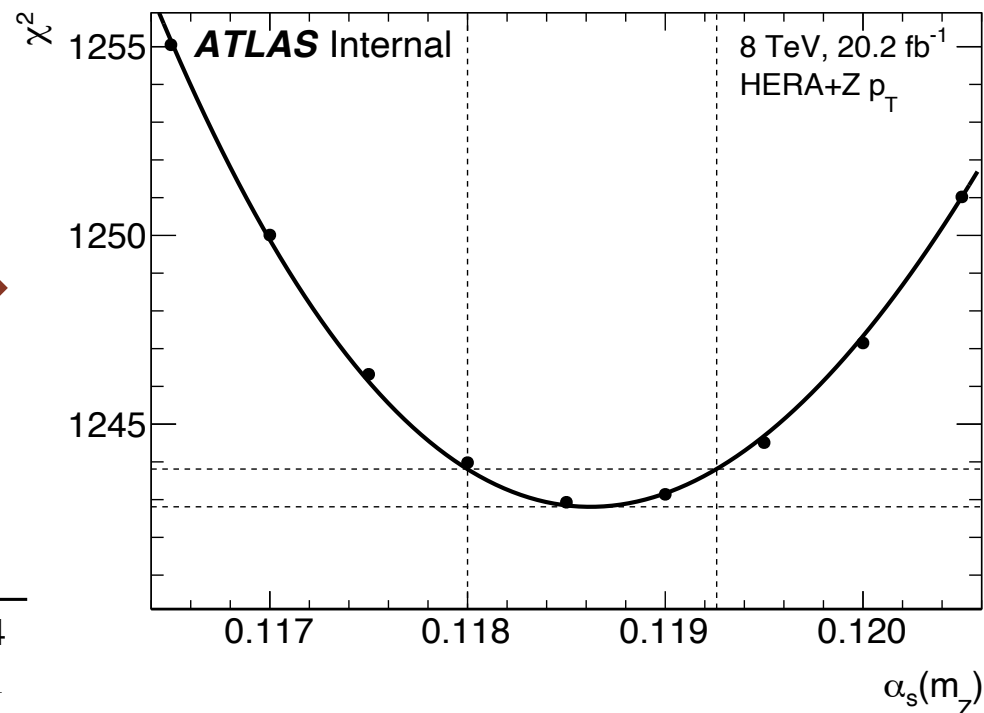
➤ Now we can compare the results with what has been found in the:

- N<sup>3</sup>LO+N<sup>3</sup>LL scan →
- $\alpha_s(m_Z)$  determination based on aN<sup>4</sup>LL+N<sup>3</sup>LO predictions



Experimental uncertainty	+0.00044	-0.00044
PDF uncertainty	+0.00051	-0.00051
Scale variations uncertainties	+0.00042	-0.00042
Matching to fixed order	0	-0.00008
Non-perturbative model	+0.00012	-0.00020
Flavour model	+0.00021	-0.00029
QED ISR	+0.00014	-0.00014
N4LL approximation	+0.00004	-0.00004
Total	+0.00084	-0.00088

$\alpha_s(m_Z) = 0.11828^{+0.00084}_{-0.00088}$



$\alpha_s(m_Z) = 0.11866 \pm 0.00064$

(from the  $\Delta\chi^2 = 1$  criterion)

**All the three approaches give consistent results!**

# **EXERCISE 3**

## **LHAPDF analysis**



## Exercise 3

- **Purpose:** Learn how to include a new dataset into an existing PDF set, without redoing a PDF fit (profiling/reweighting) – a very simple exercise which can be nicely put in a paper
- **Data set:** Tevatron W-boson charge asymmetry
- **QCD order:** NLO
- PDF sets from LHAPDF stored in `~/Software/deps/lhapdf/share/LHAPDF/`
- LHAPDF is a convenient library for the generic interpolation of PDFs as functions of  $x$  and  $Q^2$
- PDFs are saved in tables of PDF values at fixed points in  $x$  and  $Q^2$ , and fast interpolation functions allow to access the PDFs at any other value
- To download from PDF sets in LHAPDF format:

```
$> cd ~/Software/deps/lhapdf/share/LHAPDF/  
$> lhpdf --pdfdir=./install HERAPDF20_NNLO_EIG (VAR)  
$> export LHAPATH='pwd'/:$LHAPATH
```

## Exercise 3 - settings

- Settings for running a LHAPDF Analysis in `parameters.yaml`
- We need to specify that we want to use LHAPDF evolution

```
DefaultEvolution: proton-QCDNUM
```

```
Evolutions:
```

```
  proton-QCDNUM:
```

```
    ? !include evolutions/QCDNUM.yaml
```

```
    decomposition: proton #this could be omitted, as the default decomposition is set
```

```
    # The following allows QCDNUM to read PDFs from other evolutions:
```

```
    EvolutionCopy: "proton-LHAPDF"
```

```
  proton-LHAPDF:
```

```
    class: LHAPDF
```

```
    set: "HERAPDF20_NNLO_EIG"
```

```
    member: 0
```

Here you specify the LHAPDF  
set you want to use



# Profiling methodology

- The inclusion of new data into an existing PDF set can be done with a Hessian profiling technique
- We define a  $\chi^2$  with theory uncertainties ( $\beta_{th}$  represent the PDF uncertainties)

$$\begin{aligned}\chi^2(\beta_{exp}, \beta_{th}) &= \chi_{exp}^2 + \chi_{th}^2 \\ &= \sum_{i=1}^{N_{data}} \frac{(\sigma_i^{exp} + \sum_j \Gamma_{ij}^{exp} \beta_{j,exp} - \sigma_i^{th} - \sum_k \Gamma_{ik}^{th} \beta_{k,th})^2}{\Delta_i^2} + \sum_j \beta_{j,exp}^2 + \sum_k \beta_{k,th}^2\end{aligned}$$

- Find the  $\beta_{k,th}$  which minimised the  $\chi^2$  on the new data
- The fit is done by solving a system of liner equations
- Reinterpret the  $\beta_{k,th}^2$  shifts as optimisation of the PDFs

## Exercise 3 - settings

➤ `$> cd ~/xFitterTutorial/exercise3/`

➤ The Tevatron W asymmetry data sets and correlations files are set in `steering.txt`

```
&InFiles
! Number of input files
  NInputFiles = 2

! Input files:

  InputFileNames =
    'datafiles/tevatron/cdf/wzProduction/0901.2169/CDF_W_asymmetry-thexp.dat',
    'datafiles/tevatron/d0/wzProduction/1312.2895/D0_W_asymmetry-thexp.dat',
&End

&InCorr
! Number of correlation (statistical, systematical or full) files
  NCorrFiles = 1

! Correlation files:
  CorrFileNames(1) = 'datafiles/tevatron/d0/wzProduction/1312.2895/D0_W_asymmetry.corr'
&End
```

➤ We also include a correlation matrix to take statistical correlation into account (see Exercise 2 for more details)

## Exercise 3 - settings

- We follow the instructions described in the [xFitter twiki](#)

Profiler:

Evolutions:

proton-LHAPDF:

sets: [HERAPDF20\_NNLO\_EIG, HERAPDF20\_NNLO\_VAR, HERAPDF20\_NNLO\_VAR]

members: [, [0,1,10], [0,11,13]] *# when omitted, default members is [0,1,end]*

error\_type\_override: [None, hessian, symmhessian] *# treat parametrisation variations (members 11-13*

Status: "On" *# "Off" to turn off profiler*

WriteTheo: "Asymmetric" *# Can be "Off", "On" or "Asymmetric" (to store asymmetric variations)*

getChi2: "On" *# determine and report chi2 for each variation*

- Remember to set enableExternalProfiler: "On" (it creates of additional files, needed for xfitter-draw command)
- PDFs are taken from LHAPDF, so there is no need to specify a parametrisation in parameters.yaml file
- We also enable the treatment of asymmetric PDF uncertainties with 'WriteTheo' and we get the  $\chi^2$  at every single iteration ('getChi2')

# Exercise 3 – produce a new PDF set

- To produce a new PDF set in LHAPDF format

```
$> xfitter-process profile output/pdf_shifts.dat output/pdf_rotate.pdf  
output/HERAPDF20nnlo/ HERAPDF20nnlo-TevatronW
```

- Save the new PDF set into our LHAPDF collection

```
$> mv HERAPDF20nnlo-TevatronW ~/Software/deps/lhapdf/share/LHAPDF/
```

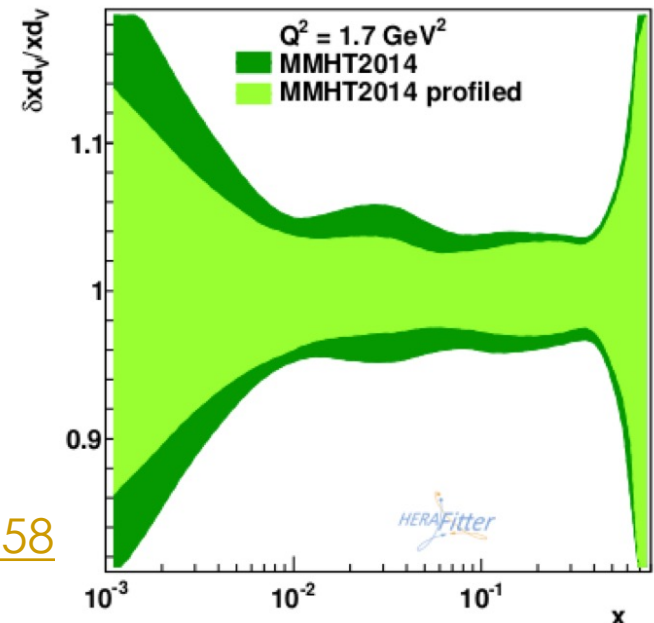
- Run a new LHAPDF analysis specifying the new PDF set in parameters.yaml file

```
proton-LHAPDF:  
sets: [HERAPDF20nnlo-TevatronW]
```

- To run xFitter: `$> xfitter`

- To draw your results: `$> xfitter-draw  
HERAPDF20nnlo HERAPDF20nnlo-TevatronW`

[EPJC 75 \(2015\) 458](#)





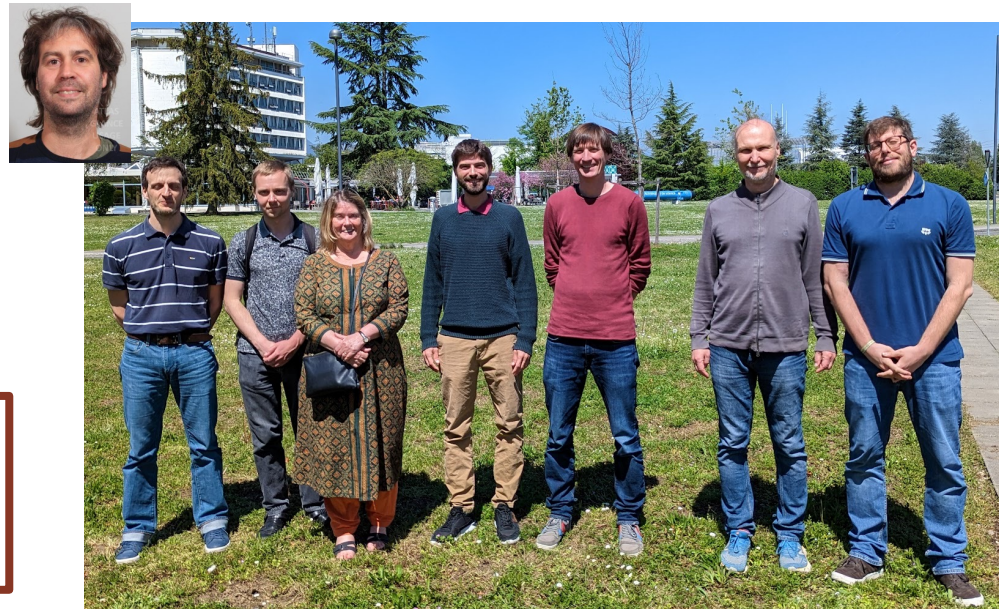
# Summary

- xFitter is **open-source QCD fit framework!** The program has many settings to address very different problems
- Big efforts have been made to keep the user interface accessible for simple and basic usage
- **Release 2.2.0** now out! (major update of evolution and reaction interfaces)
  - Modular and flexible! More examples in the '[examples](#)' folder
- The PDF world is amazing, fantastic and marvellous! ☺



## WE WANT YOU!

We are nice people! You should really consider the possibility to join and work with us! ☺



# ***Backup Slides***

---





# xFitter usage in the HEP community

## ➤ CMS:

- Multi-differential  $t\bar{t}$  cross sections at 13 TeV - [EPJC 80 \(2020\) 7 658](#)
- Extraction of PDFs,  $\alpha_s$  and contact-interactions from new inclusive jet cross section measurement at 13 TeV - [JHEP 02 \(2022\) 142](#) (more in this [talk](#))
- W+charm analysis at 8 TeV - [2112.00895](#)

- Strange quark PDF analysis with DIS HERA2 data, ATLAS W,Z cross-sections and ATLAS, CMS W+charm cross-sections - [PRD 104 \(2021\) 7 076004](#)

- NLO analysis of heavy-quark production cross-sections using **different mass renormalisation schemes** - [JHEP 04 \(2021\) 043](#)

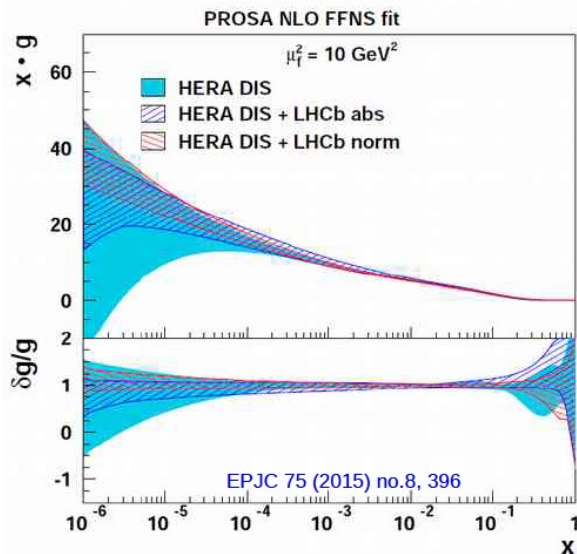
- **TMD parton densities** and corresponding parton showers: the advantage of four- and five-flavour schemes - [2106.09791](#)

- Implementation of **target mass corrections and higher-twist effects** in the xFitter framework - [PRD 101 \(2020\) 7 074015](#)

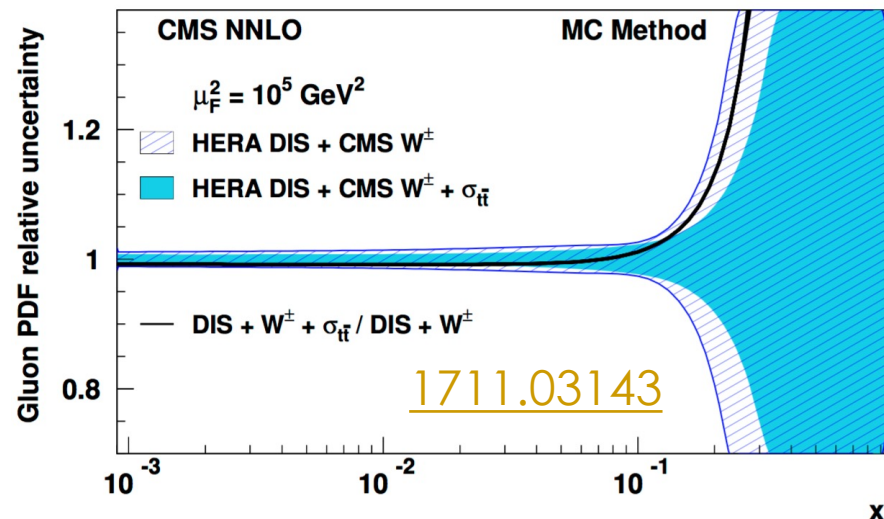
- NNLO PDFs with EW boson data from the LHC (**nuclear PDFs**) - [2112.11904](#)

# Results obtained with xFitter: Examples (2)

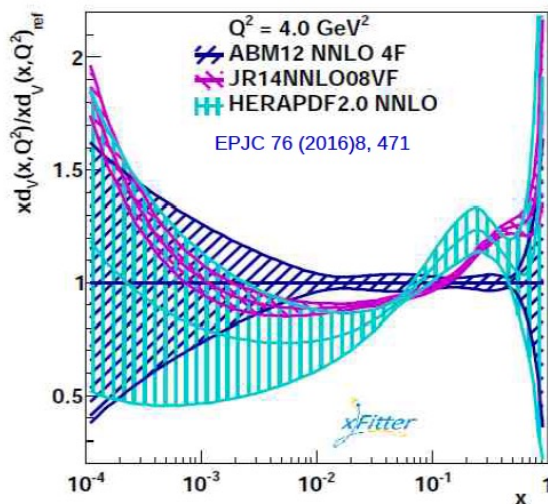
## Heavy quark production ( $ep, pp, p\bar{p}$ )



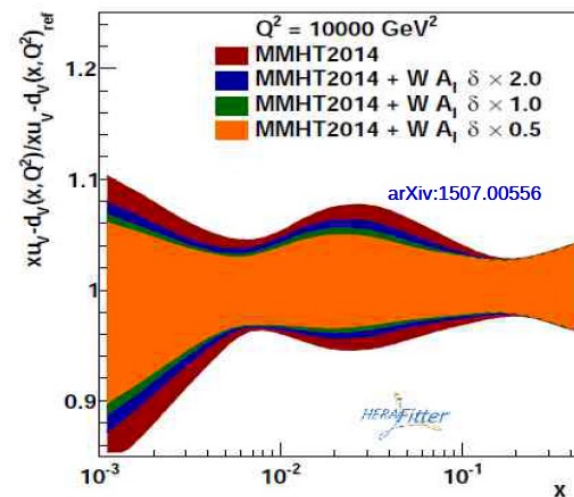
## Top-quark production ( $pp, p\bar{p}$ )



## Evolution of moder PDFs (benchmarking)



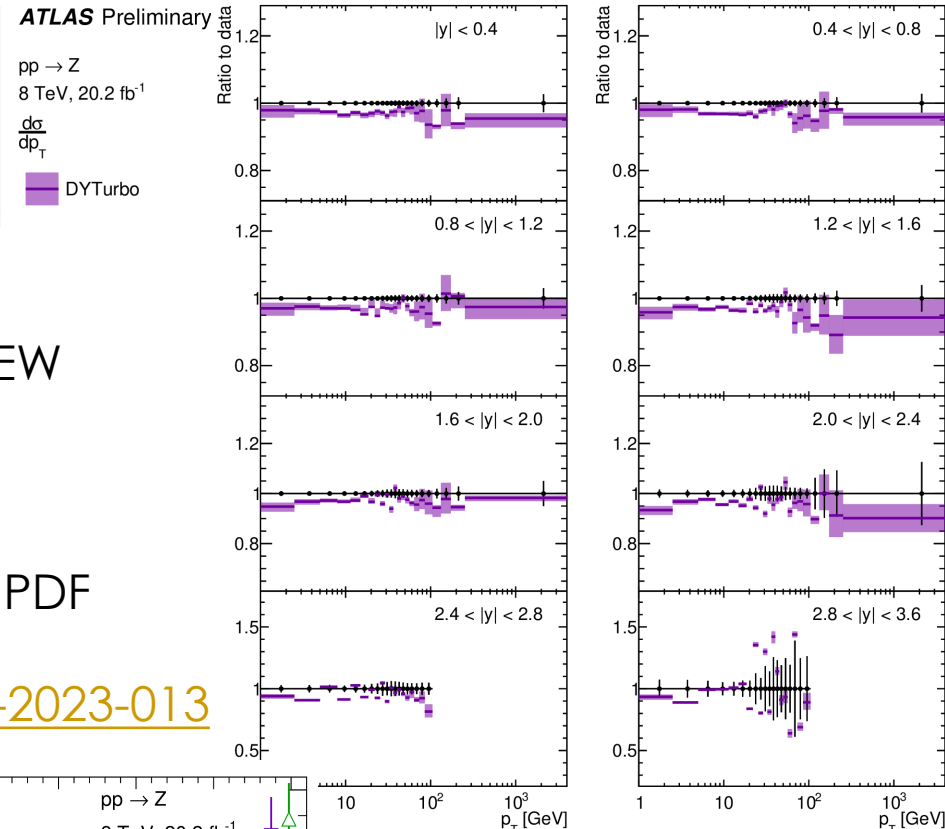
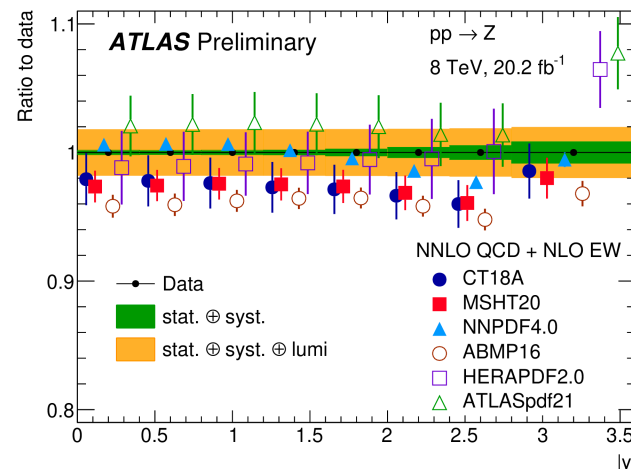
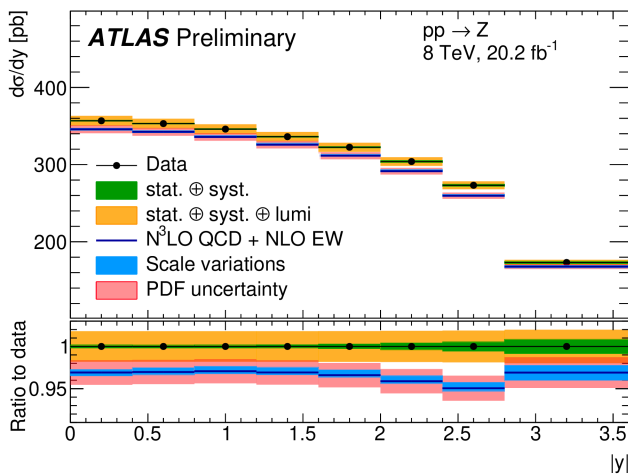
## PDF4LHC report (benchmarking)



# Z $p_T$ and rapidity at 8 TeV

- Per mille level precision in the central region
- Sub-percent precision up to  $|y| < 3.6$
- First comparison to N<sup>3</sup>LO QCD + NLO EW predictions ([DYPurbo](#) + [ReneSANCe](#))
- Allow precise PDF interpretations with QCD scale uncertainties smaller than PDF uncertainties

[ATLAS-CONF-2023-013](#)



**Good agreement  
with several high-  
order qT-resummed  
predictions**

# $\alpha_s$ extraction from $Z p_T$ at 8 TeV

- Evaluate  $\chi^2(\alpha_s)$  with  $\alpha_s$  variations in LHAPDF
  - Include experimental ( $\beta_{j,exp}$ ) and PDF uncertainties ( $\beta_{k,th}$ ) in the  $\chi^2(\alpha_s)$  definition
  - For each value of  $\alpha_s$ ,  $\beta_{k,th}$  terms explore the PDF space to find the best fit to  $Z p_T$  data
  - aN<sup>3</sup>LO MSHT20 PDF set is used for the  $\alpha_s$  extraction
- Fit  **$Z p_T < 29$  GeV region**
  - Non-perturbative form factor (affecting  $Z p_T < 5$  GeV) is added with unconstrained nuisance parameter
- $\alpha_s(m_Z)$  extracted by fitting the **2D ( $p_T$ ,  $y$ ) cross section** in full lepton phase space
- $\chi^2/ndf = 82/72$

$$\chi^2(\beta_{exp}, \beta_{th}) =$$

$$\sum_{i=1}^{N_{data}} \frac{\left( \sigma_i^{exp} + \sum_j \Gamma_{ij}^{exp} \beta_{j,exp} - \sigma_i^{th} - \sum_k \Gamma_{ik}^{th} \beta_{k,th} \right)^2}{\Delta_i^2} + \sum_j \beta_{j,exp}^2 + \sum_k \beta_{k,th}^2$$

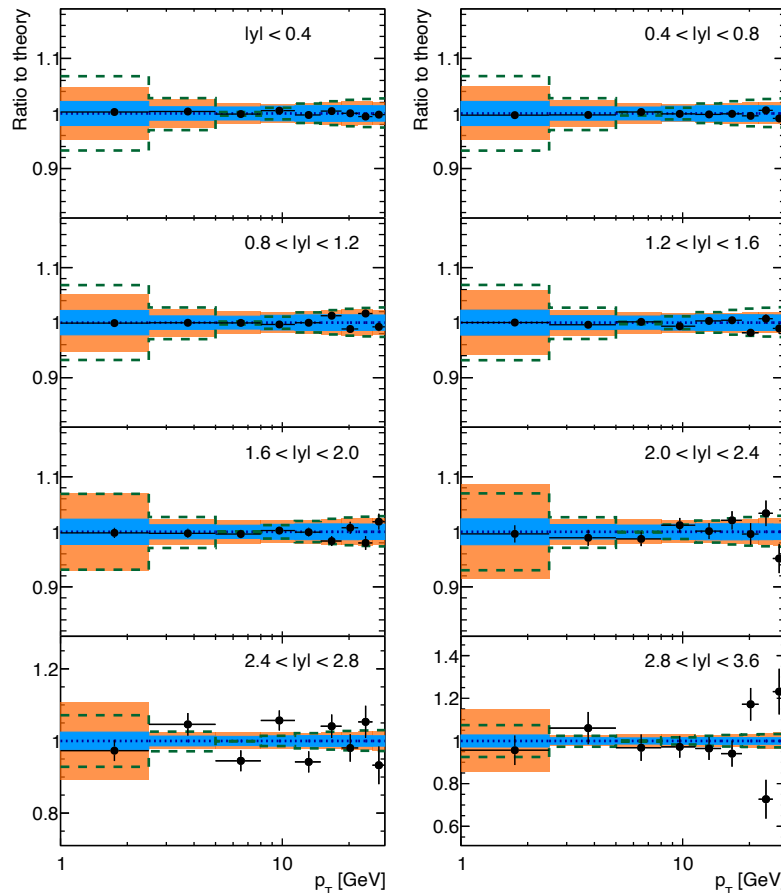
correlated systematic uncertainties

uncorrelated systematic uncertainties

ATLAS Preliminary

pp → Z  
8 TeV, 20.2 fb<sup>-1</sup>

• Data  
..... Post-fit  
■ PDF unc.  
■ PDF ⊕ Theory unc.  
- -  $\alpha_s(m_Z) \pm 0.002$

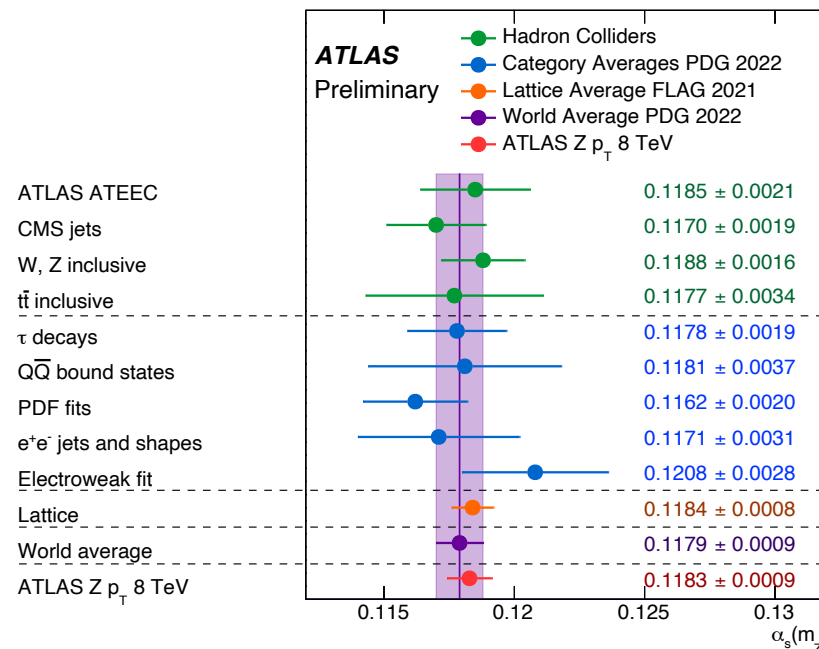
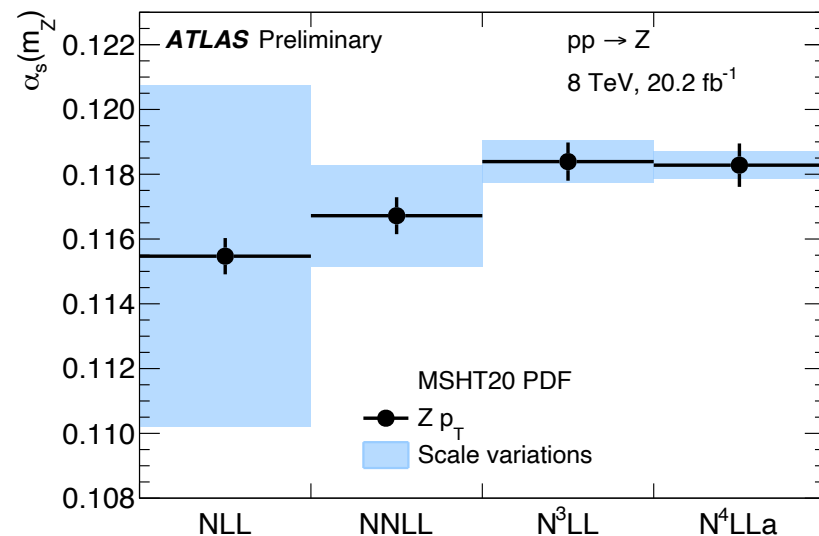


# Exercise 2 - results

- **First  $\alpha_s(m_Z)$  determination based on  $\alpha\text{N}^4\text{LL}+\text{N}^3\text{LO}$  predictions**
- $\alpha_s(m_Z)$  determined at lower orders  $\rightarrow$  good perturbative series convergence
- **Most precise experimental determination of  $\alpha_s(m_Z)$**
- ATLAS-CONF-2023-015

Experimental uncertainty	+0.00044	-0.00044
PDF uncertainty	+0.00051	-0.00051
Scale variations uncertainties	+0.00042	-0.00042
Matching to fixed order	0	-0.00008
Non-perturbative model	+0.00012	-0.00020
Flavour model	+0.00021	-0.00029
QED ISR	+0.00014	-0.00014
N4LL approximation	+0.00004	-0.00004
<b>Total</b>	<b>+0.00084</b>	<b>-0.00088</b>

$$\alpha_s(m_Z) = 0.11828^{+0.00084}_{-0.00088}$$

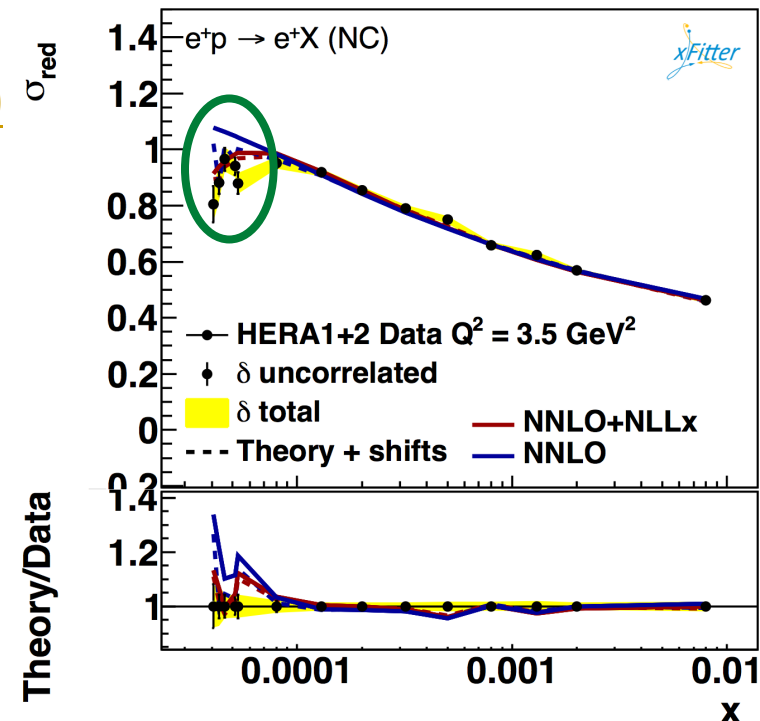


# EXERCISE 4

**Including small-x  
resummation corrections**

# Exercise 4

- **Purpose:** Test the impact of small- $x$  resummation corrections on PDFs
- **Data set:** Final combined HERA I+II DIS data
- **QCD order:** NNLO (+ NLL $x$ )
- Small- $x$  resummation formalism based on  **$k_T$ -factorization** and **BFKL**
- Developed in the 90s-00s
- Recent developments: [1607.02153](#), [1708.07510](#)
  - Resummation matched to NNLO, allowing NNLO+NLL $x$  phenomenology
  - Public code: [HELL](#)
  - Installed automatically with the provided [install-xFitter](#) script



# Small-x logarithmic enhancement

$$\sigma_{DIS} = C_i \otimes f_i$$

$$\mu^2 \frac{\partial}{\partial \mu^2} f_i(\mu) = P_{ij} \otimes f_j(\mu)$$

$$\text{LO} \quad \frac{1}{x} \alpha_S^0 \left[ \quad 1 \quad \right]$$

$$\text{NLO} \quad \frac{1}{x} \alpha_S \left[ \# \log \left( \frac{1}{x} \right) + \quad 1 \quad \right]$$

$$\text{NNLO} \quad \frac{1}{x} \alpha_S^2 \left[ \# \log^2 \left( \frac{1}{x} \right) + \# \log \left( \frac{1}{x} \right) + \quad 1 \quad \right]$$

$$\text{N}^3\text{LO} \quad \frac{1}{x} \alpha_S^3 \left[ \# \log^3 \left( \frac{1}{x} \right) + \# \log^2 \left( \frac{1}{x} \right) + \# \log \left( \frac{1}{x} \right) + \quad 1 \quad \right]$$

LL

NLL

NNLL

If  $\alpha_S \log \left( \frac{1}{x} \right) \sim 1 \rightarrow$  all such terms in the perturbative series are equally important

Reorganisation of the expansion:

$$\frac{1}{x} \left[ 1 + \# \alpha_S \log \left( \frac{1}{x} \right) + \# \alpha_S^2 \log^2 \left( \frac{1}{x} \right) + \# \alpha_S^3 \log^3 \left( \frac{1}{x} \right) + \dots \right] \quad (\text{LL})$$

$$\frac{\alpha_S}{x} \left[ 1 + \# \alpha_S \log \left( \frac{1}{x} \right) + \# \alpha_S^2 \log^2 \left( \frac{1}{x} \right) + \# \alpha_S^3 \log^3 \left( \frac{1}{x} \right) + \dots \right] \quad (\text{NLL})$$

**All-order resummation**



# Exercise 4 - settings

- `$> cd ~/xFitterTutorial/exercise4`
- Final combined HERA+II DIS data in `steering.txt`

`&InFiles`

`! Number of input files`

`NInputFiles = 7`

`! Input files:`

`InputFileNames =`

```
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_920-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_820-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_575-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_460-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCem-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCep-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_C Cem-thexp.dat',
```

`&End`

- Bonus: you can repeat this exercise with more data sets which are probing the low- $x$  region ☺ i.e. low mass or very forward DY,  $J/\psi$  or  $\Upsilon$  production etc.

# Exercise 4 - settings

- First, we change the program to evolve PDFs: from QCDNUM to APFEL
- Then:
  - We raise the charm matching scale  $\mu_c = \kappa_c \cdot m_c$  (with  $m_c = 1.43$  GeV), so it can be generated perturbatively
  - We switch on the small-x resummation

DefaultEvolution: proton-APFELff

Evolutions:

proton-APFELff:

```
? !include evolutions/APFEL.yaml
decomposition: proton
kmc : 1.2 # ratio between charm quark threshold and mass
nllxResummation : "On"
```

- We change HF scheme

byReaction:

# FONLL scheme settings:

FONLL\_DISNC:

```
? !include reactions/FONLL_DISNC.yaml
```

FONLL\_DISCC:

```
? !include reactions/FONLL_DISCC.yaml
```

# Specify HF scheme used for DIS NC processes:

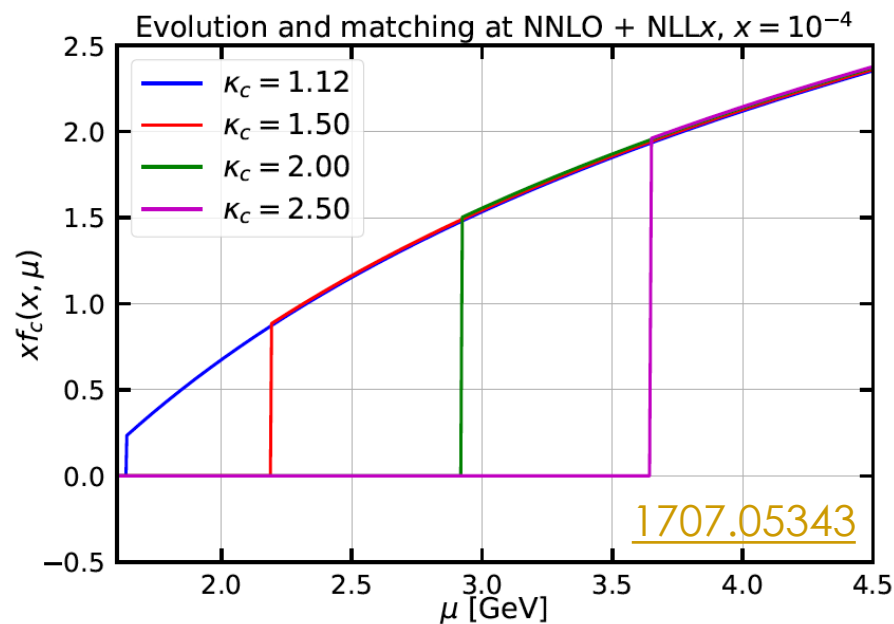
hf\_scheme\_DISNC :

```
defaultValue : 'FONLL_DISNC' # global specification
```

# Specify HF scheme used for DIS CC processes:

hf\_scheme\_DISCC :

```
defaultValue : 'FONLL_DISCC' # global specification
```



	NNLO	NNLO+NLLx
Total $\chi^2/\text{d.o.f}$	1388/1131	1316/1131

Gain in  $\chi^2$  of 72 units

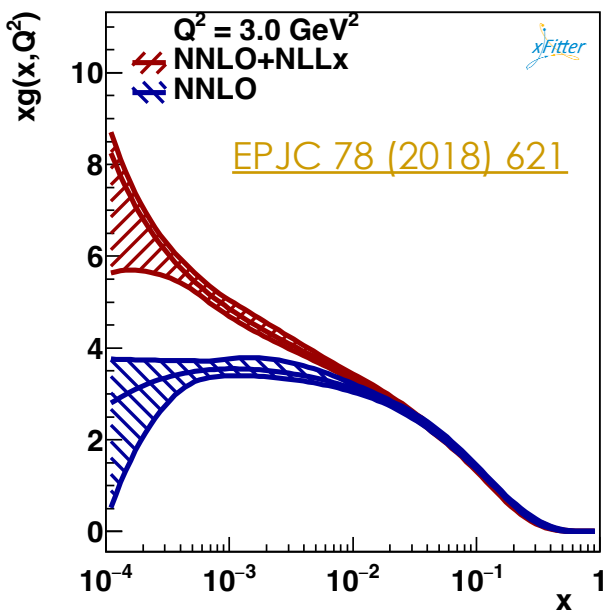
# Exercise 4 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You need to compare these PDFs with HERAPDF2.0 NNLO

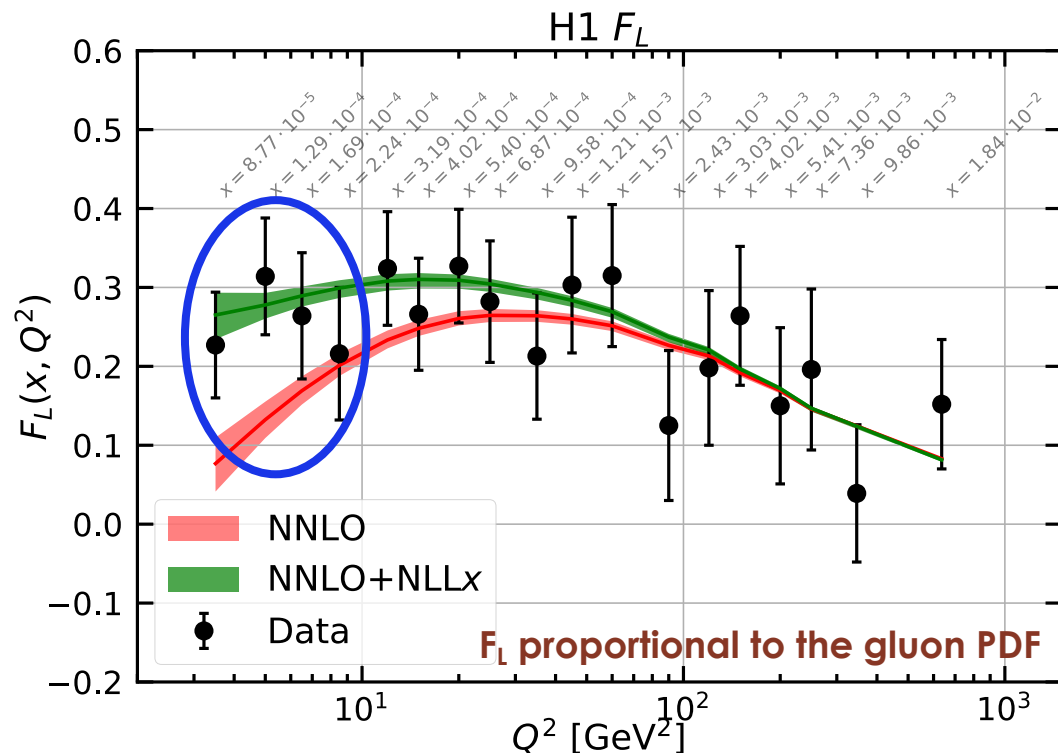
$$\sigma_{\text{red}} = F_2 - \frac{y^2}{Y_+} F_L$$

$$Y_+ = (1 + (1 - y)^2)$$

$$y = Q^2/(sx)$$



Other PDFs  
unaffected



# EXERCISE 5

**Add your preferred  
PDF parametrisation**

# Exercise 5

- **Purpose:** Test alternative PDF parametrisation
  - **Data set:** Final combined HERA I+II DIS data
  - **QCD order:** NNLO (+ NLLx)
  - To model small- $x$  region we proposed polynomial in  $\log(x)$   
 $(1 + F \log(x) + G \log^2(x) + H \log^3(x) + \dots)$
  - Considered both a multiplicative and an additive option, and we chose the latter:  
[EPJ Plus \(2019\) 134, 531](#)
- $$xf(x, \mu_0^2) = Ax^B(1-x)^C[1 + Dx + Ex^2 + F \log(x) + G \log^2(x) + H \log^3(x)]$$
- Public code: [HELL](#)
  - Installed automatically with the provided [install-xFitter](#) script
  - FYI this is just one possible alternative parametrisation → many more to test!  
Bernstein or Chebyshev polynomials etc.

# Exercise 5 - settings

- `$> cd ~/xFitterTutorial/exercise5`
- Final combined HERAI+II DIS data in `steering.txt`

`&InFiles`

`! Number of input files`

`NInputFiles = 7`

`! Input files:`

`InputFileNames =`

```
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_920-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_820-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_575-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_460-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCem-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCep-thexp.dat',  
'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCem-thexp.dat',
```

`&End`



# Exercise 5 - settings

- We need to modify the parametrization in `parameters.yaml`
- You can define as many parameters as you want
- You provide your preferred parametrization here

## Parameterisations:

```

par_uv:
  class: Expression
  expression: "Auv*(x^Buv*(1-x)^Cuv)*(1+Euv*x^2+Fuv*ln(x)+Guv*ln(x)^2)"
par_dv:
  class: Expression
  expression: "Adv*(x^Bdv*(1-x)^Cdv)"
par_ubar:
  class: Expression
  expression: "Adbar*(x^Bdbar*(1-x)^Cubar)*(1+Dubar*x+Fdbar*ln(x))"
par_dbar:
  class: Expression
  expression: "Adbar*(x^Bdbar*(1-x)^Cdbar)*(1+Ddbar*x+Fdbar*ln(x))"
par_s:
  class: Expression
  expression: "Adbar*fs/(1-fs)*(x^Bdbar*(1-x)^Cdbar)*(1+Ddbar*x+Fdbar*ln(x))"
par_g:
  class: Expression
  expression: "Ag*(x^Bg*(1-x)^Cg)*(1+Fg*ln(x)+Gg*ln(x)^2)"

```

## Parameters:

```

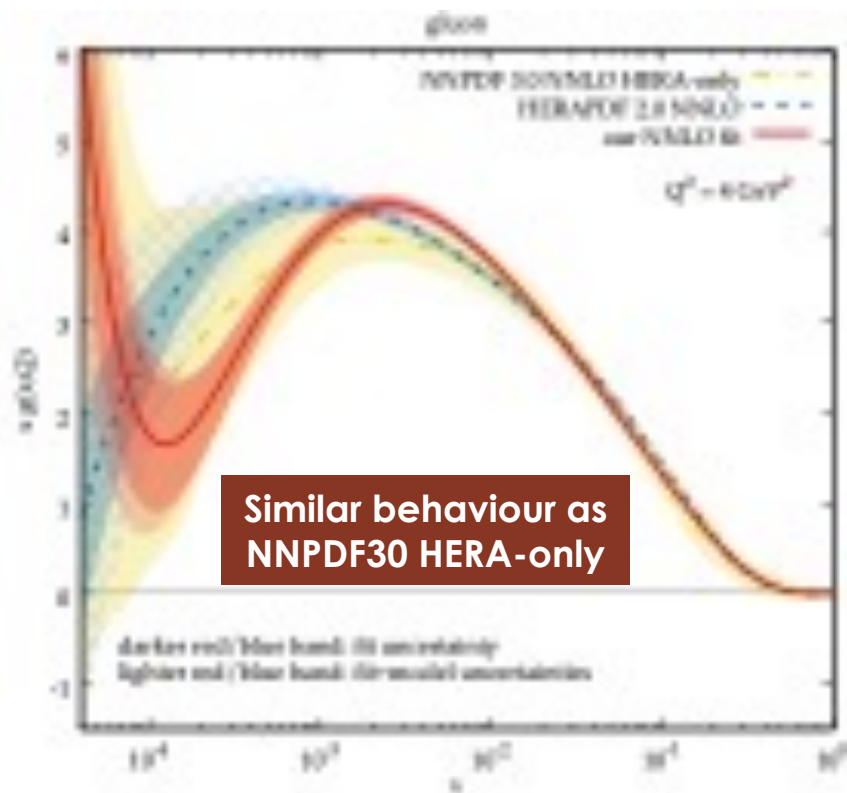
Ag  : DEPENDENT
Bg  : [ -0.5009, 0.0060 ]
Cg  : [ 4.4885, 0.1944 ]
Fg  : [ 0.2156, 0.0005 ]
Gg  : [ 0.0119, 0.0010 ]
Auv : DEPENDENT
Buv : [ 0.7392, 0.0021 ]
Cuv : [ 4.5845, 0.0170 ]
Euv : [ 2.7839, 0.0633 ]
Fuv : [ 0.3416, 0.0027 ]
Guv : [ 0.0470, 0.0040 ]
Adv : DEPENDENT
Bdv : [ 0.9882, 0.0108 ]
Cdv : [ 4.6983, 0.0742 ]
Cubar: [ 10.9607, 0.2749 ]
Dubar: [ 17.2935, 0.2808 ]
Adbar: [ 0.0854, 0.0241 ]
Bdbar: [ -0.3354, 0.0031 ]
Cdbar: [ 23.8266, 0.9917 ]
Ddbar: [ 35.0368, 4.5302 ]
Fdbar: [ 0.0744, 0.0011 ]
ZERO : 0
fs  : [ 0.4, 0.0 ]

```

- You can also switch on small-x resummation (see Exercise 4) to check if any improvement in  $\chi^2$

# Exercise 5 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You need to compare these PDFs with HERAPDF2.0 NNLO



Contribution to $\chi^2$	HERAPDF2.0	Our fit (new parametrization)
subset NC $e^+$ 920 $\tilde{\chi}^2/\text{n.d.p.}$	444/377	403/377
subset NC $e^+$ 820 $\tilde{\chi}^2/\text{n.d.p.}$	66/70	74/70
subset NC $e^+$ 575 $\tilde{\chi}^2/\text{n.d.p.}$	219/254	221/254
subset NC $e^+$ 460 $\tilde{\chi}^2/\text{n.d.p.}$	217/204	222/204
subset NC $e^-$ $\tilde{\chi}^2/\text{n.d.p.}$	219/159	220/159
subset CC $e^+$ $\tilde{\chi}^2/\text{n.d.p.}$	45/39	38/39
subset CC $e^-$ $\tilde{\chi}^2/\text{n.d.p.}$	56/42	50/42
correlation term + log term	91 + 5	75 - 3
<b>Total <math>\chi^2/\text{d.o.f.}</math></b>	<b>1363/1131</b>	<b>1301/1127</b>

- If small- $x$  resummation included, further gain of 28 units in  $\chi^2$
- **The addition of small- $x$  resummation is thus very important**



# EXERCISE 6

**ATLASepWZ16: fixed vs free  $r_s$**

## Exercise 6

- **Purpose:** Reproduce the ATLASepWZ16 fit results and  $\chi^2$  comparison for two different cases → fixed VS free  $r_s$
- **Data set:** Final combined HERAI+II DIS data and ATLAS W,Z precise measurement at 7 TeV
- Below the datasets we need to add to the steering.txt file:

```
'datafiles/lhc/atlas/wzProduction/1612.03016/wminus-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/wplus-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zyhigh_cc-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zyhigh_cf-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zypeak_cc-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zypeak_cf-thexp.dat',
```
- We also need to apply a cut on the minimum  $Q^2$  of the data to enter the fit to be greater than 10 GeV – so we are not sensitive to non-perturbative effects i.e. higher-twist, small-x logarithmic enhancement, etc.
- Do you remember how to do it?
  - Hint: look inside `steering.txt` ☺

## Exercise 6

- Two different folders:

```
$> cd ~/xFitterTutorial/exercise6/rsFixed  
$> cd ~/xFitterTutorial/exercise6/rsFree
```

$$r_s = \frac{f_s}{1 - f_s}$$

$$f_s = \frac{r_s}{1 + r_s}$$

- Then, we have to freeze/free  $r_s$  parameter in the `parameters.yaml` file
- ATLASepWZ16  $\rightarrow r_s \sim 1.19$  so  $f_s \sim 0.54$

Parameters:

```
rs : [ 1.1007, 0.1785 ]
```

Proposed range to scan:  
 $0.91 < r_s < 1.21$

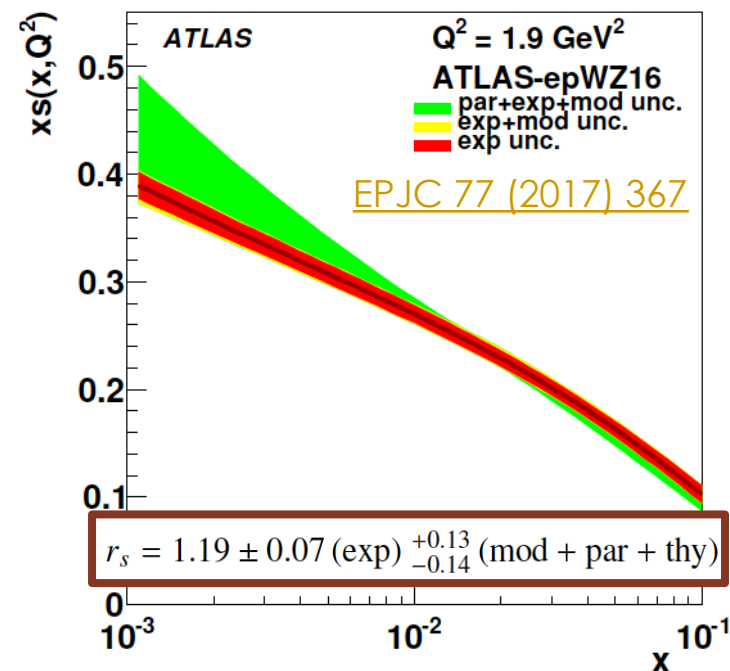
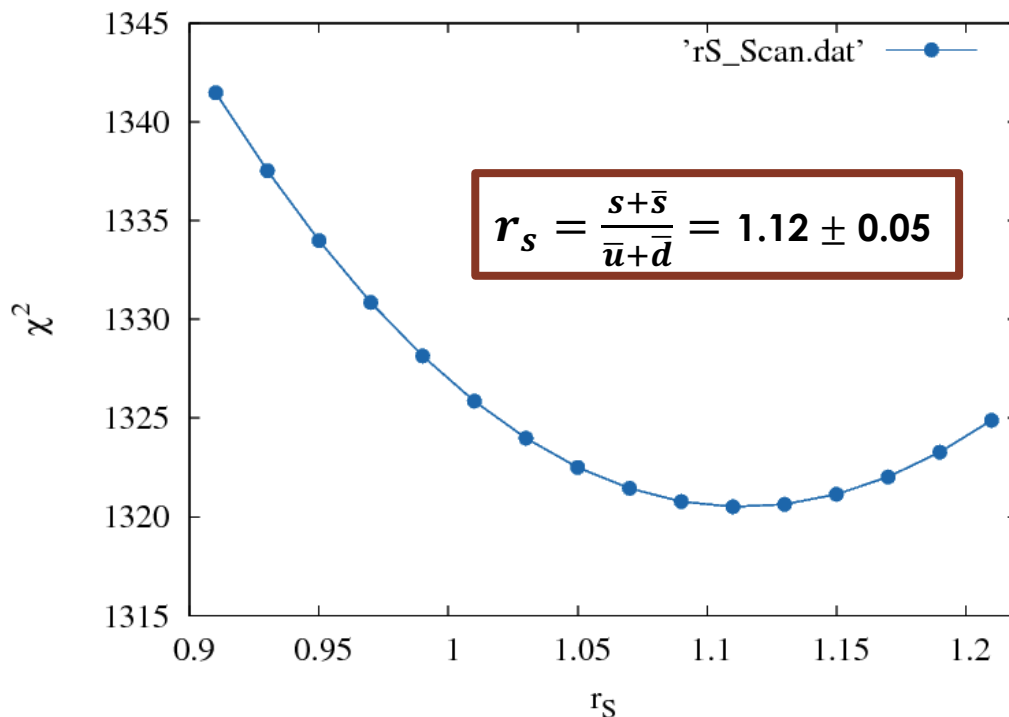
- FYI in HERAI+II  $\rightarrow f_s = 0.4$  (fixed) so  $r_s \sim 0.667$
- To obtain datafiles: 

```
$> ln -s ~/Software/xfitter-master/datafiles .
```
- To run xFitter: 

```
$> xfitter
```
- To draw your results: 

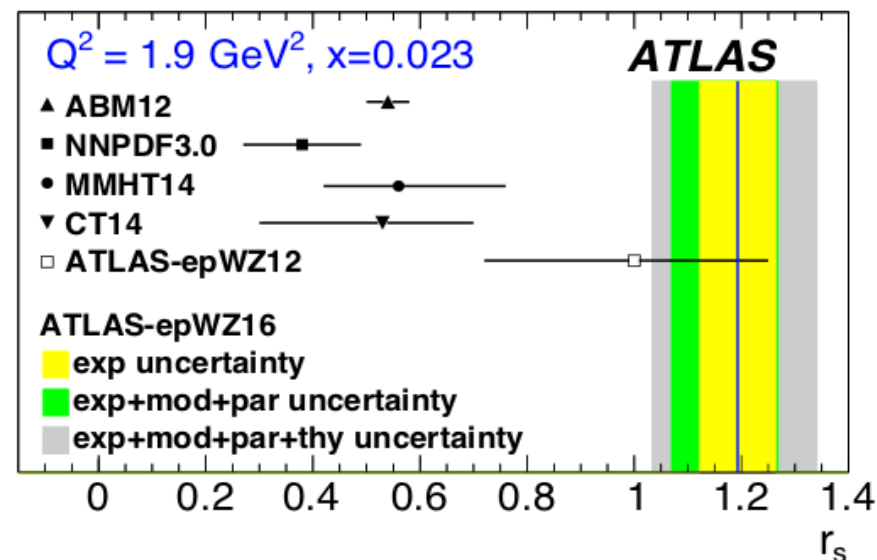
```
$> xfitter-draw rsFixed rsFree
```

# Exercise 6 - Results



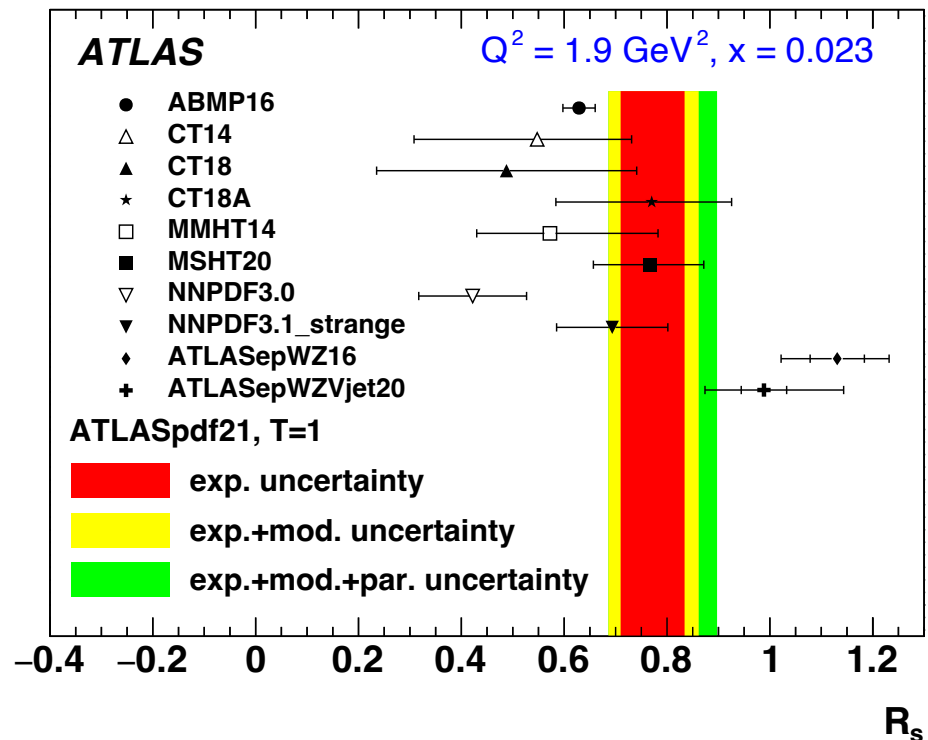
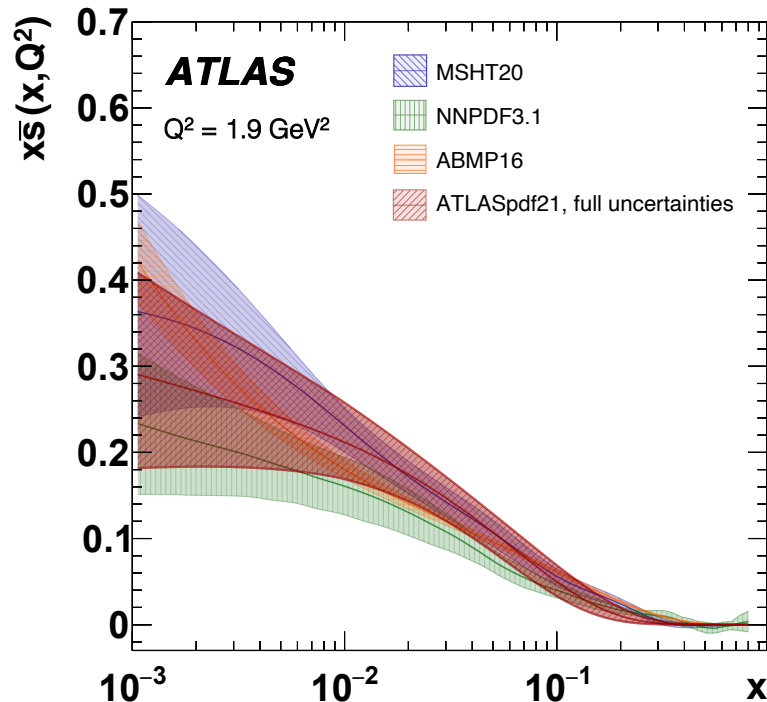
Enhanced  $r_s$  confirmed!

The two approaches  
give compatible results



# Exercise 6 - bonus

- What happens if you start adding more and more ATLAS data?
- **ATLASpdf21** is a PDF fit to **multiple ATLAS data sets** - [EPJC 82 \(2022\) 5, 438](#)
  - [Fit example](#) + [data files](#) (to reproduce published results)
- **ATLAS  $r_s$**  has come **DOWN** from  $\sim 1.2$  to 0.8
- **MSHT, CT** and **NNPDF  $r_s$**  have come **UP** from  $\sim 0.5$  to 0.8 when including W,Z 7 TeV ATLAS data



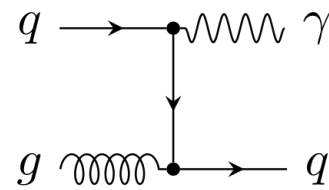
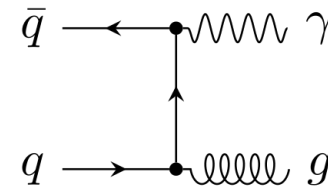
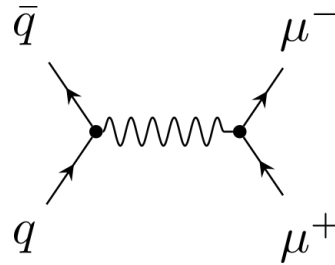
# EXERCISE 7

## Charged pion PDF

# Exercise 7

➤ **Purpose:** Extract the charged pion PDF (poorly studied experimentally)

➤ **Data set:** Data from **E615**, **NA10** and **WA70** experiments (di-muon and direct photon production)



➤ Charge symmetry  $d = \bar{u}$  and SU(3)-symmetric sea  $u = \bar{d} = s = \bar{s}$  at the initial scale  $Q_0^2 = 1.9 \text{ GeV}^2$

$$v := (d - \bar{d}) - (u - \bar{u}),$$

$$S := 2u + 2\bar{d} + s + \bar{s} = 6u,$$

$$g := g,$$

$$xv(x) = A_v x^{B_v} (1-x)^{C_v} (1 + D_v x^{\frac{5}{2}}),$$

$$xs(x) = A_s x^{B_s} (1-x)^{C_s},$$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g}.$$

➤ The  $A_v$  and  $A_g$  parameters are determined by the sum rules:

$$\int_0^1 v(x) dx = 2,$$

$$\int_0^1 x(v(x) + S(x) + g(x)) dx = 1$$

# Exercise 7 - settings

➤ `$> cd ~/xFitterTutorial/exercise7`

➤ We need to add data from **E615**, **NA10** and **WA70** experiments in the `steering.txt` file

`InputFileNames =`

```
'datafiles/fixedTarget/NA10/thexp-0.dat',
'datafiles/fixedTarget/NA10/thexp-1.dat',
'datafiles/fixedTarget/NA10/thexp-2.dat',
'datafiles/fixedTarget/NA10/thexp-3.dat',
'datafiles/fixedTarget/NA10/thexp-4.dat',
'datafiles/fixedTarget/NA10/thexp-5.dat',
'datafiles/fixedTarget/NA10/thexp-6.dat',
'datafiles/fixedTarget/NA10/thexp-7.dat',
'datafiles/fixedTarget/NA10/thexp-8.dat',
'datafiles/fixedTarget/WA70/thexp-0.dat',
'datafiles/fixedTarget/WA70/thexp-1.dat',
'datafiles/fixedTarget/WA70/thexp-2.dat',
'datafiles/fixedTarget/WA70/thexp-3.dat',
'datafiles/fixedTarget/WA70/thexp-4.dat',
'datafiles/fixedTarget/WA70/thexp-5.dat',
'datafiles/fixedTarget/WA70/thexp-6.dat',
'datafiles/fixedTarget/WA70positive/thexp-0.dat',
'datafiles/fixedTarget/WA70positive/thexp-1.dat',
'datafiles/fixedTarget/WA70positive/thexp-2.dat',
'datafiles/fixedTarget/WA70positive/thexp-3.dat',
'datafiles/fixedTarget/WA70positive/thexp-4.dat',
'datafiles/fixedTarget/WA70positive/thexp-5.dat',
'datafiles/fixedTarget/WA70positive/thexp-6.dat',
```

```
'datafiles/fixedTarget/NA10-286/thexp-0.dat',
'datafiles/fixedTarget/NA10-286/thexp-1.dat',
'datafiles/fixedTarget/NA10-286/thexp-2.dat',
'datafiles/fixedTarget/NA10-286/thexp-3.dat',
'datafiles/fixedTarget/NA10-286/thexp-4.dat',
'datafiles/fixedTarget/NA10-286/thexp-5.dat',
'datafiles/fixedTarget/NA10-286/thexp-6.dat',
'datafiles/fixedTarget/NA10-286/thexp-7.dat',
'datafiles/fixedTarget/NA10-286/thexp-8.dat',
'datafiles/fixedTarget/NA10-286/thexp-9.dat',
'datafiles/fixedTarget/NA10-286/thexp-10.dat',
'datafiles/fixedTarget/E615/thexp-0.dat',
'datafiles/fixedTarget/E615/thexp-1.dat',
'datafiles/fixedTarget/E615/thexp-2.dat',
'datafiles/fixedTarget/E615/thexp-3.dat',
'datafiles/fixedTarget/E615/thexp-4.dat',
'datafiles/fixedTarget/E615/thexp-5.dat',
'datafiles/fixedTarget/E615/thexp-6.dat',
'datafiles/fixedTarget/E615/thexp-7.dat',
'datafiles/fixedTarget/E615/thexp-8.dat',
'datafiles/fixedTarget/E615/thexp-9.dat',
'datafiles/fixedTarget/E615/thexp-13.dat',
'datafiles/fixedTarget/E615/thexp-14.dat',
'datafiles/fixedTarget/E615/thexp-15.dat',
'datafiles/fixedTarget/E615/thexp-16.dat',
'datafiles/fixedTarget/E615/thexp-17.dat',
```



# Exercise 7 - settings

- We need to modify the parametrization in `parameters.yaml`, as well as decomposition

## Parameters:

```
Av: SUMRULE
Bv: [ 0.75,0.03]
Cv: [ 0.95,0.04, 0,10]
As: [ 0.21,0.1]
Bs: [ 0.5 ,0.1,-1,10]
Cs: [ 8,3]
Ag: SUMRULE
Bg: 0
Cg: [ 3,1]
```

## Parameterisations:

```
v:
  class: HERAPDF
  parameters: [Av,Bv,Cv]
S:
  class: Normalized
  parameters: [As,Bs,Cs]
g:
  class: Normalized
  parameters: [Ag,Bg,Cg]
```

## Decompositions:

```
pion:
  class: SU3_Pion
  valence: v
  sea: S
  gluon: g
```

- We also need to change evolution, and define it for both  $\pi^+$  and  $\pi^-$

## Evolutions:

```
negative_pion:
  ? !include evolutions/QCDNUM.yaml
  decomposition: pion
```

```
positive_pion:
  class: FlipCharge
  input: negative_pion
```

```
tungsten_target:
  class: LHAPDF
  set: nCTEQ15FullNuc_184_74
  member: 0
proton:
  class: LHAPDF
  set: nCTEQ15FullNuc_1_1
  member: 0
```

```
DefaultEvolution: negative_pion
```

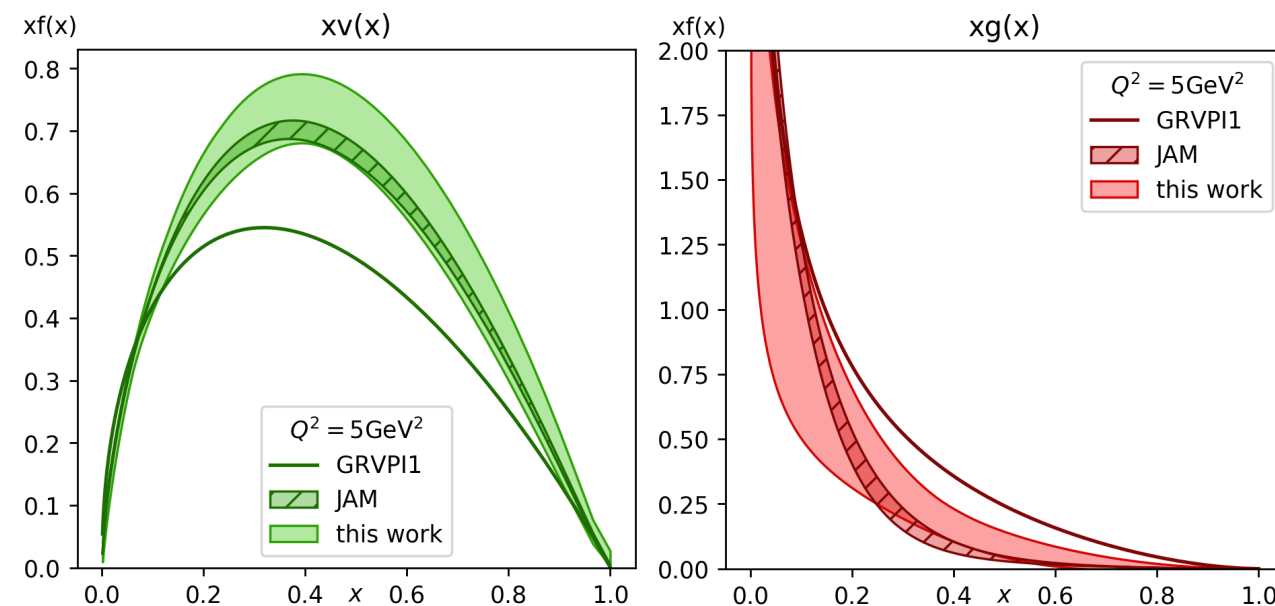
Nice feature! In this way you have the same evolution used for  $\pi^-$ , just with inverted charged

We have to define a nuclear PDF set for both the incoming proton and the target (tungsten in this case)

# Exercise 7 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You need to compare these PDFs with i.e. JAM or GRVPI1
- Valence and gluon distributions in good agreement with JAM and both disagree with the early GRV analysis

[Phys. Rev. D 102 \(2020\) 014040](#)



Experiment	$\chi^2/N_{\text{points}}$
E615	194/140
NA10 (194 GeV)	98/67
NA10 (286 GeV)	92/73
WA70	74/99

# EXERCISE 8

## Charged pion Fragmentation Functions

# Exercise 8

- **Purpose:** Extract the charged pion **fragmentation functions** (FFs)
- **Data set:** Single inclusive electron-positron annihilation (SIA) + BELLE13/20 data
- **Parametrization form:** 
$$D_i^{\pi^\pm}(z, Q_0) = \frac{\mathcal{N}_i z^{\alpha_i} (1-z)^{\beta_i} [1 + \gamma_i (1-z)^{\delta_i}]}{B[2+\alpha_i, \beta_i+1] + \gamma_i B[2+\alpha_i, \beta_i+\delta_i+1]}$$
- We assume isospin symmetry  $D_u^{\pi^+} = D_{\bar{d}}^{\pi^-}$  and  $D_{\bar{u}}^{\pi^+} = D_d^{\pi^-}$
- We assume the charge conjugate  $D_i^{\pi^+} = D_i^{\pi^-}$  for all the flavour component
- We fit the flavour combinations  $i = u^+, d^+, s^+, c^+, b^+$  and  $g$
- We parametrise FFs at a starting scale of  $Q_0^2 = 5 \text{ GeV}^2$
- **19 free parameters in total**
- Fitted distributions:  $\frac{d\sigma^h}{dz}, \frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}, \frac{s}{\beta} \frac{d\sigma^h}{dz}, \frac{1}{\beta\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}, \dots$  (  $z = 2E_h/\sqrt{s}$  )

# Exercise 8 - settings

➤ `$> cd ~/xFitterTutorial/exercise8`

➤ We need to add SIA and BELLE13/20 data in the `steering.txt` file

```
NInputFiles = 17
InputFileNames =
! Input files:
!   4 active flavour
      'datafiles/NC_SIA/BABAR/inclusive/BABAR_inclusive_pi_o.dat',
      'datafiles/NC_SIA/BELLE20/BELLE20_inclusive_pi_1.dat'

!   Inclusive
      'datafiles/NC_SIA/ALEPH/inclusive/ALEPH_inclusive_pi_h.dat',
      'datafiles/NC_SIA/DELPHI/inclusive/DELPHI_inclusive_pi.dat',
      'datafiles/NC_SIA/OPAL/inclusive/OPAL_inclusive_pi.dat',
      'datafiles/NC_SIA/SLD/inclusive/SLD_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_12_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_14_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_22_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_34_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_44_inclusive_pi.dat',
      'datafiles/NC_SIA/TPC/TPC_inclusive_pi.dat',

!   b tag
      'datafiles/NC_SIA/DELPHI/b_tag/DELPHI_b_tag_pi.dat',
      'datafiles/NC_SIA/SLD/b_tag/SLD_b_tag_pi.dat',

!   c tag
      'datafiles/NC_SIA/SLD/c_tag/SLD_c_tag_pi.dat',

!   light tag
      'datafiles/NC_SIA/DELPHI/light_tag/DELPHI_light_tag_pi_o.dat',
      'datafiles/NC_SIA/SLD/light_tag/SLD_light_tag_pi.dat',
```

# Exercise 8 - settings

- We need to modify the parametrization in `parameters.yaml`, as well as decomposition

## Parameters:

```
ABp : [ 1.0199, 0.01618693 ]
ACp : [ 1.1305, 0.01827819 ]
ASp : [ 0.7049, 0.09370628 ]
Ag : [ 2.0073, 0.03766856 ]
Aup : [ 1.4261, 0.04923525 ]
BBp : [ -0.4543, 0.04601485 ]
BCp : [ -1.0443, 0.04583320 ]
BSp : [ -0.5754, 0.55702822 ]
Bg : [ 3.3722, 0.37066418 ]
Bup : [ -0.7829, 0.04777496 ]
CBp : [ 3.9881, 0.22672656 ]
CCp : [ 4.6312, 0.16315390 ]
CSp : [ 8.7524, 1.01469245 ]
Cg : [ 58.3529, 3.15872362 ]
Cup : [ 1.6871, 0.02898839 ]
DBp : [ 17.0749, 1.31370713 ]
DCp : [ 0.00000000, 0.00000000 ]
DSp : [ 0.00000000, 0.00000000 ]
Dg : [ 0.00000000, 0.00000000 ]
Dup : [ 5.1060, 0.61927213 ]
EBp : [ 9.0314, 0.68378218 ]
ECp : [ 0.00000000, 0.00000000 ]
ESp : [ 0.00000000, 0.00000000 ]
Eg : [ 0.00000000, 0.00000000 ]
Eup : [ 4.0594, 0.32218262 ]
ZERO : [ 0.00000000, 0.00000000 ]
```

## Parameterisations:

```
par_up:
  class: Pion_FF
  parameters: [Aup,Bup,Cup,Dup,Eup]
par_cp:
  class: Pion_FF
  parameters: [ACp,BCp,CCp,DCp,ECp]
par_bp:
  class: Pion_FF
  parameters: [ABp,BBp,CBp,DBp,EBp]
par_sp: # s=fs/(1-fs) * Dbar
  class: Pion_FF
  parameters: [ASp,BSp,CSp,DSp,ESp]
par_g:
  class: Pion_FF
  parameters: [Ag,Bg,Cg,Dg,Eg]
```

DefaultDecomposition: `Pion_FF_B_C`

## Decompositions:

```
Pion_FF_B_C: #proton:
  class: Pion_FF_BC
  xup: par_up
  xcp: par_cp
  xbp: par_bp
  xsp: par_sp
  xg: par_g
```

DefaultEvolution: `proton-APFELff`

## Evolutions:

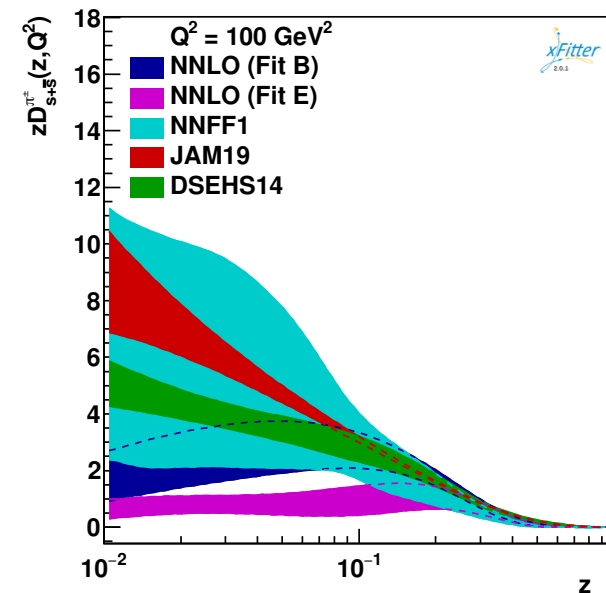
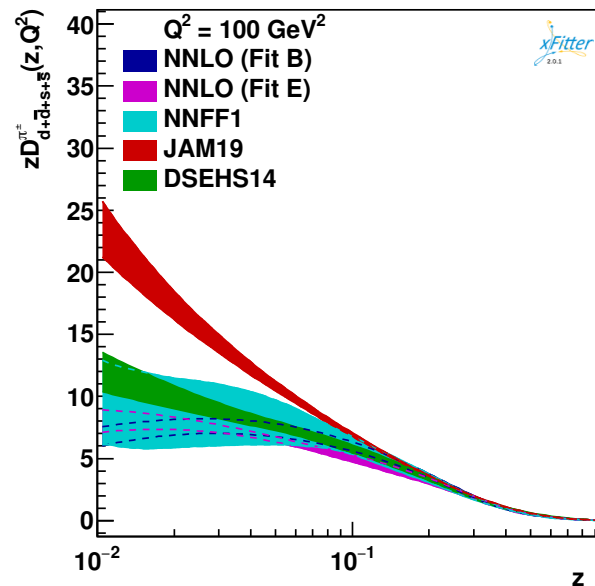
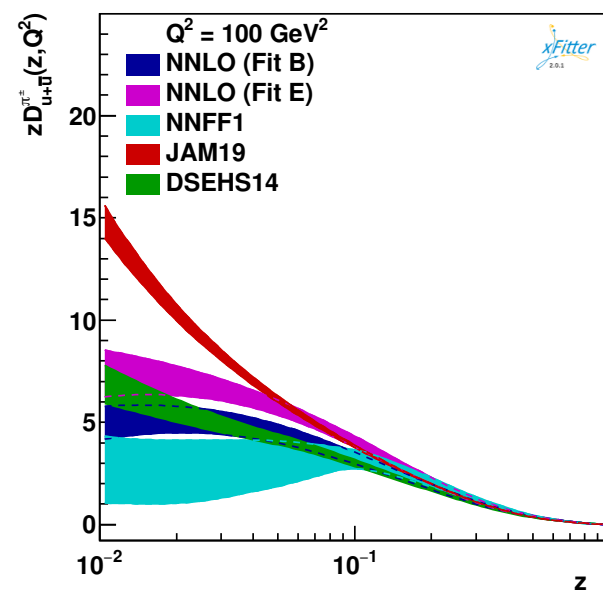
```
proton-APFELff:
  ? !include evolutions/APFEL.yaml
  fragmentation : "on"
  decomposition: Pion_FF_B_C #proton
proton-LHAPDF:
  class: LHAPDF
  set: "NNPDF30_nlo_as_0118"
  #set: "CT10nlo"
  member: 0
antiproton:
  class: FlipCharge
  #input: proton-QCDNUM
  input: proton-LHAPDF
```

- We also need to change evolution – to study antiproton, we used the same trick used for  $\pi^+$  in Exercise 7 (FlipCharge)

# Exercise 8 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You can compare these PDFs with NNLO NNFF1 and NLO JAM19 and DSEHS14
- **Generally compatible with NNFF1 and DSEHS14 at larger  $z$ , but they differ at low- $z$  (more pronounced for Fit E)**

[PRD 104 \(2021\) 5 056019](#)





# How to generate fixed order predictions

- First of all, you need to download APPLgrid from [here](#)
  - You can download the latest version available 1.6.32
- Then you need to download aMC@NLO from [here](#)
  - I would recommend you to download version 2.9.X/3.5.X (standard in ATLAS)
- After having installed aMC@NLO you need to generate the process you want to simulate, so e.g.  $p p \rightarrow l \nu l$ . An example set of commands might be:

```
import model loop_sm-no_b_mass
define p = p b b~
define j = p
define l = e+ e- mu+ mu-
define vl = ve ve~ vm vm~
generate p p > l vl [NLO]
output run_Wlnu
```

If you have doubts, please follow the instructions on any MG5\_aMC@NLO tutorial to produce this process

- Then download aMCfast and follow the instructions described [here](#)
- At this stage, you need to write your analysis file (I would suggest the top-drawer format). You have lots of examples in the FOAnalysis folder, please have a look there
  - It is in fortran, but it should be pretty straightforward to understand how to define new distribution



# How to generate fixed order predictions

- Then you have to run first a preparatory run

- To perform this preparatory run, we set in the run card

```
1 = iappl ! aMCfast switch (0=OFF, 1=prepare APPLgrids, 2=fill grids)
```

- Since at this stage the interpolation grids are not filled up, there is no need of a high accuracy, thus setting something like `0.01 = req_acc_F0` in the run card is enough

- If the run finishes successfully, the code will have created the starting grid that now need to be filled up. So we have to run again the code giving: `launch -o` ("-o" ensures that the code restarts the run from the grids generated in the previous run)

- Now for this second run, we only need to edit the run card and to set:

```
2 = iappl ! aMCfast switch (0=OFF, 1=prepare APPLgrids, 2=fill grids)
```

- In addition, we might want to increase the accuracy of the integration by setting, for example: `0.001 = req_acc_F0`

- Requiring an higher accuracy should get rid of the statistical fluctuation