

# **Static Distortion Update**

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# Comparison between Direct Laser Data and Statics Distortion Model Calculation

- Apply the likelihood-fit method to direct-laser data to obtain both straight-line and Bézier fits.
- Apply the current calculated static-distortion map to the straight-line fit to obtain the distortion-shifted trajectory.
  - Straight-line fit as approximation of baseline.
  - The input static-distortion map: `$CALIBRATIONROOT/distortion_maps/static_only_inverted_10-new.root`
- Compare the distortion-shifted trajectory with the real data and the Bézier likelihood fit.

# Polynomial Fit Method in 3D

- To better describe the Laser Track in the real data, we use Cubic Bézier (degree 3) Polynomial Curve in 3D to fit:

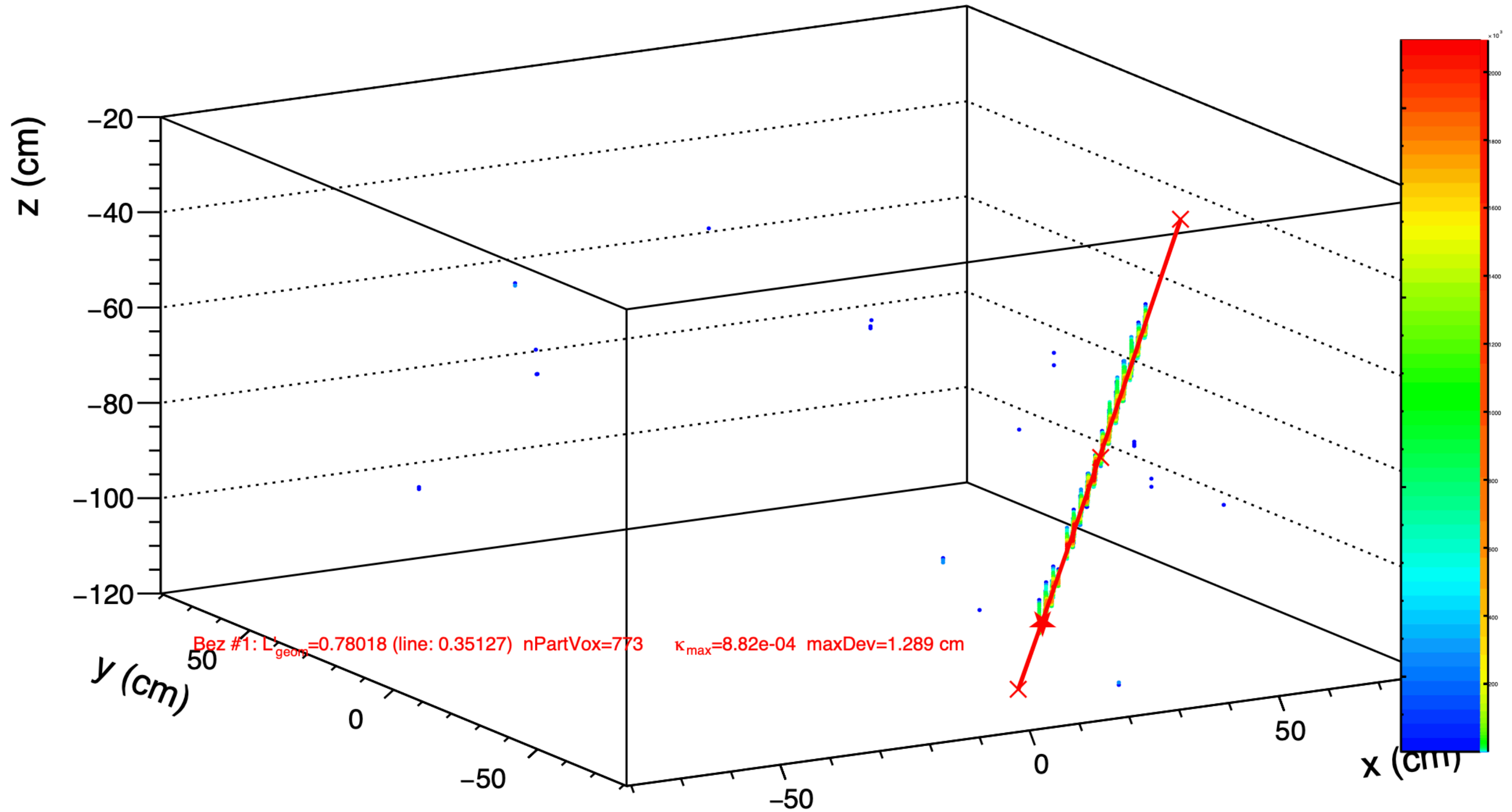
$$\mathbf{B}(t) = (1 - t)^3 \mathbf{P}_0 + 3(1 - t)^2 t \mathbf{P}_1 + 3(1 - t) t^2 \mathbf{P}_2 + t^3 \mathbf{P}_3$$

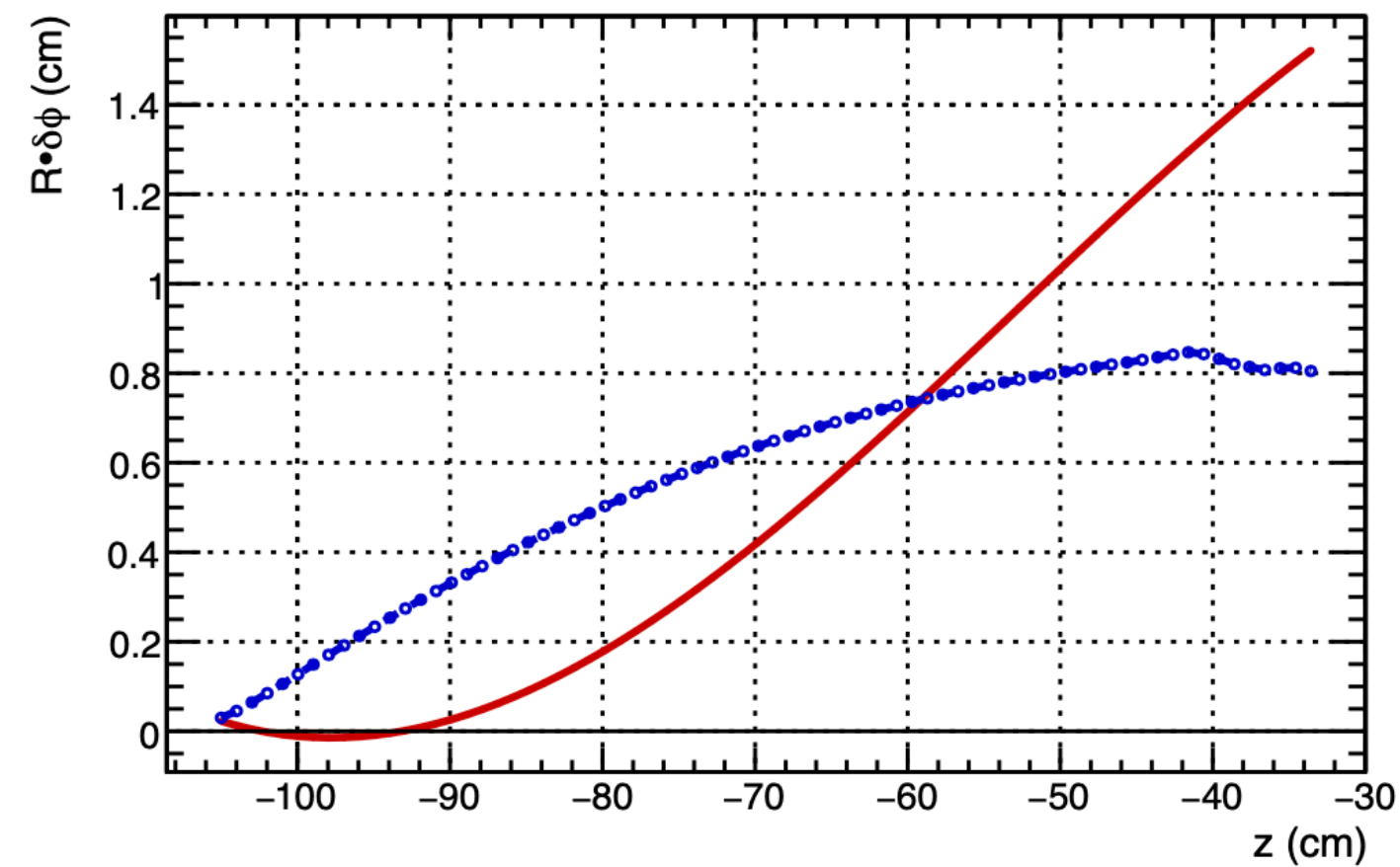
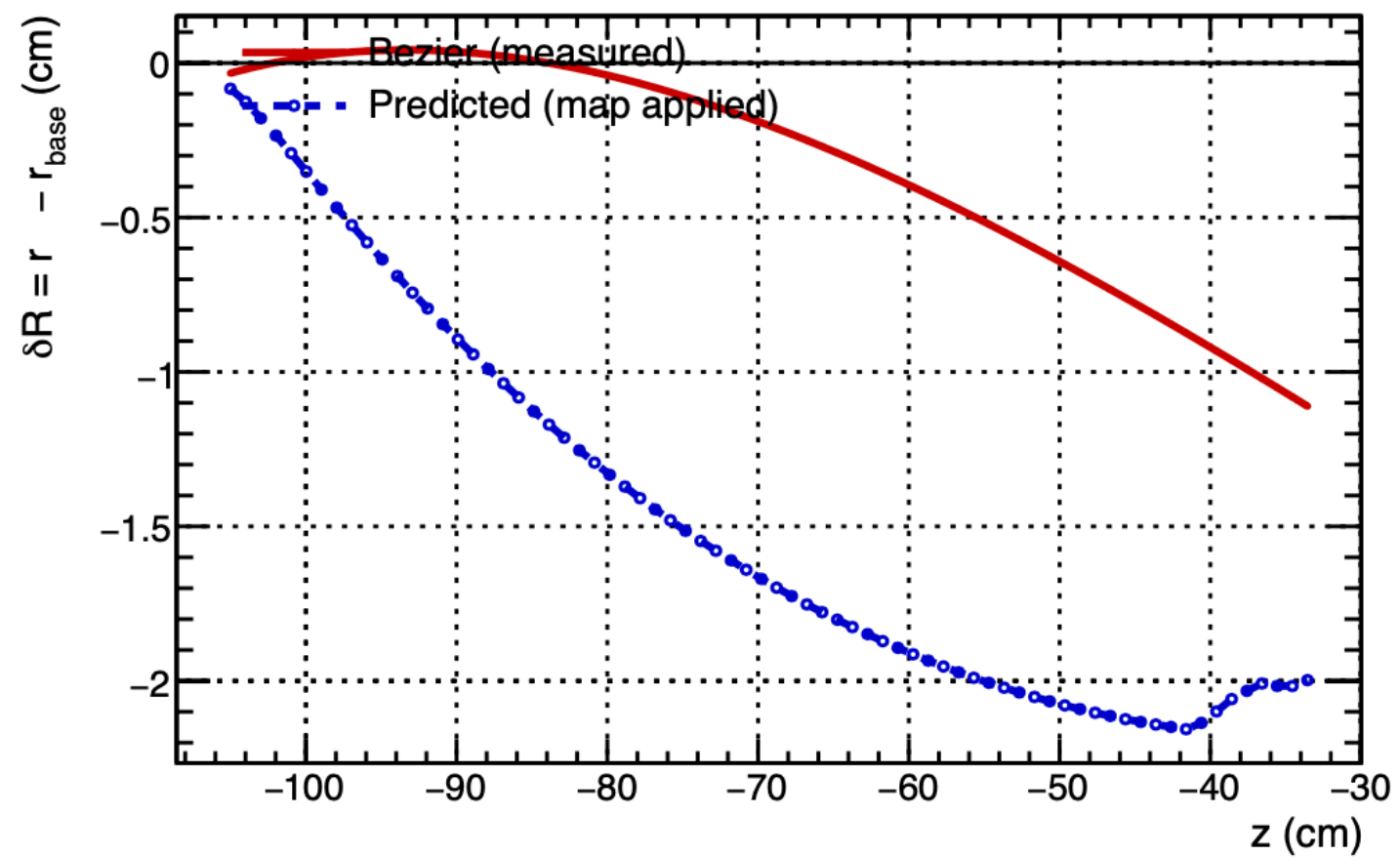
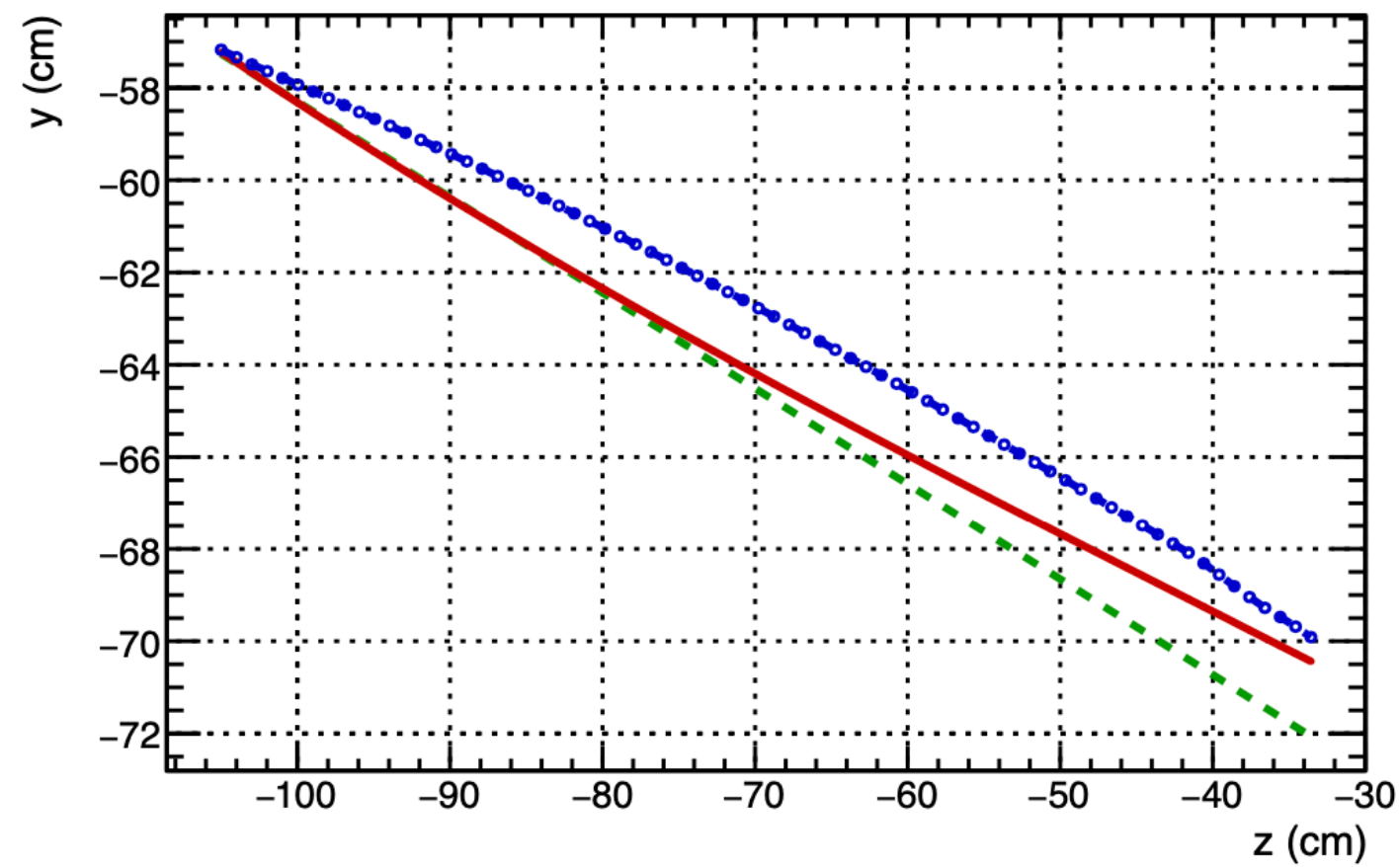
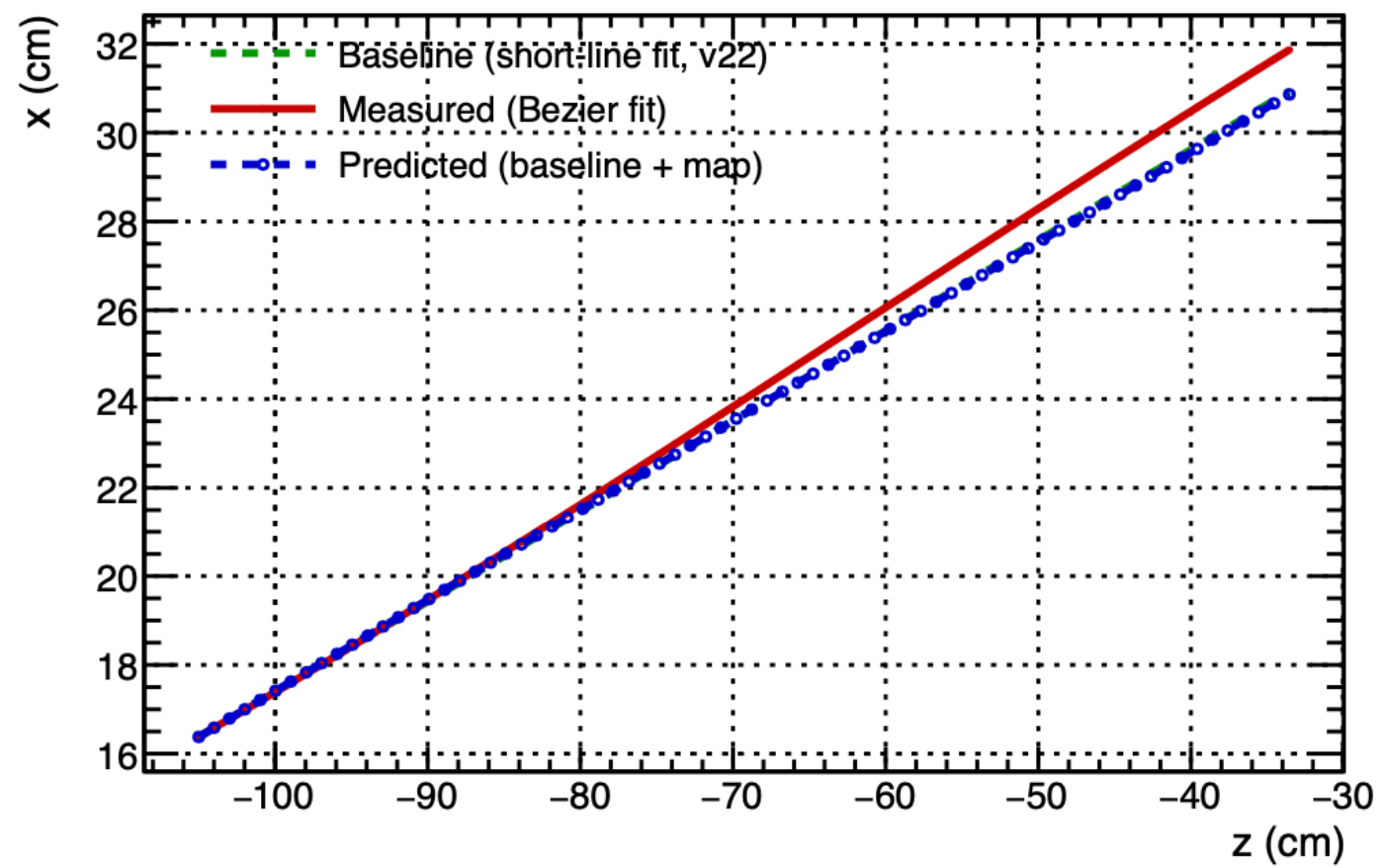
- We define parameter  $t \in [0, 1]$  and 4 control points.  $z$  is purely linear:  $z(t) = z_{\text{Min}} + t \cdot (z_{\text{Max}} - z_{\text{Min}})$ , 4 control points are evenly spaced in  $z$ .
- The control points are parameterised as deviations from the original straight-line prediction:

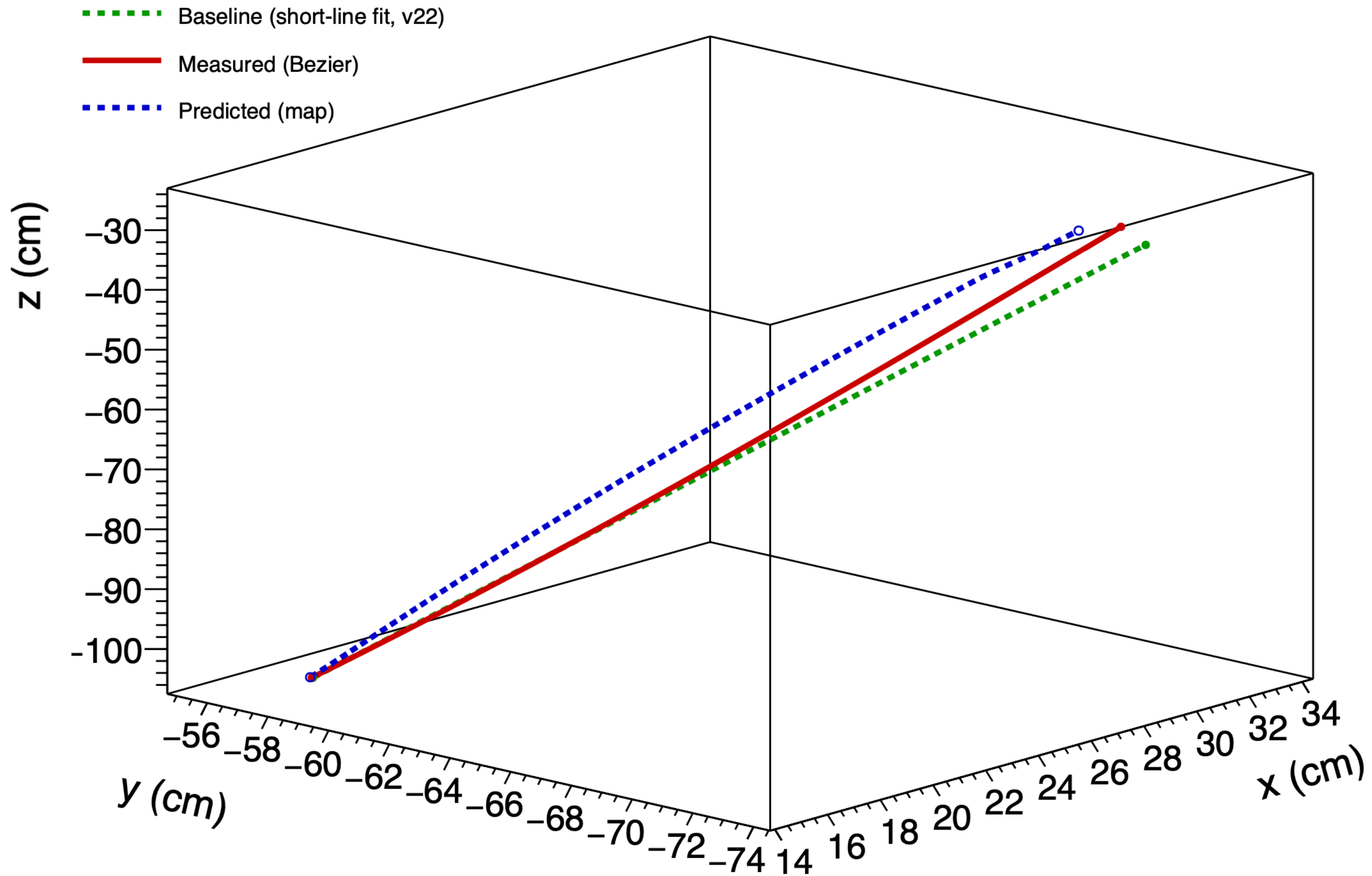
$$c_{x,i} = x_{\text{line}}(z_i) + \delta c_{x,i}, \quad c_{y,i} = y_{\text{line}}(z_i) + \delta c_{y,i}, \quad i = 0, 1, 2, 3$$

- The 8 free parameters fitted by Minuit:  $\boldsymbol{\theta} = (\delta c_{x,0}, \delta c_{y,0}, \delta c_{x,1}, \delta c_{y,1}, \delta c_{x,2}, \delta c_{y,2}, \delta c_{x,3}, \delta c_{y,3})$

# Run 80032 | side0 3D z=[-120,-20] nVox=799

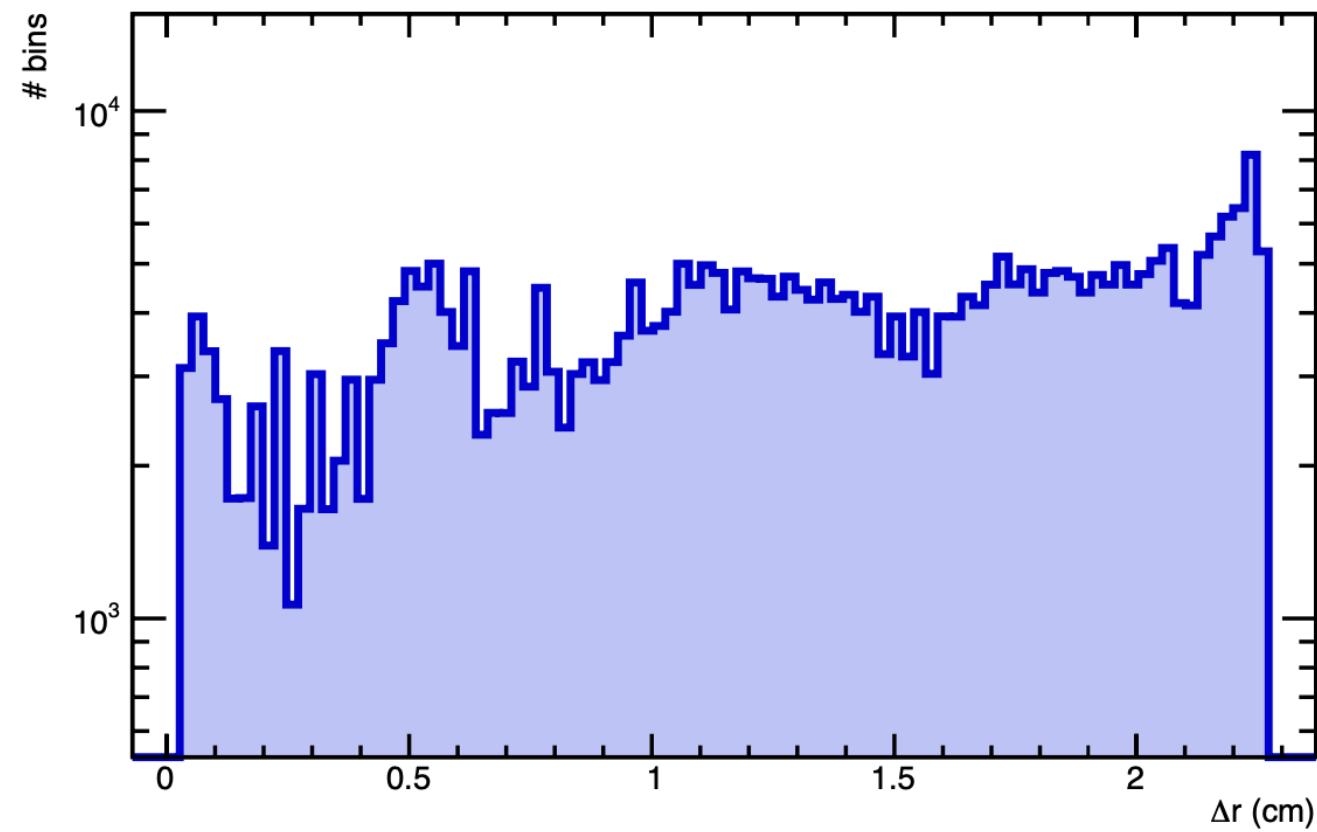




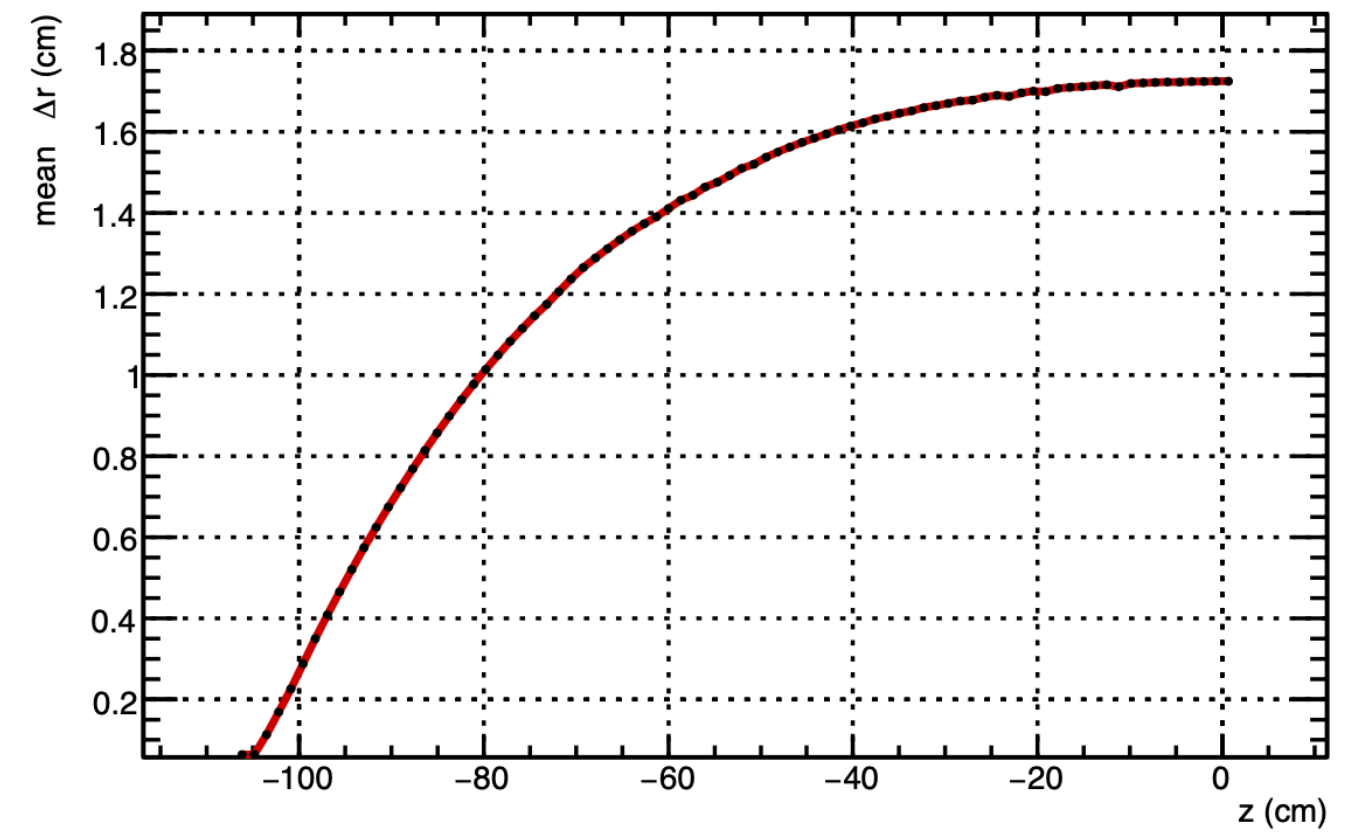


# Back Up

$\Delta r$  [neg z (South)] QA profiles (averaged over the two other axes)  
Distribution of bin values

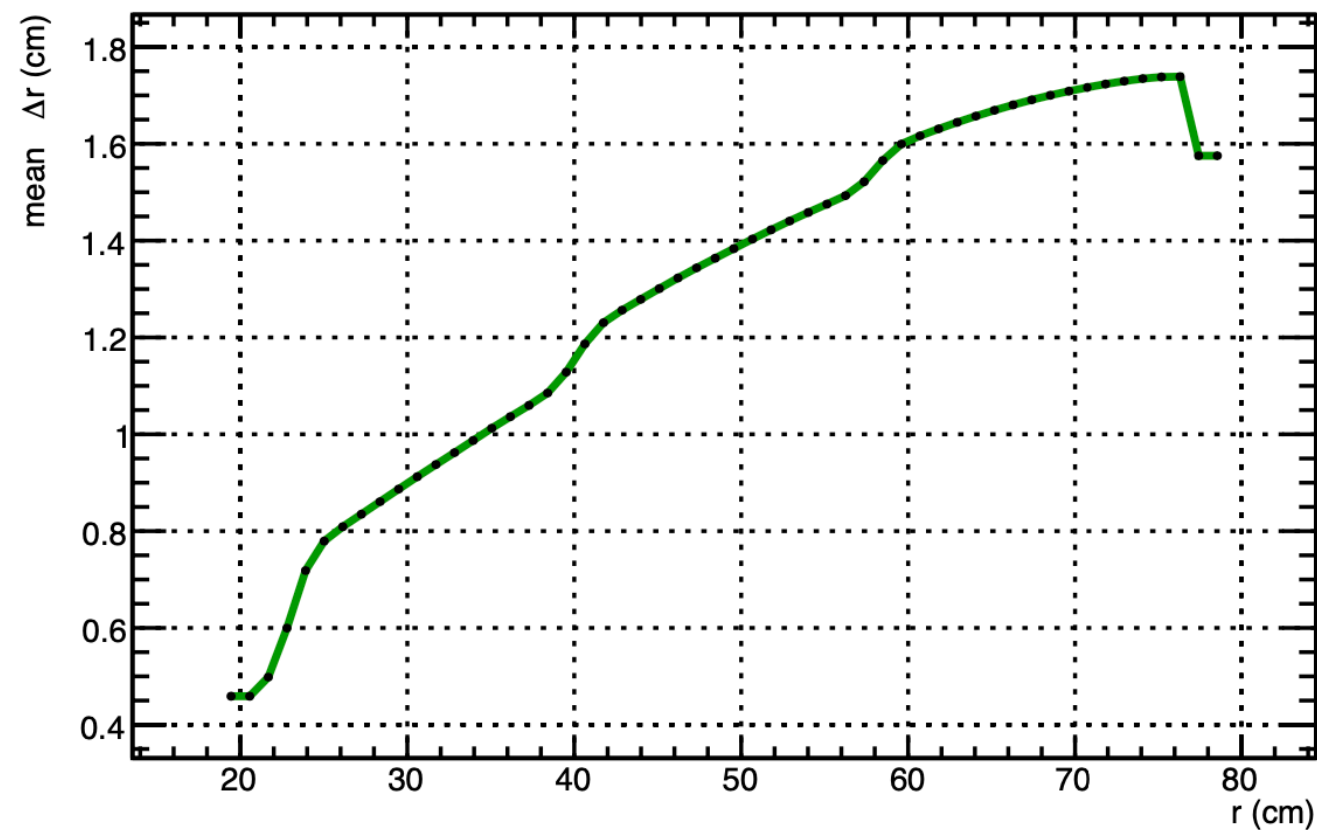


Mean distortion vs  $z$  ( $\langle \Delta r \rangle_{\phi,r}$ )

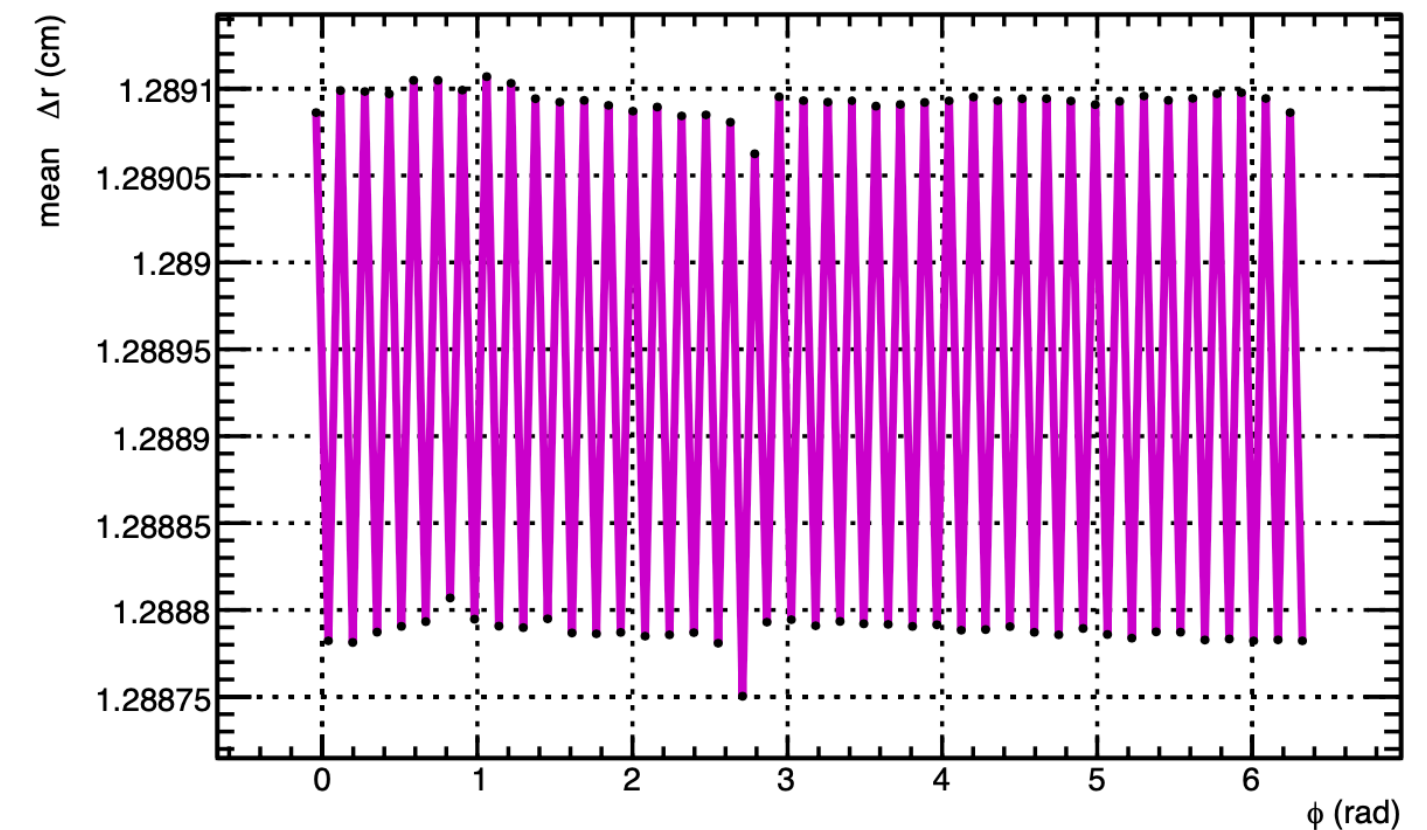


# Static Distortion Map: $\Delta r$ drift from $(r, \phi, z)$ 1D projection

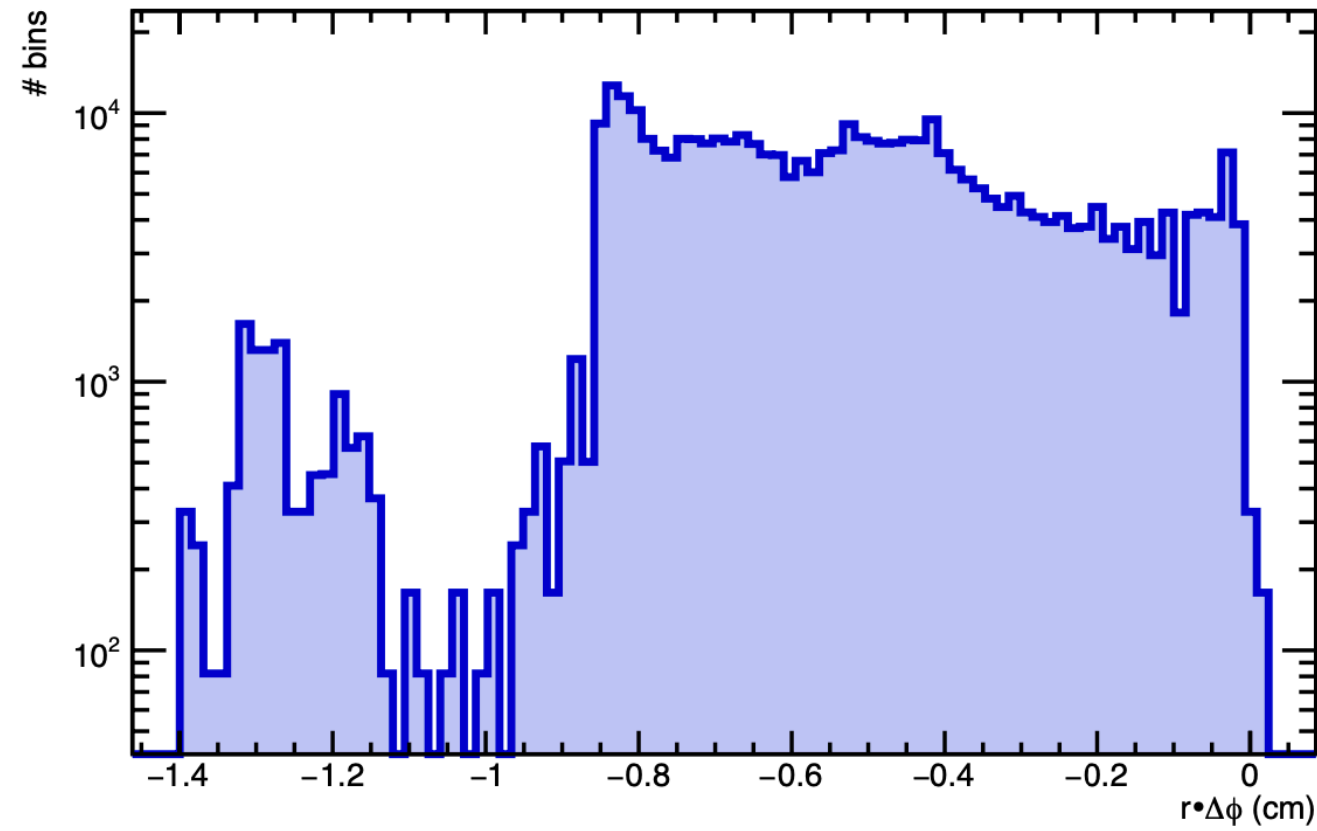
Mean distortion vs  $r$  ( $\langle \Delta r \rangle_{\phi,z}$ )



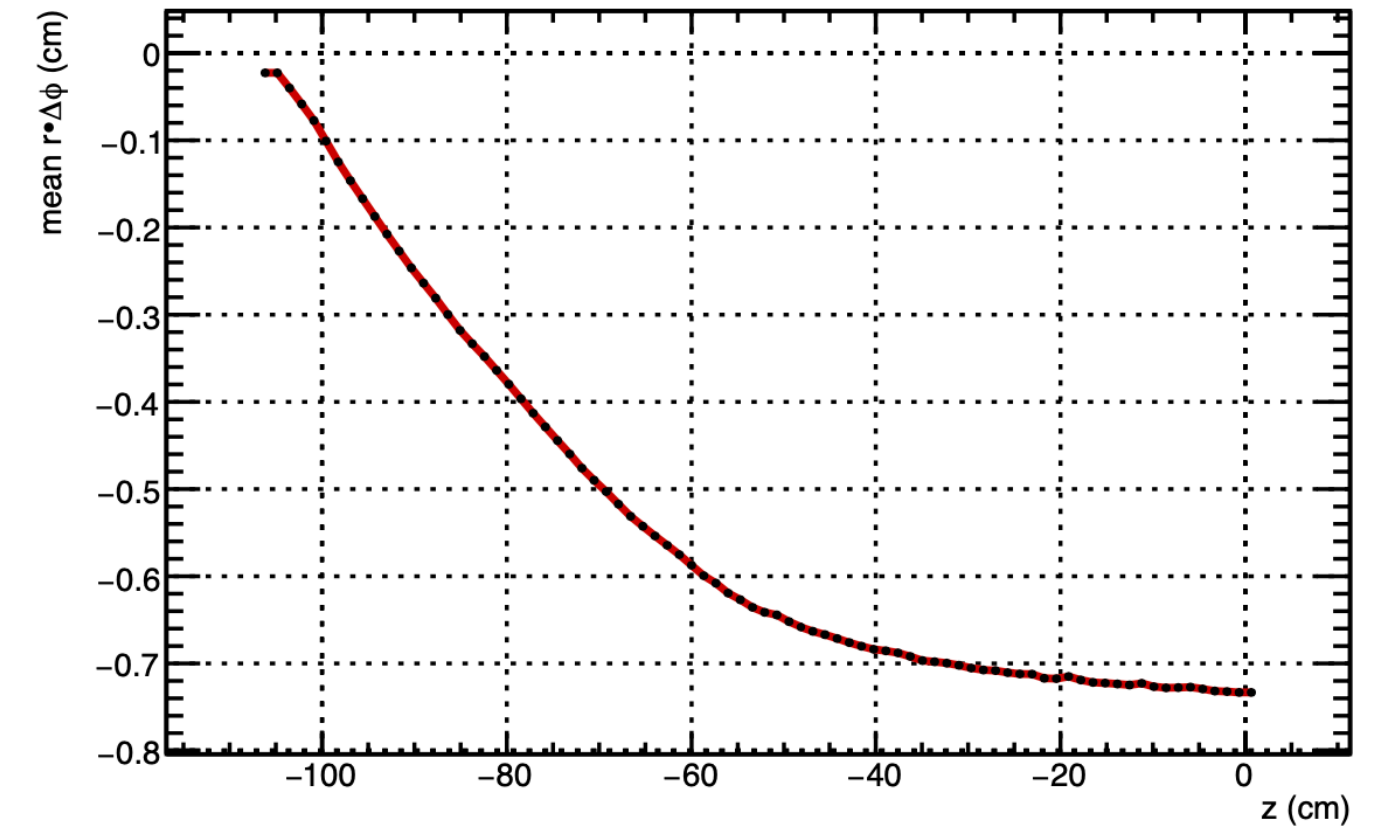
Mean distortion vs  $\phi$  ( $\langle \Delta r \rangle_{r,z}$ )



$r \cdot \Delta\phi$  [neg z (South)] QA profiles (averaged over the two other axes)  
Distribution of bin values

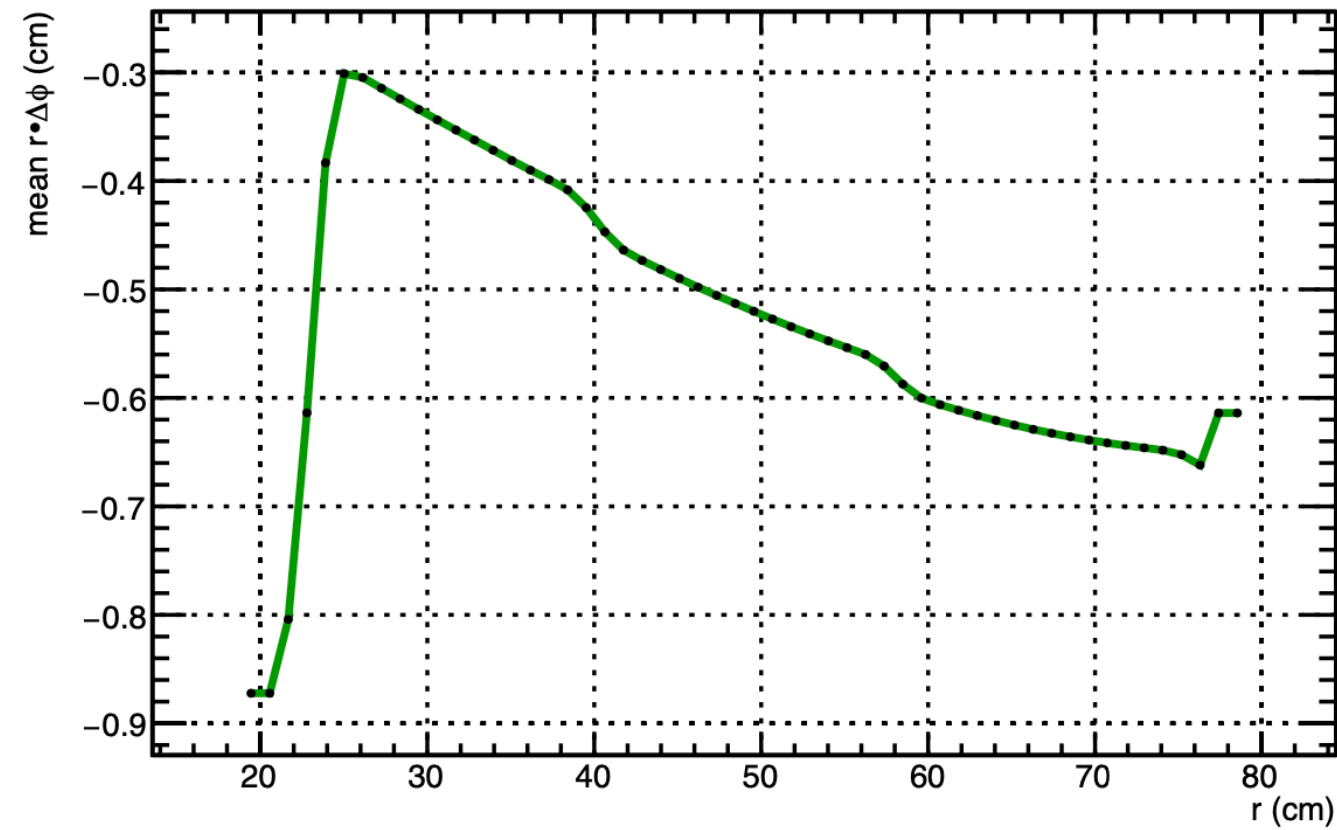


Mean distortion vs z ( $\langle r \cdot \Delta\phi \rangle_{\phi,r}$ )



# Static Distortion Map: $r \Delta\phi$ drift from $(r, \phi, z)$ 1D projection

Mean distortion vs r ( $\langle r \cdot \Delta\phi \rangle_{\phi,z}$ )



Mean distortion vs  $\phi$  ( $\langle r \cdot \Delta\phi \rangle_{r,z}$ )

